

Summerschool – MPG-UBC-UTokyo Center
X-rays for the study of quantum materials

High resolution RIXS for the study of strongly-correlated and novel materials



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Summary

RIXS: resonant inelastic x-ray scattering

1. From XAS to RIXS: a second order process
2. RIXS instrumentation
3. Orbital (*dd*) excitations
4. Magnetic excitations
5. Phonons and charge order
6. REXS: the elastic part of RIXS spectra
7. Time resolved RIXS

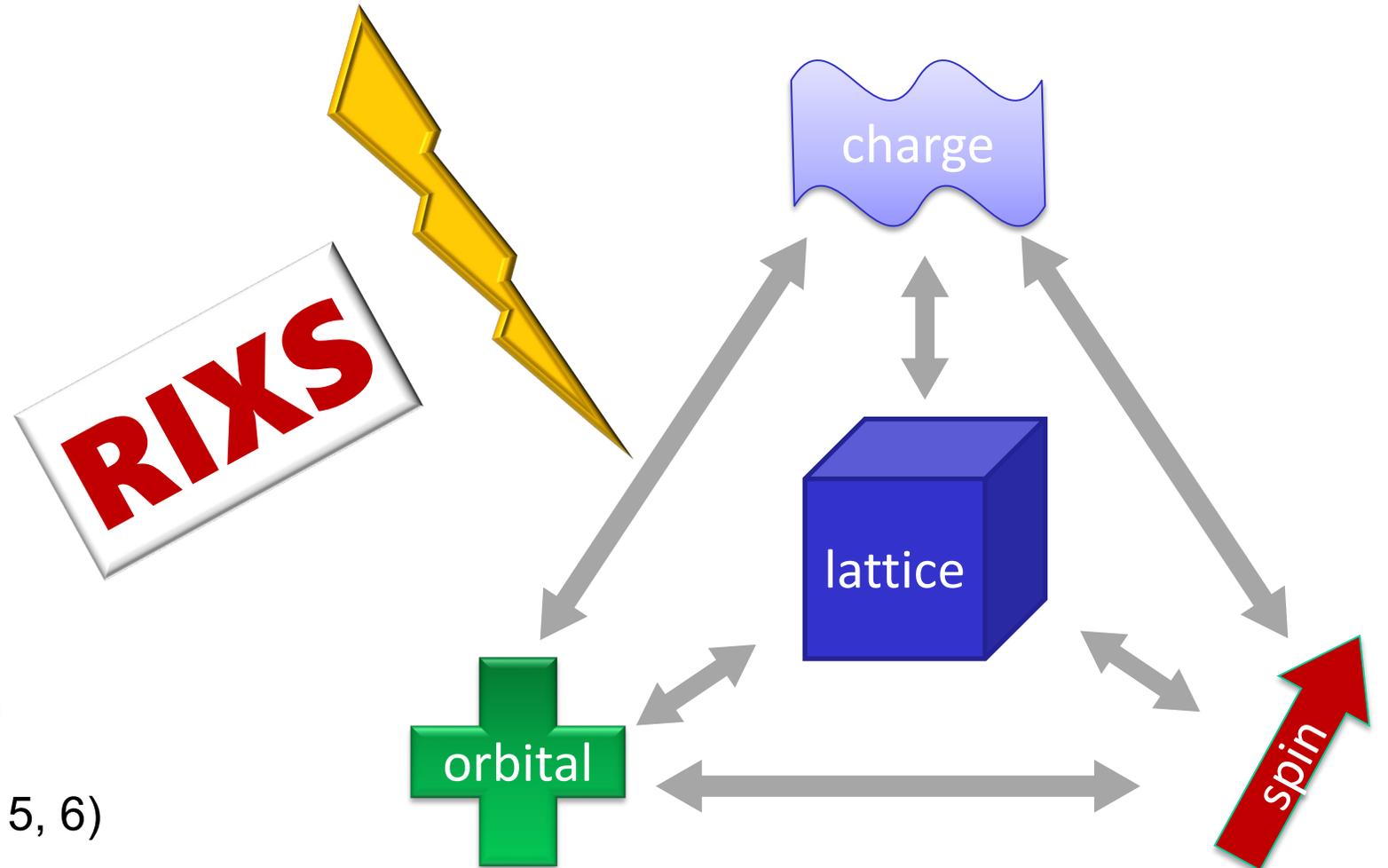
One probe for several degrees of freedom

1. Energy loss spectroscopy
2. Momentum resolution
3. Coupling to
 - a. Charge
 - b. Spin
 - c. Orbital
 - d. Lattice
4. Bulk sensitivity
5. Good energy resolution
6. Decent count rate

electrons (1, 2, 3, 5, 6)

neutrons (1, 2, 3b, 3d, 4, 5)

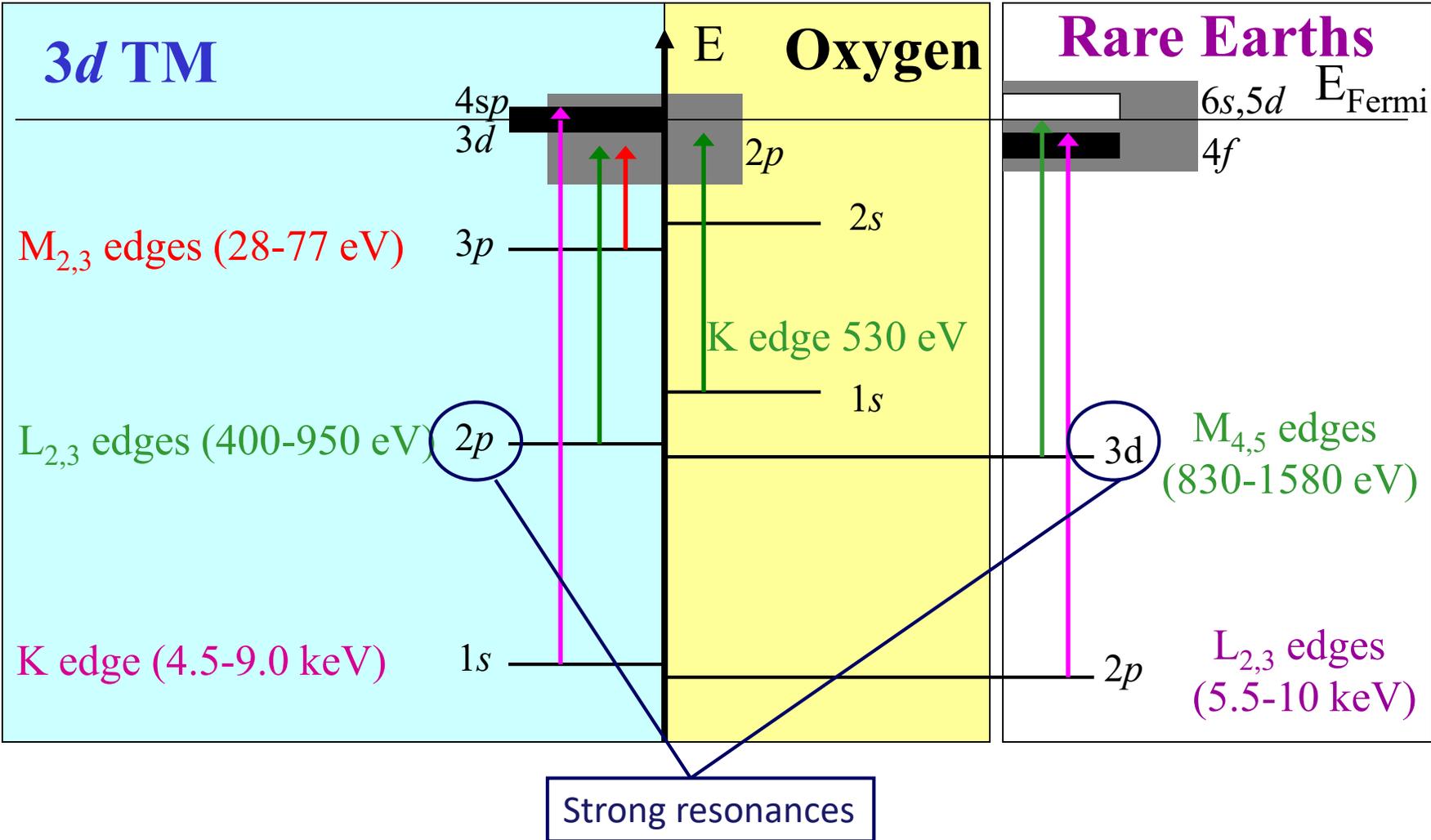
photons (1, 2, 3a, 3c, 3d, 4, 5, 6)



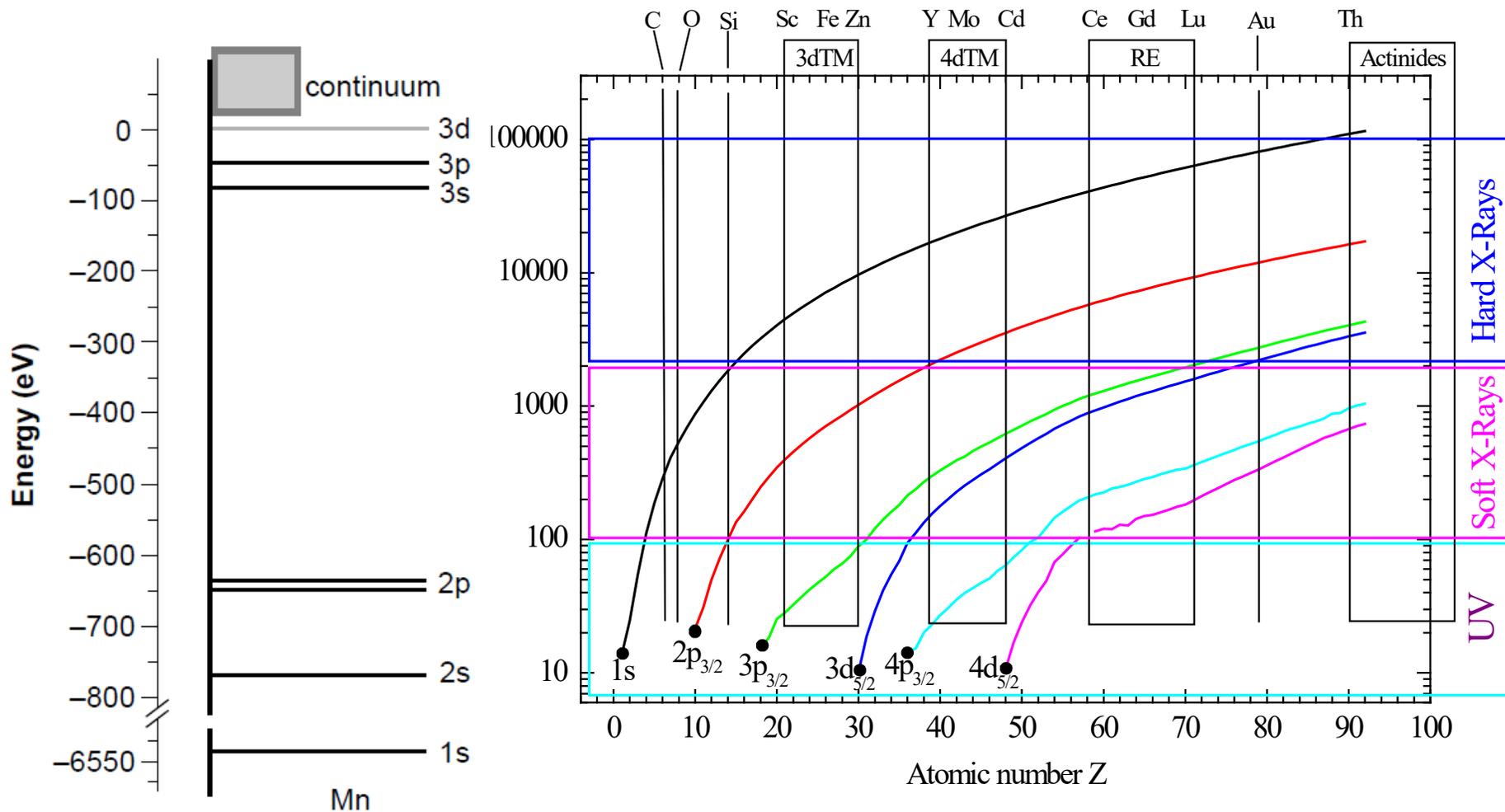
Part 1

FROM XAS TO RIXS

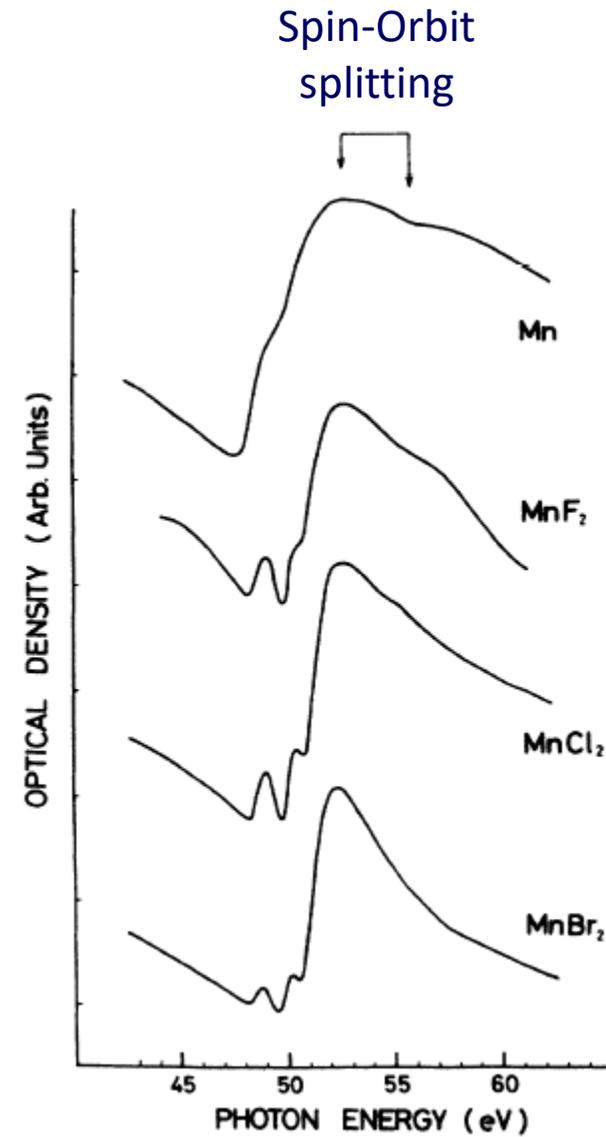
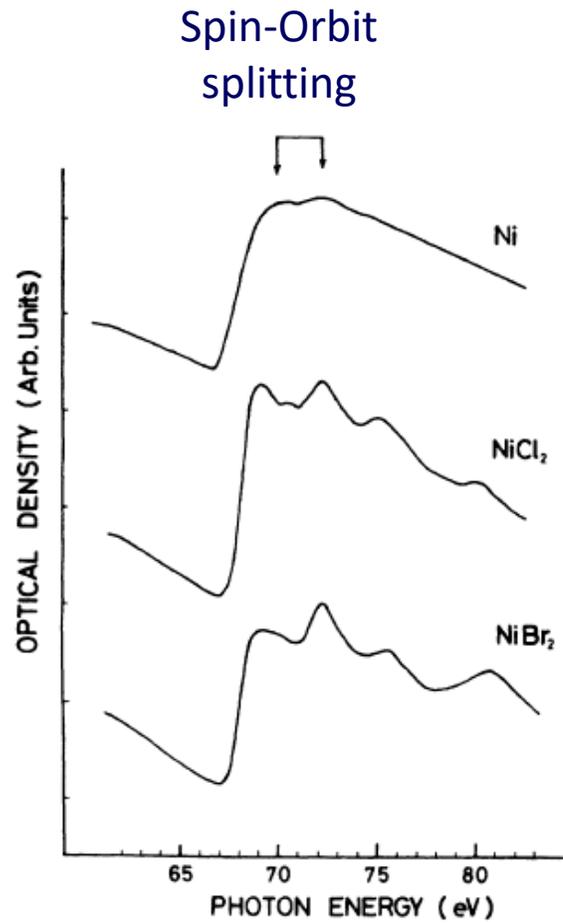
Resonances in the XAS



Core level binding energies and edges

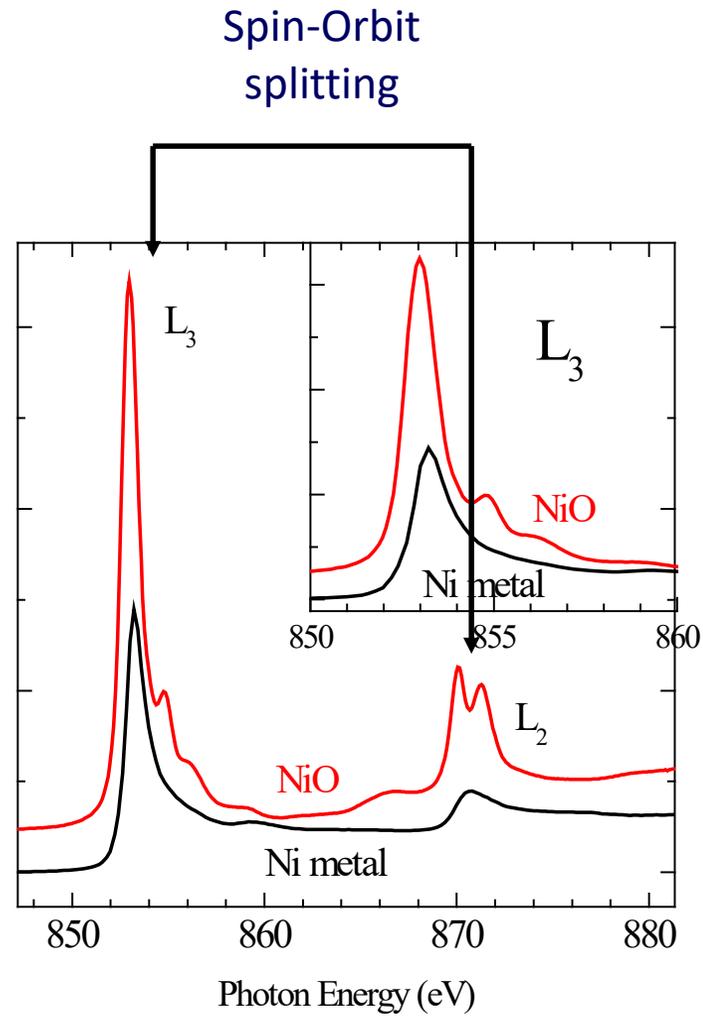


3p. M_{2,3} edge XAS

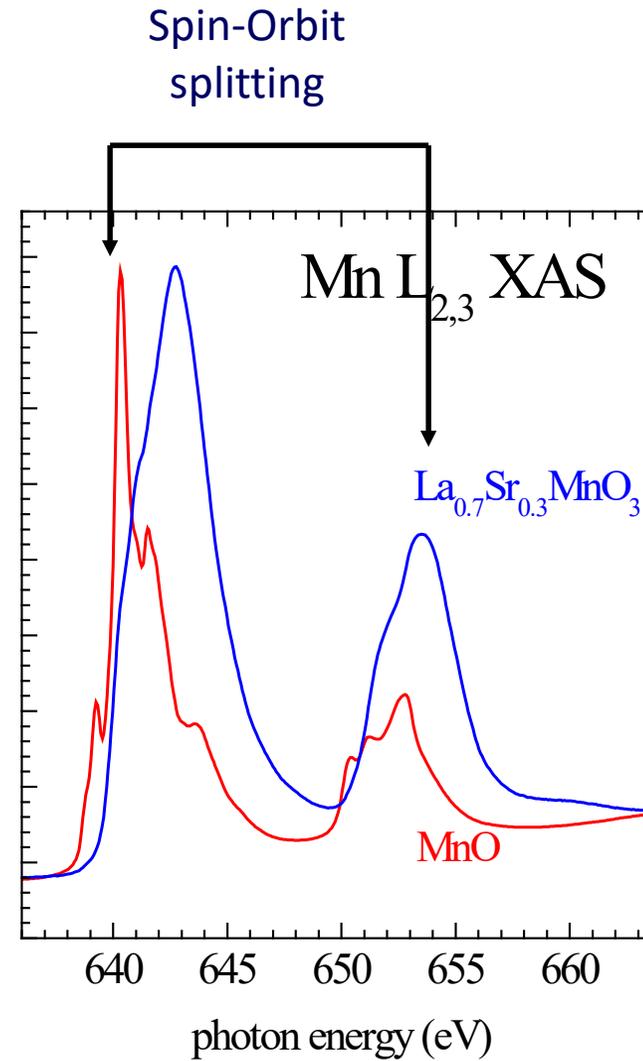


Source: S. Nakai, *et al* PRB 9, 1870 (1974)

2p. L_{2,3} edge XAS



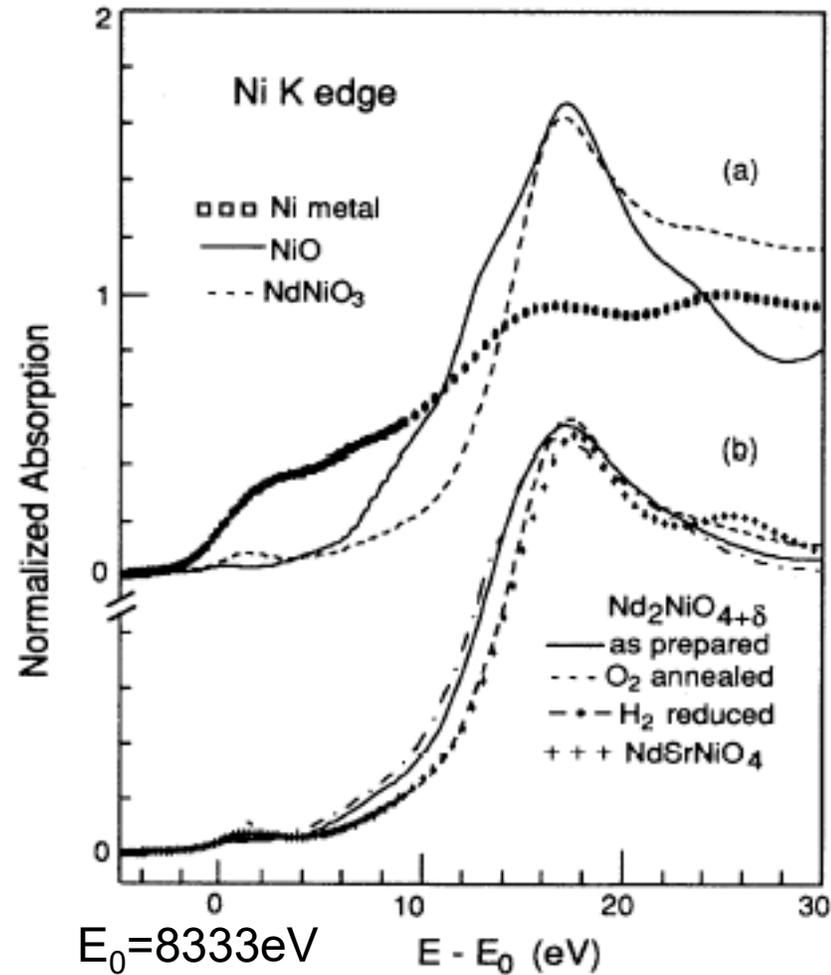
Source: G. Ghiringhelli, N.B. Brookes *et al* unpublished



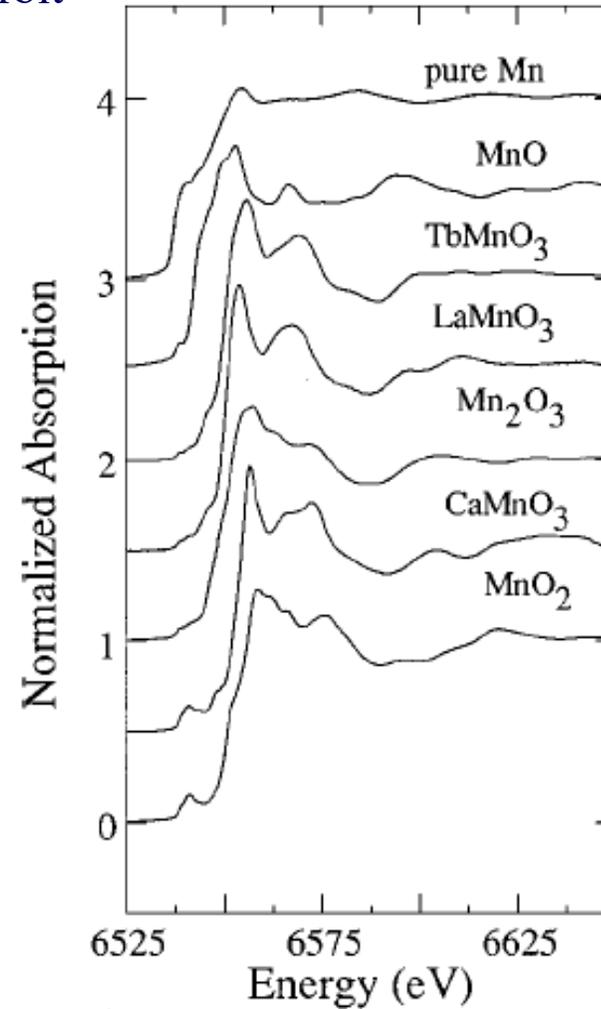
Source: C. Aruta, G. Ghiringhelli *et al* unpublished

1s. Ni and Mn K edge XAS

NO Spin-Orbit
splitting

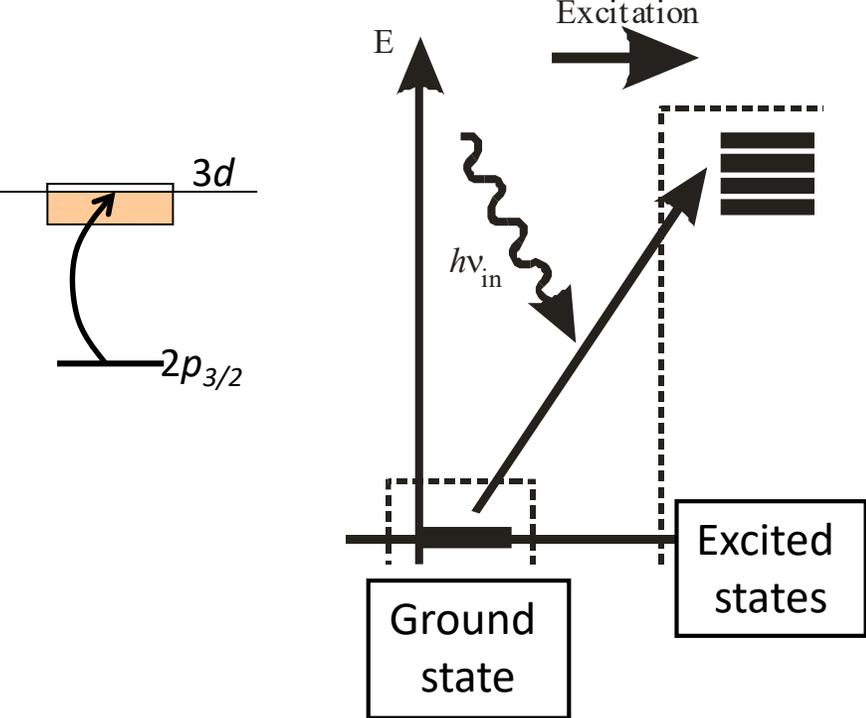


Source: Z. Tan *et al* Phys. Rev. B **47**, 12365 (1993)



Source: G. Subias, *et al* PRB **56**, 8183 (1997)

L₃ XAS and multiplets



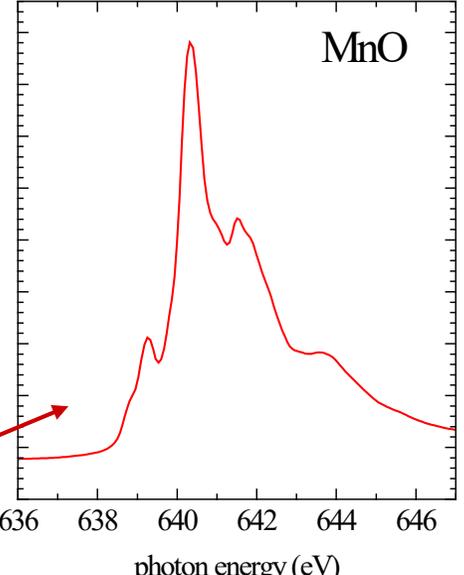
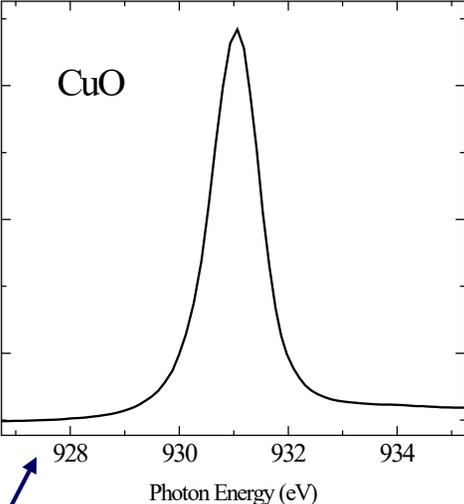
$$3d^n \rightarrow 2p^5 3d^{n+1}$$

CuO: $3d^9 \rightarrow 3d^{10}$

NiO: $3d^8 \rightarrow 3d^9$
 MnO: $3d^5 \rightarrow 3d^6$

One single peak

Many peaks



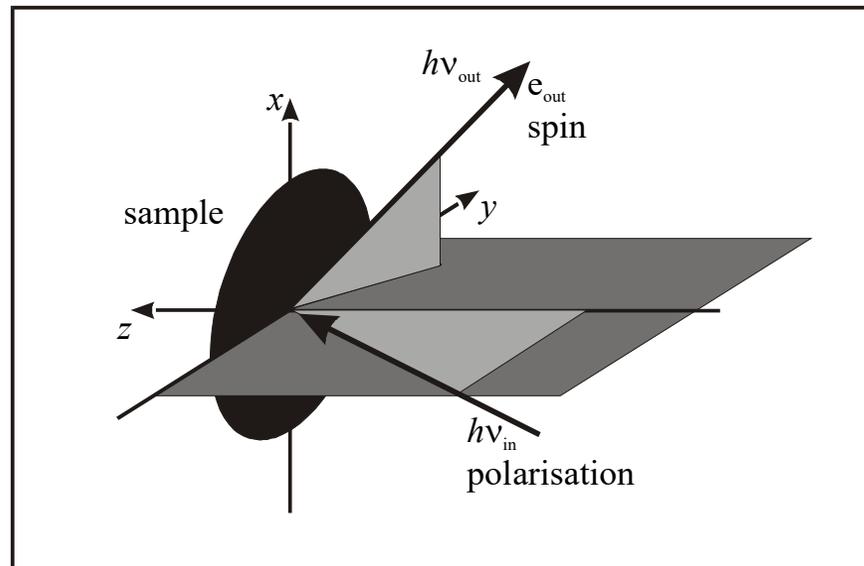
Second order processes: what after XAS?

What about looking at the emitted x-rays after a resonant absorption?

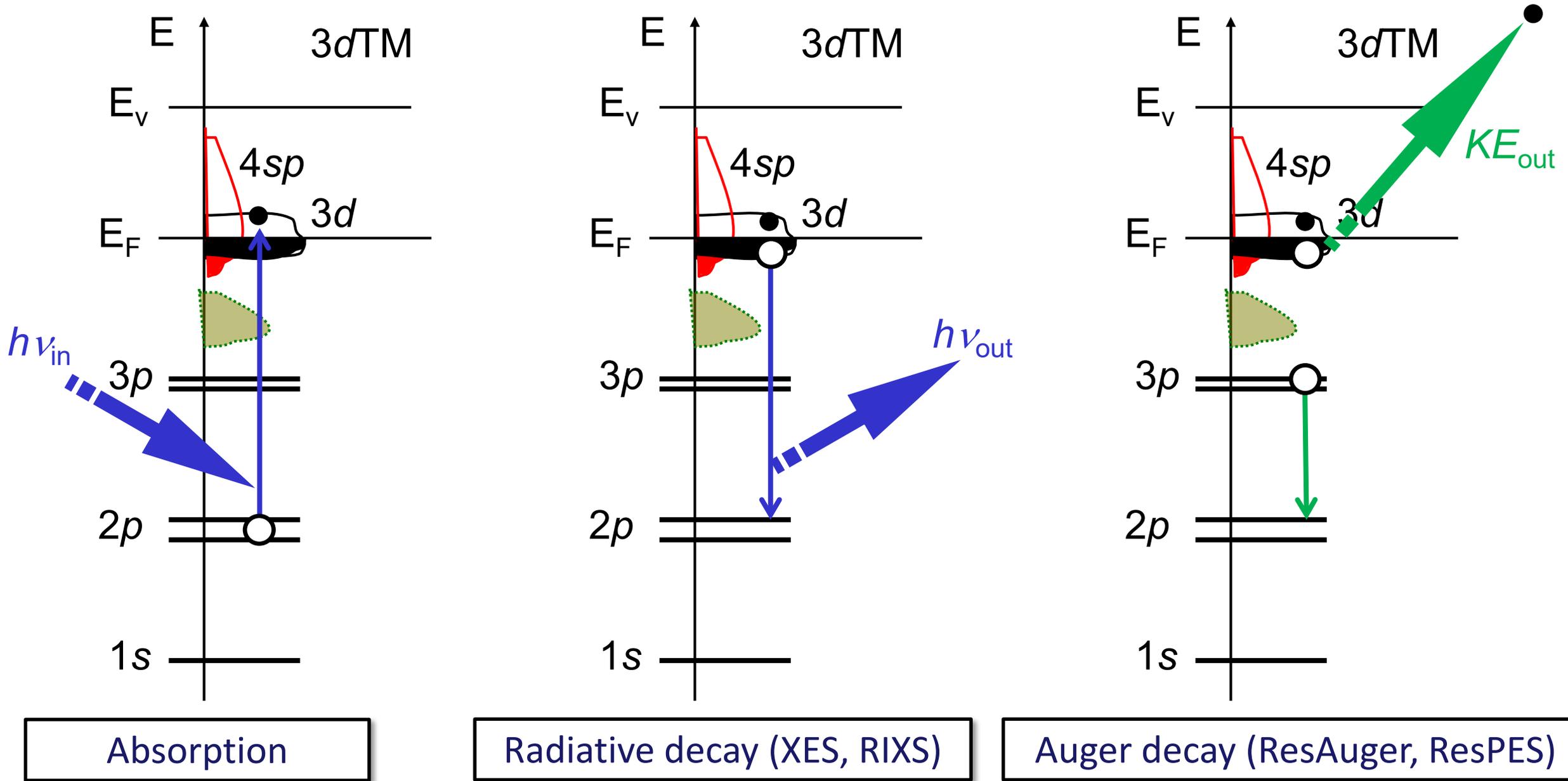
We can access local and collective excitations.

Electric dipole selection rules are not a limitation.

Photon momentum can be used to probe dispersion.

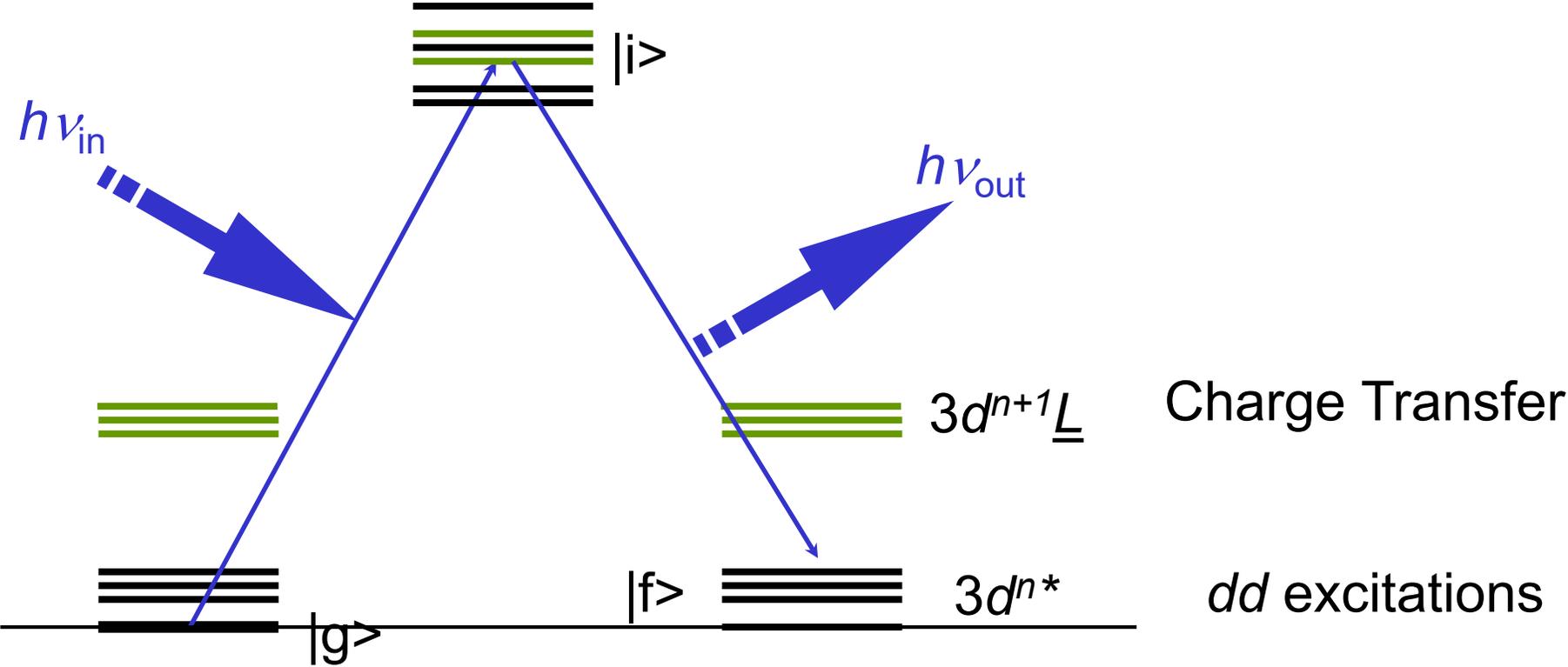


Decay of the core hole after a resonant absorption



RIXS: a resonant inelastic scattering

$$E_{\text{transferred}} = h\nu_{\text{in}} - h\nu_{\text{out}}$$



RIXS probes charge neutral local excitations

RIXS: a 2nd order process described by Kramers-Heisenberg formula

Several spectral features coming from different final states via the same set of intermediate states

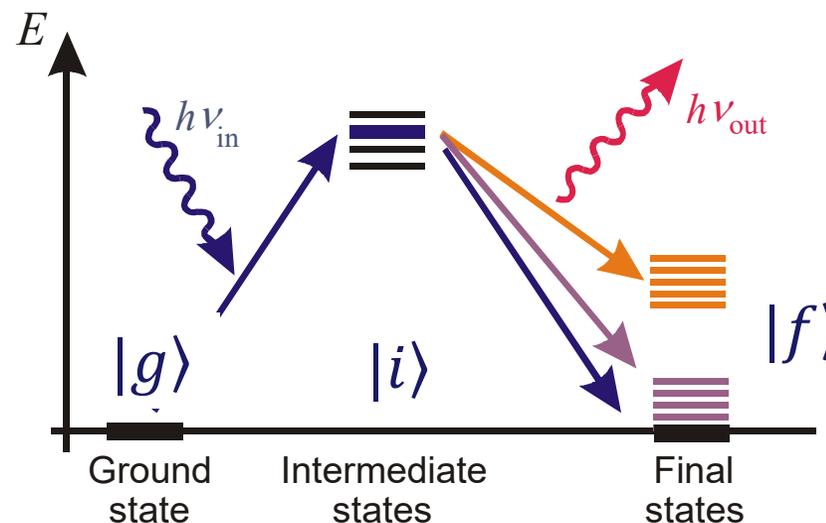
The intermediate state is not known: we sum over amplitudes given by different intermediate states

Intensity :

$$\sum_f \left| \sum_i \frac{\langle f | T^{(e)} | i \rangle \langle i | T^{(a)} | g \rangle}{E_g + h\nu_{in} - E_i - i\Gamma_i} \right|^2 \times \frac{\Gamma_f / \pi}{(E_g + h\nu_{in} - E_f - h\nu_{out})^2 + \Gamma_f^2}$$

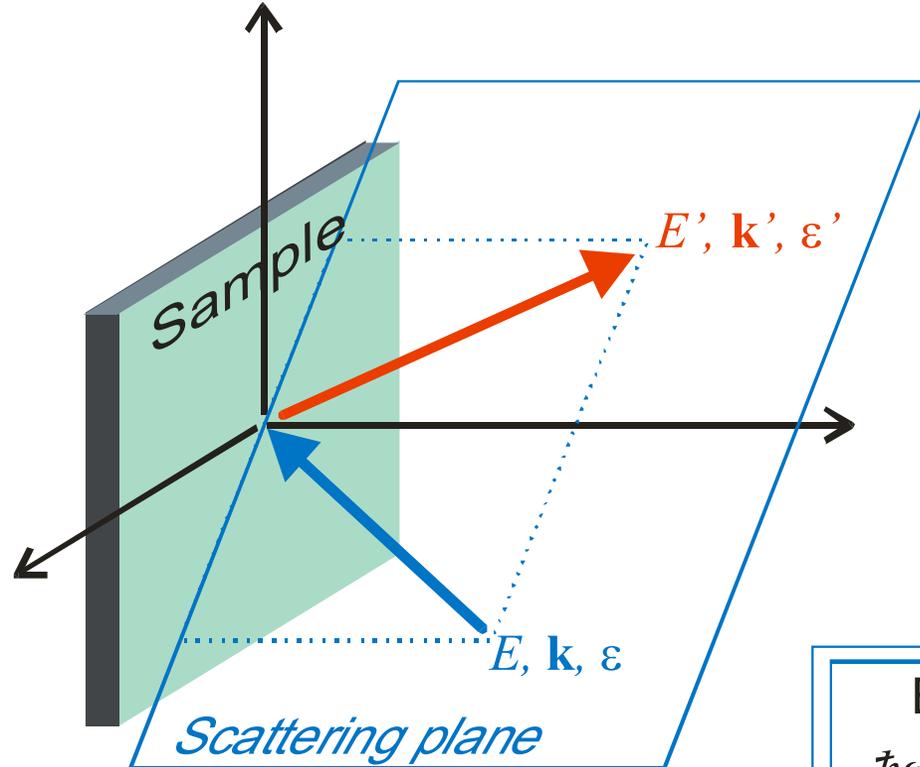
Resonance in the excitation step

Energy transfer from photon to sample



Lorentzian broadening due to final state lifetime

L edge RIXS : energy and momentum transfer

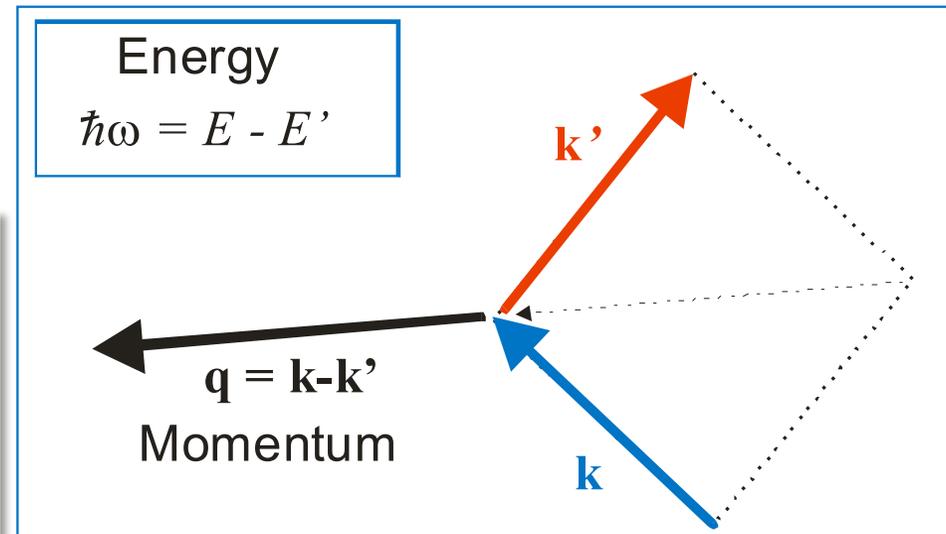


Resonant Inelastic X-ray Scattering:

- an energy loss experiment
- made with photons of high energy
- at a core absorption resonance

Conservation laws:

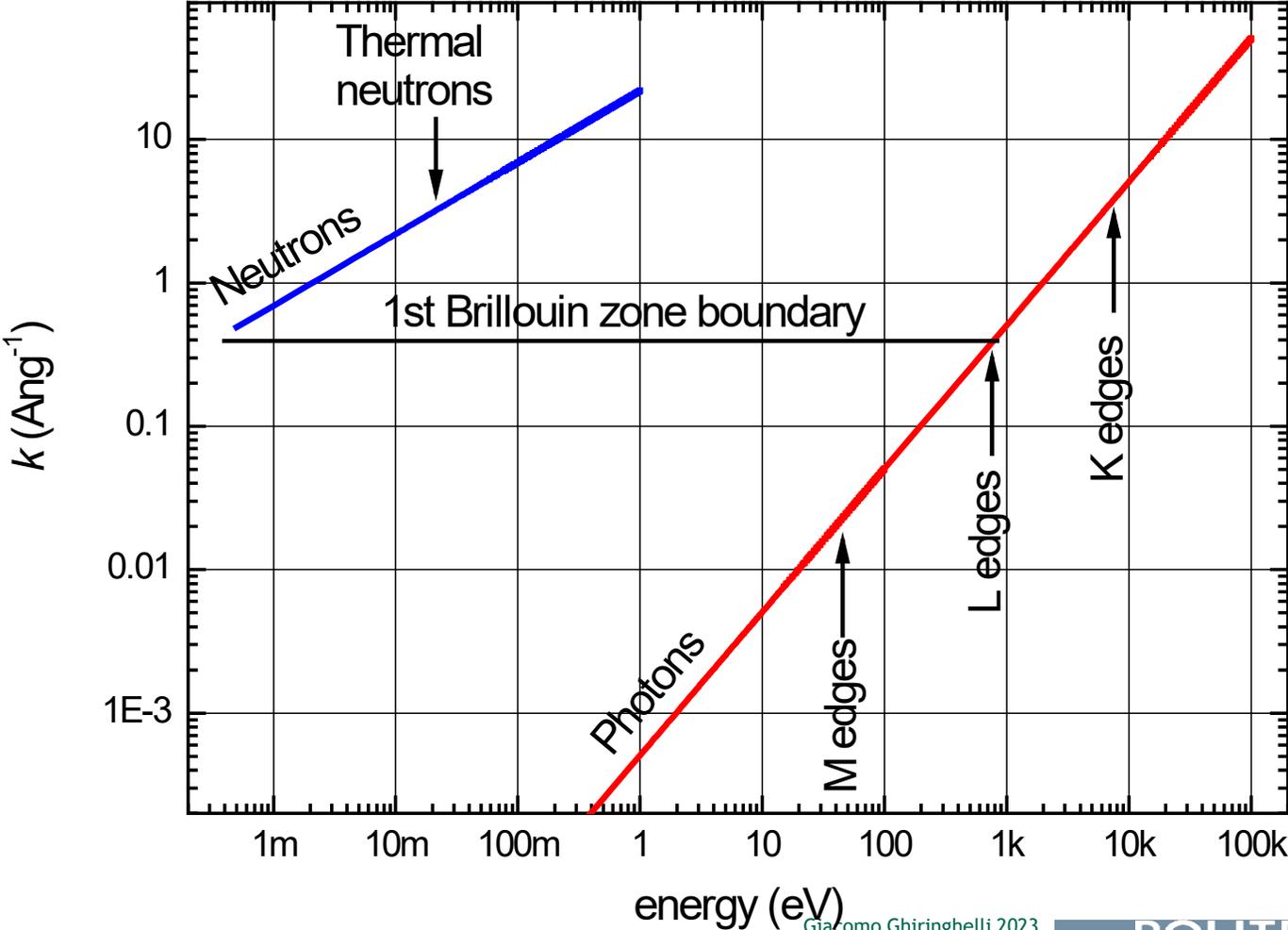
- Energy
- Momentum
- "Angular momentum"



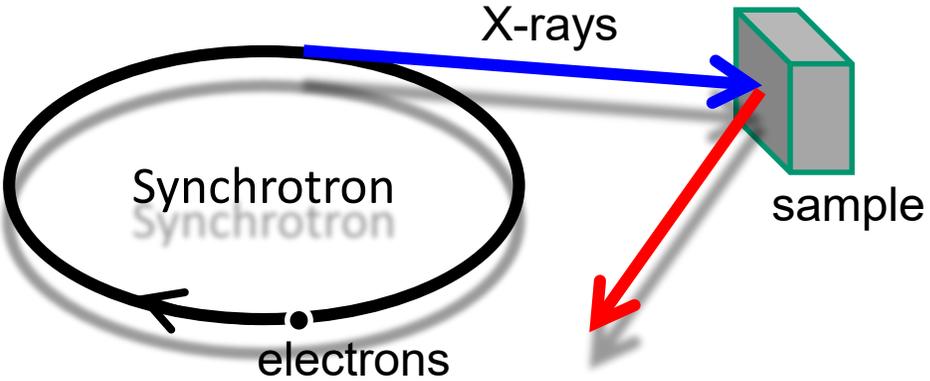
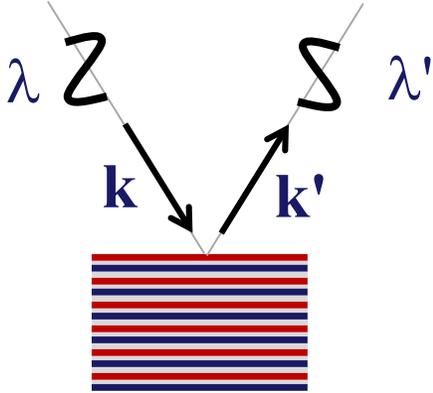
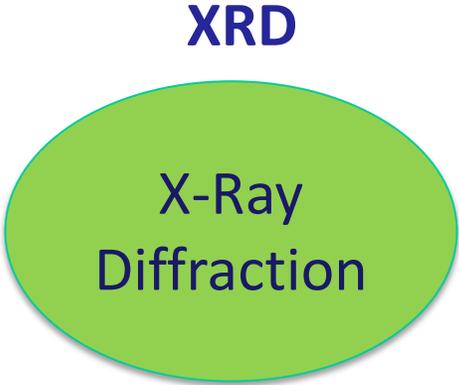
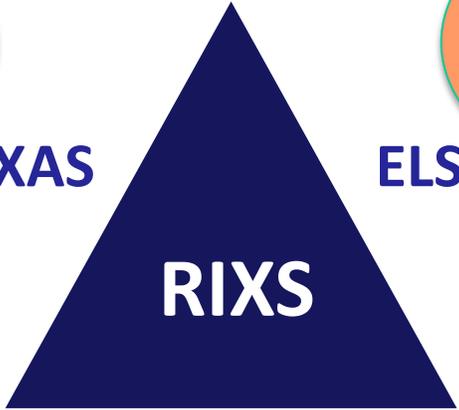
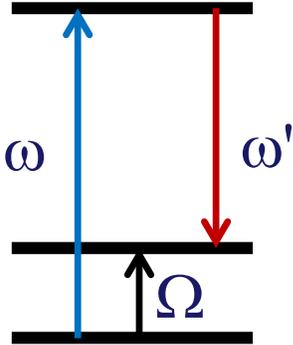
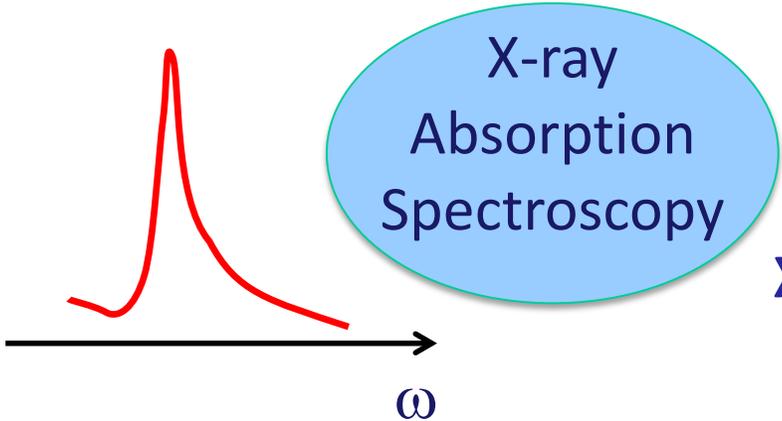
Photon momentum and kinematics

Photons vs Neutrons: energy and momentum

Wavevector of particles used in inelastic scattering



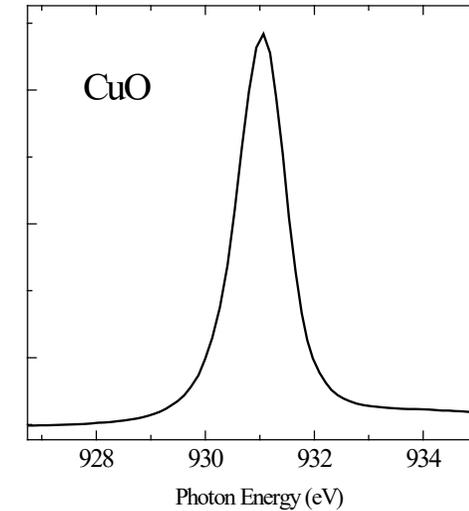
Resonant Inelastic X-ray Scattering



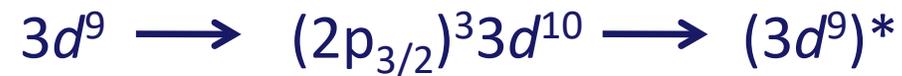
Cuprates: the “easy” case

In cuprates Cu is divalent: $\text{Cu}^{2+} \leftrightarrow 3d^9$

This makes XAS almost trivial: 1 peak only

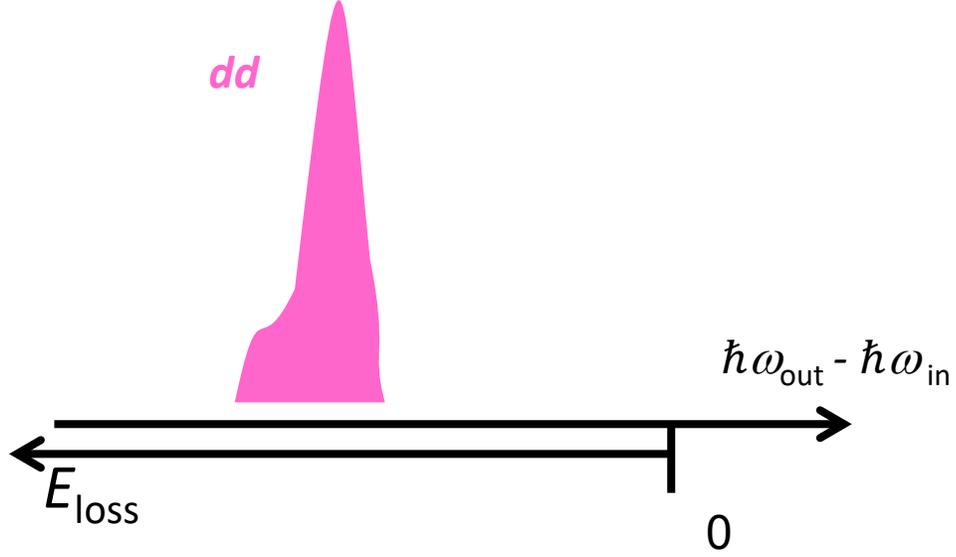
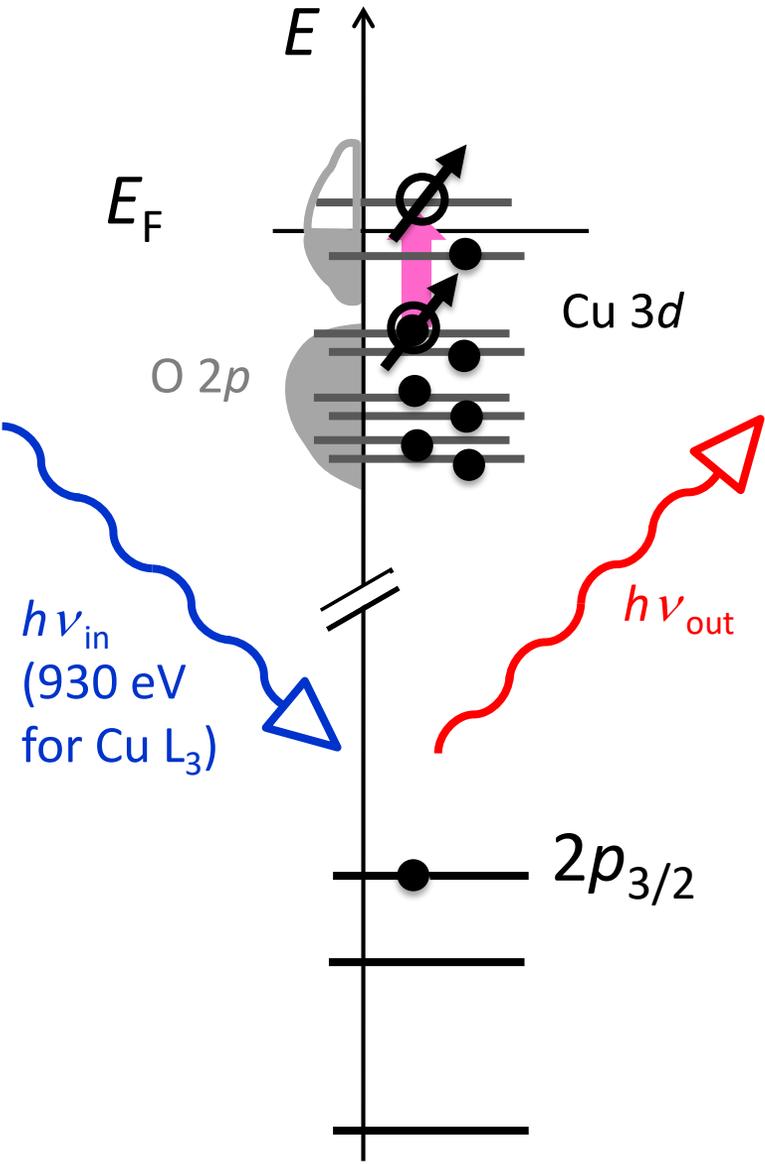


RIXS can be calculated even by hand:

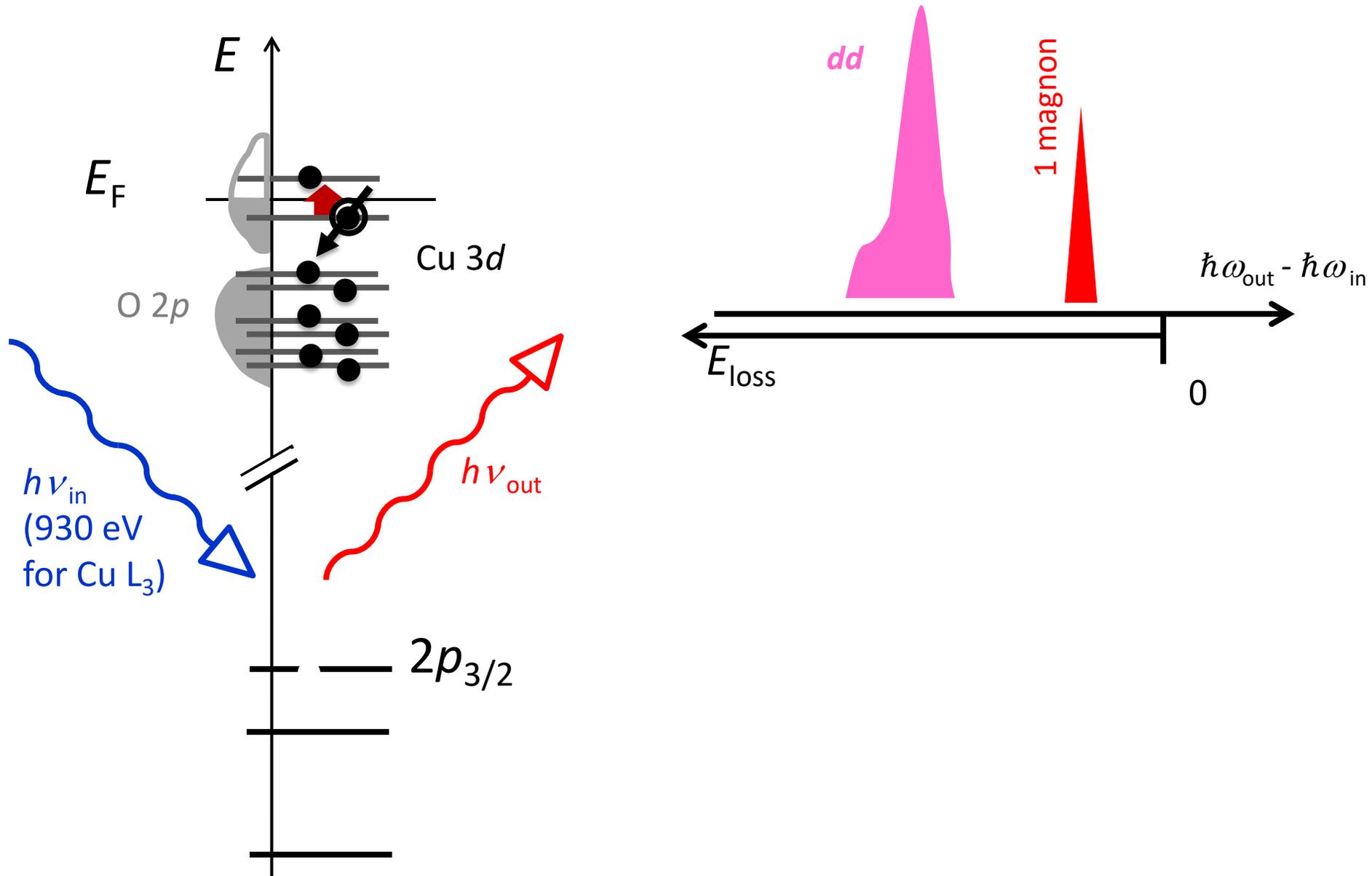


Even for magnetic excitations (spin waves),
because fast collision approximation is a very
good approximation

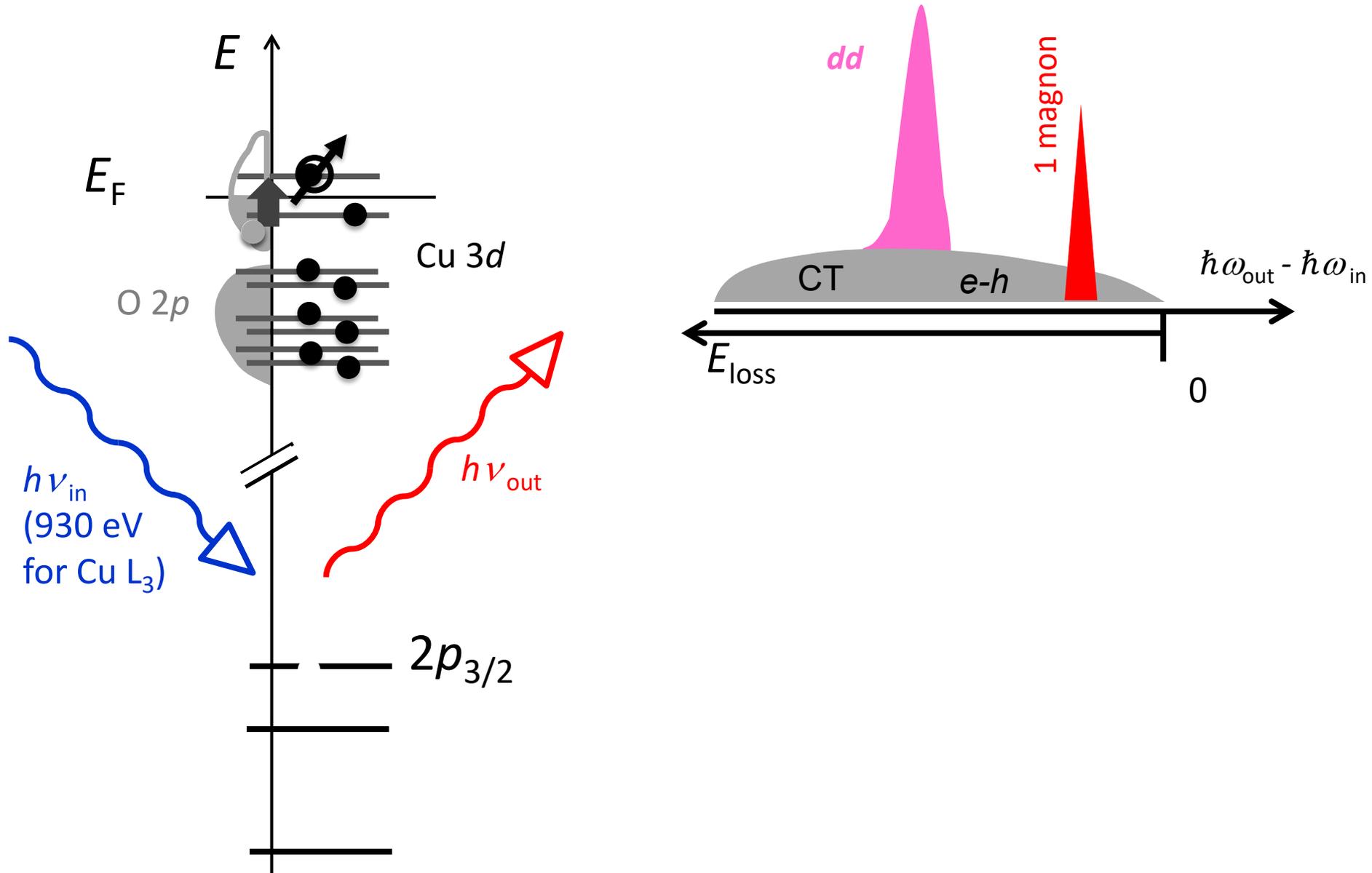
RIXS at the Cu L₃ resonance



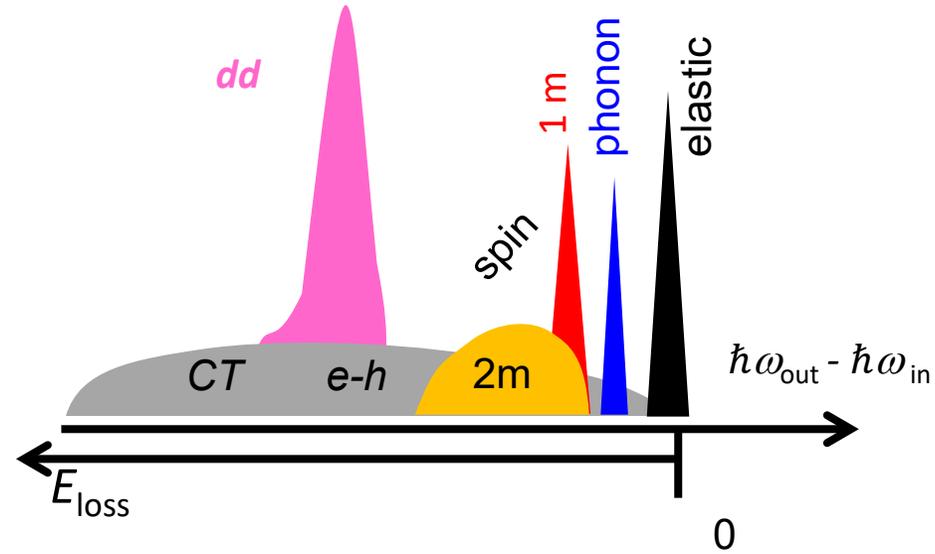
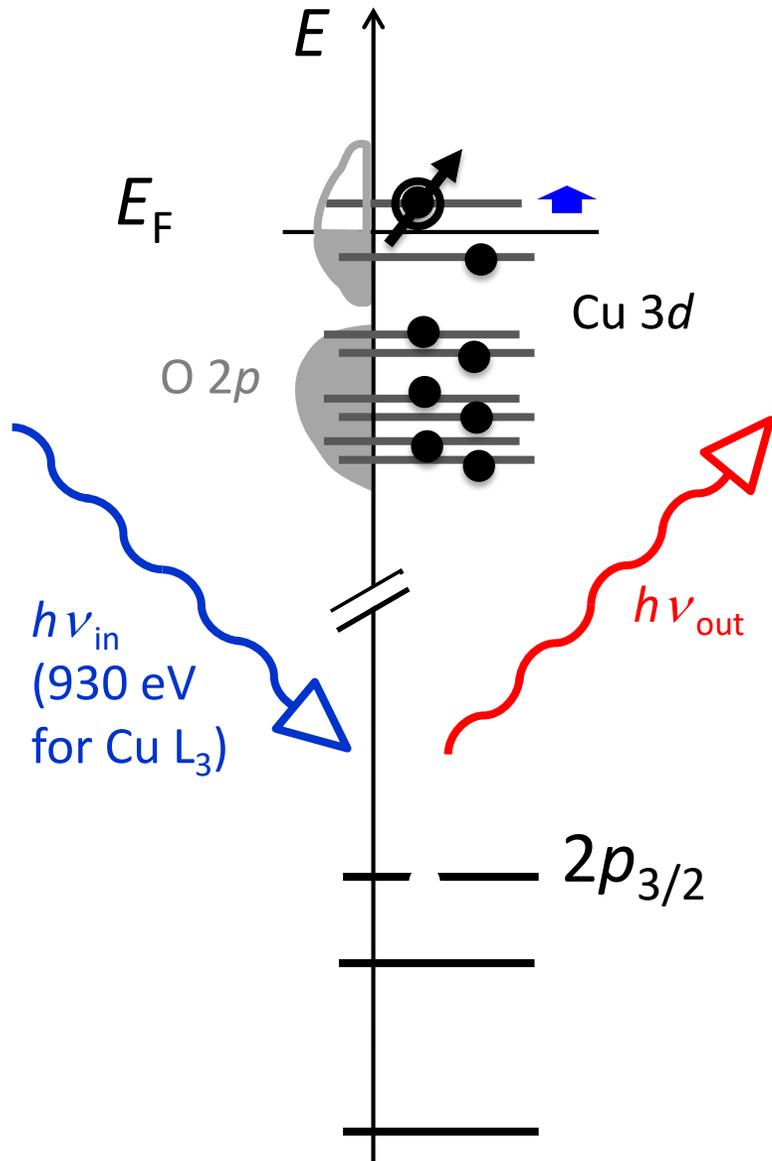
Cu L₃ RIXS: magnon excitations



Cu L₃ RIXS: charge transfer and *e-h* excitations



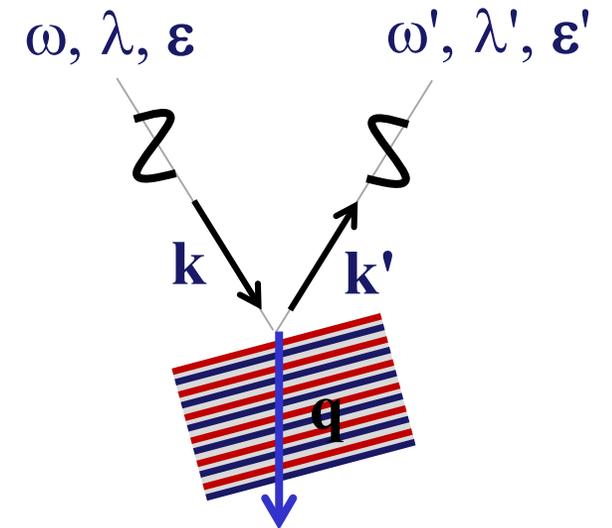
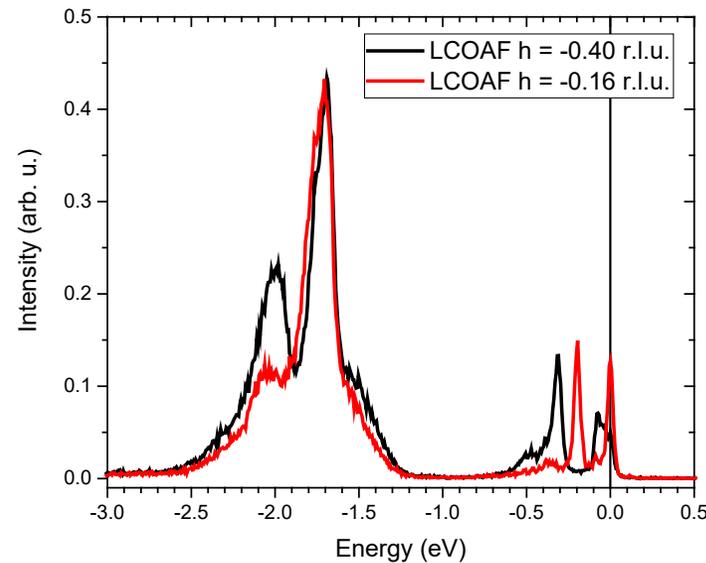
Cu L₃ RIXS: elastic, phonon, 2-magnon



$$\Omega = \omega - \omega'$$

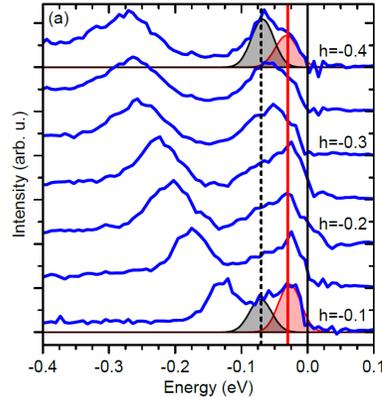
$$\mathbf{q} = \mathbf{k}' - \mathbf{k}$$

$\varepsilon, \varepsilon'$: polarization

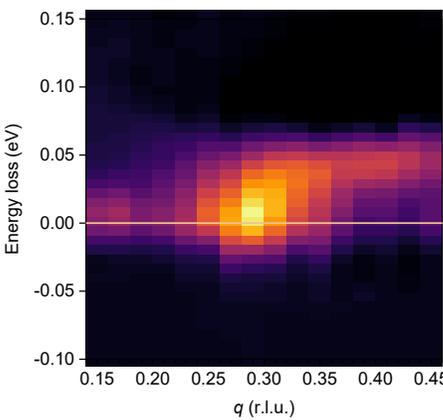
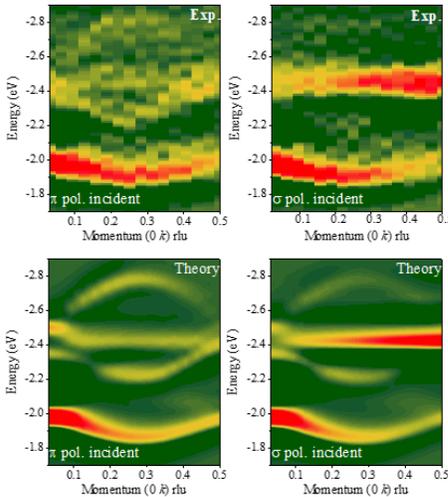


RIXS catalogue

Lattice excitations
(phonons)

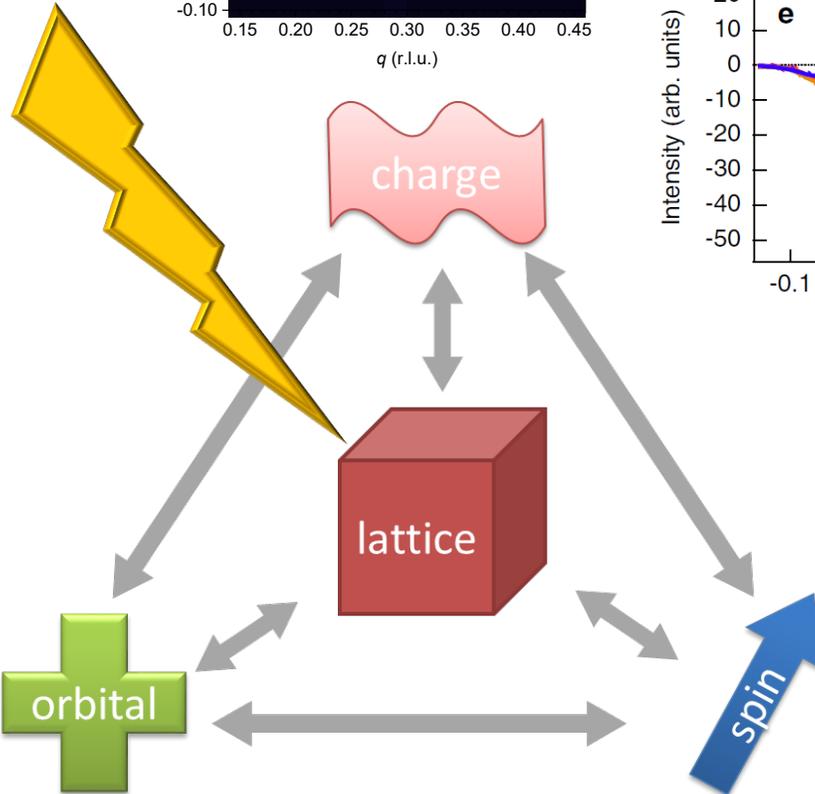
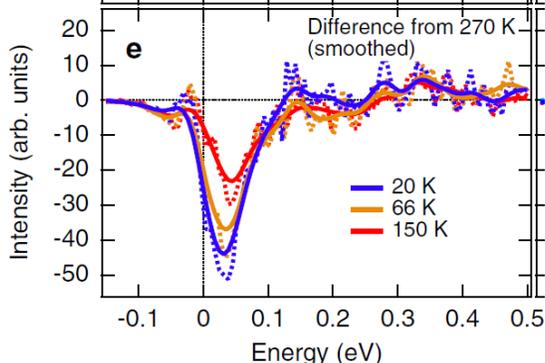


dd excitations

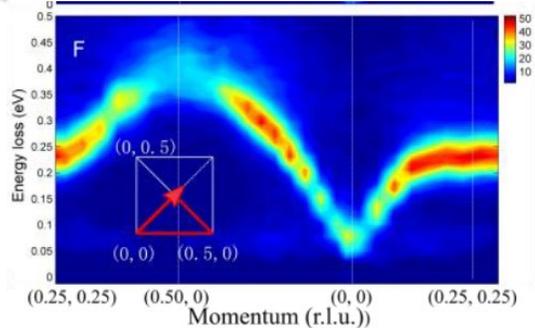


Charge Order
(CDW, CDF)

Charge excitations
(SC gap, pseudogap)



Spin excitations (magnons)



Part 2

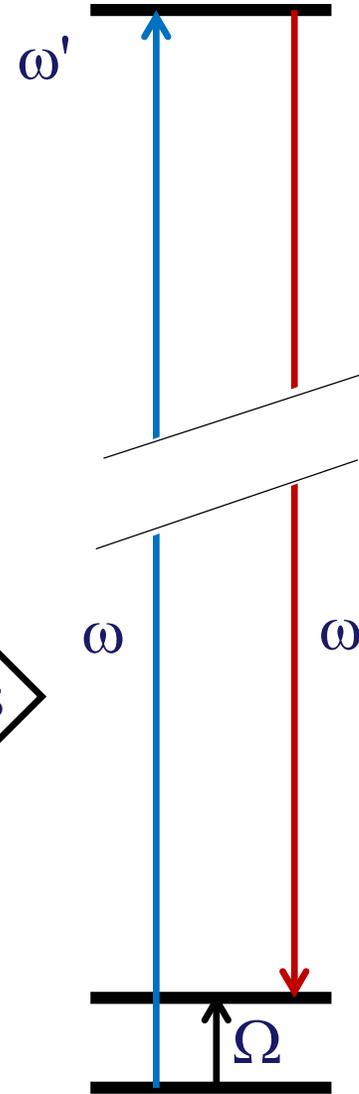
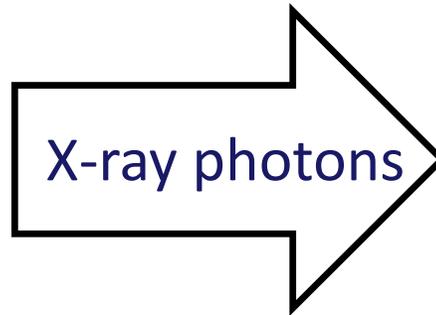
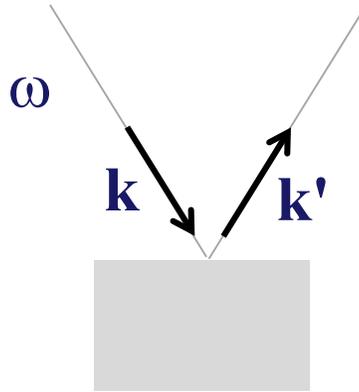
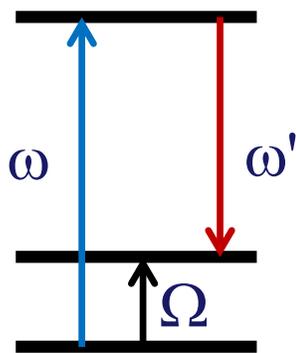
INSTRUMENTATION FOR RIXS (MOSTLY SOFT X-RAY REGIME)

RIXS: a sort of resonant Raman spectroscopy

Energy Loss Spectroscopy

Raman light scattering

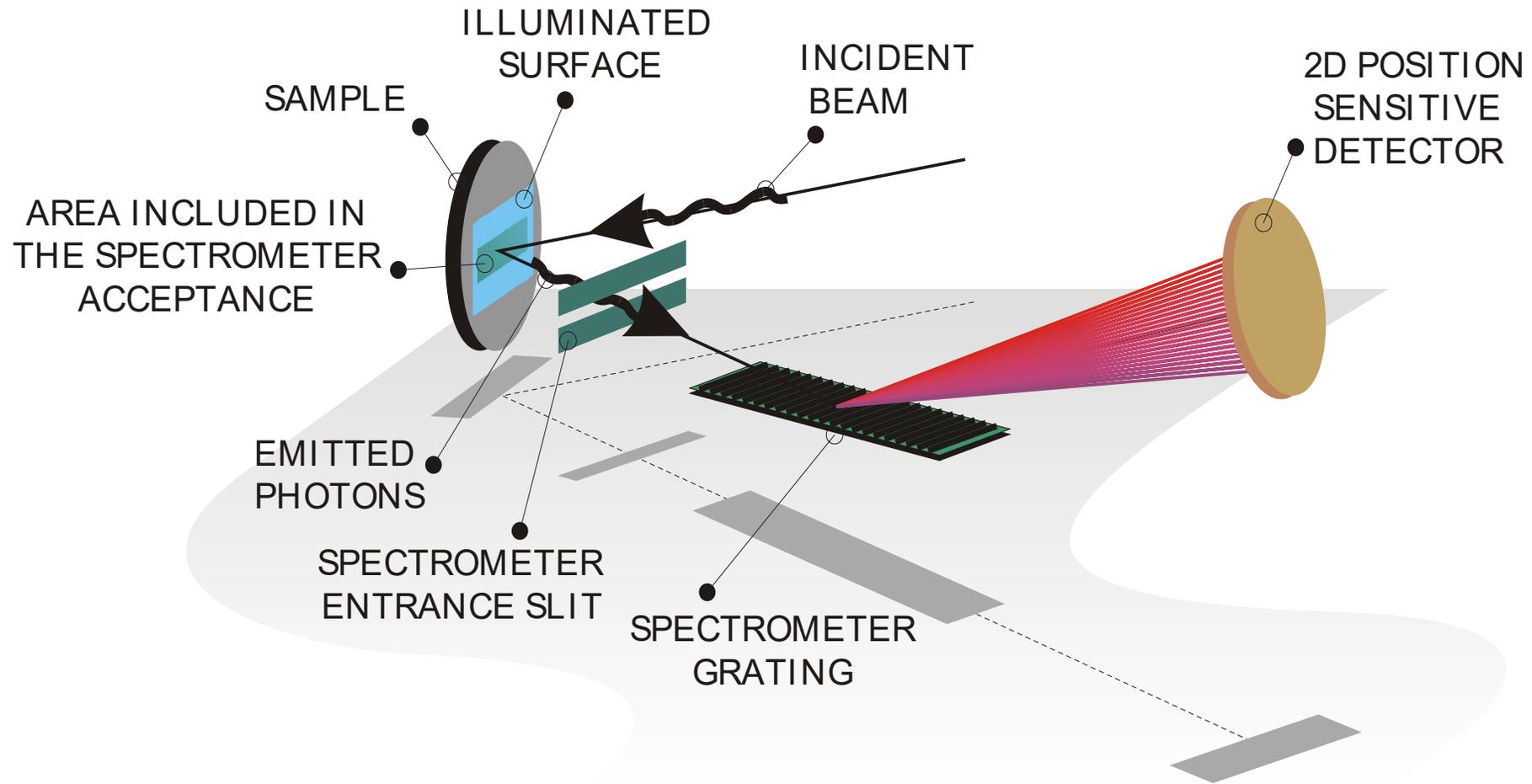
$$k \approx 0, q \approx 0, \\ \Omega = \omega - \omega'$$



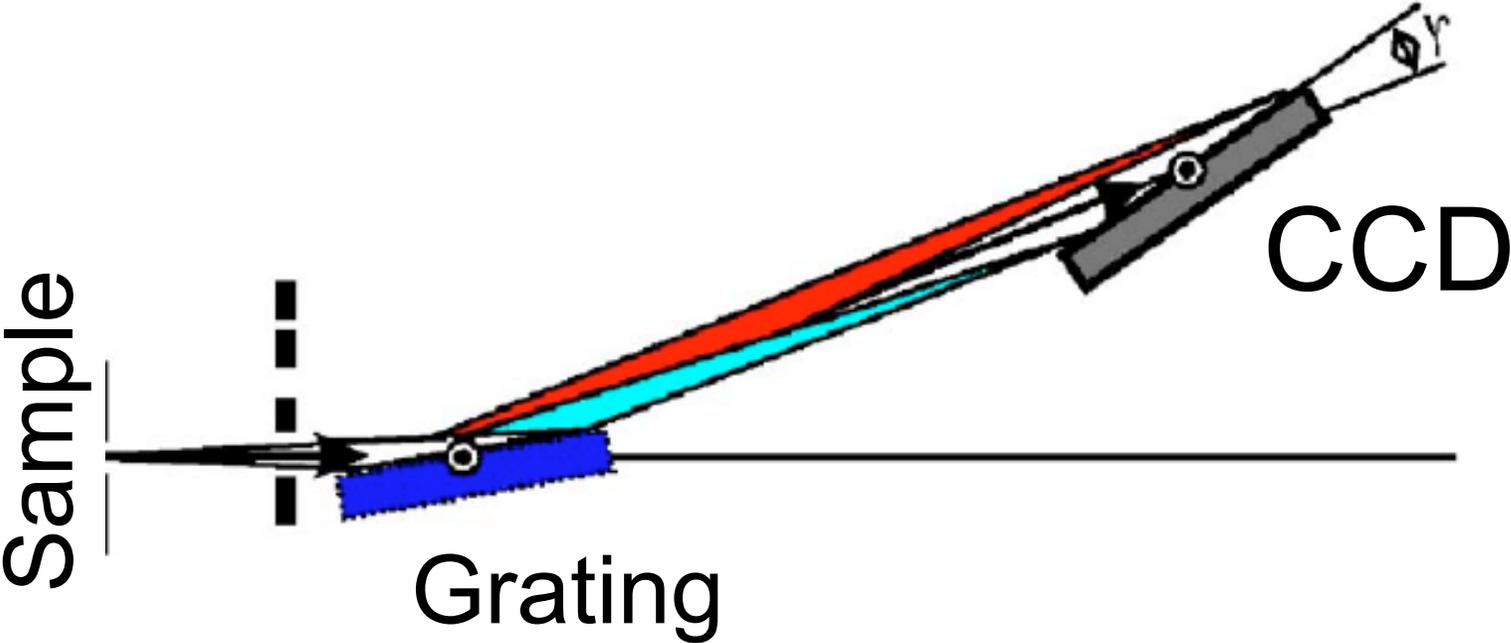
Inelastic X-ray Scattering

$$\Omega = \omega - \omega' \\ \mathbf{q} = \mathbf{k}' - \mathbf{k}$$

Soft x-ray spectrometer



Longer instruments for better resolution





AXES, ESRF: **2.2 m**
1994 – 2012
 $E/\Delta E \sim 3000$

The progress in instrumentation has been the key of the RIXS success: discoveries were enabled by better resolution.



SAXES, SLS: **5 m**
Since 2007
 $E/\Delta E \sim 10,000$

Similar instruments:

- TPS Taiwan
- European XFEL
- Bessy II



ERIXS, ID32: **10 m,**
Since 2015
 $E/\Delta E \sim 50,000$
Polarization Analysis

- Diamond I21
- NSLS II SIX

ERIXS at ID32

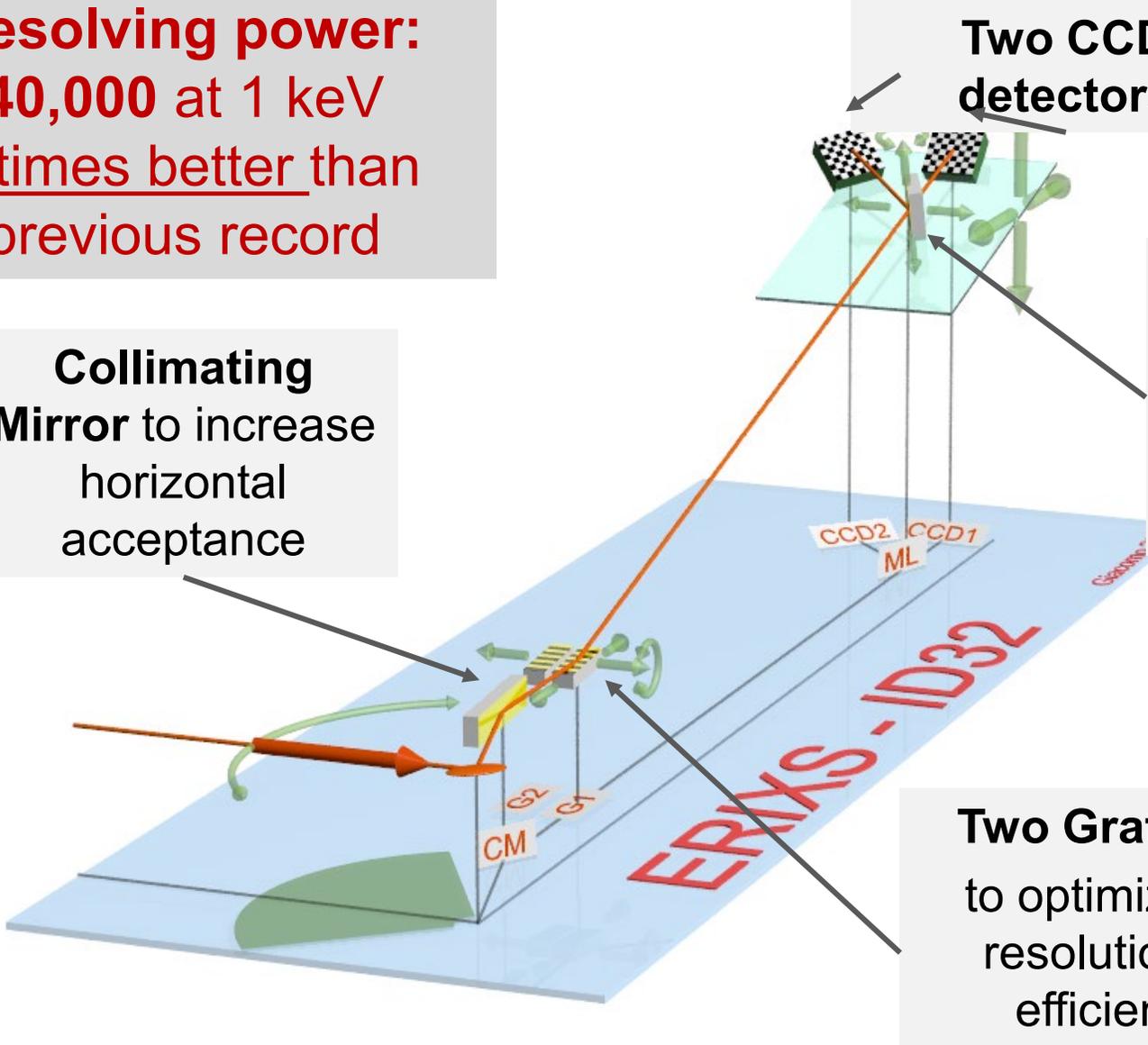


Resolving power:
40,000 at 1 keV
3 times better than
previous record

Collimating Mirror to increase horizontal acceptance

Two CCD detectors

Multi-layer mirror,
to measure polarization of scattered photons



Two Gratings,
to optimize for resolution or efficiency

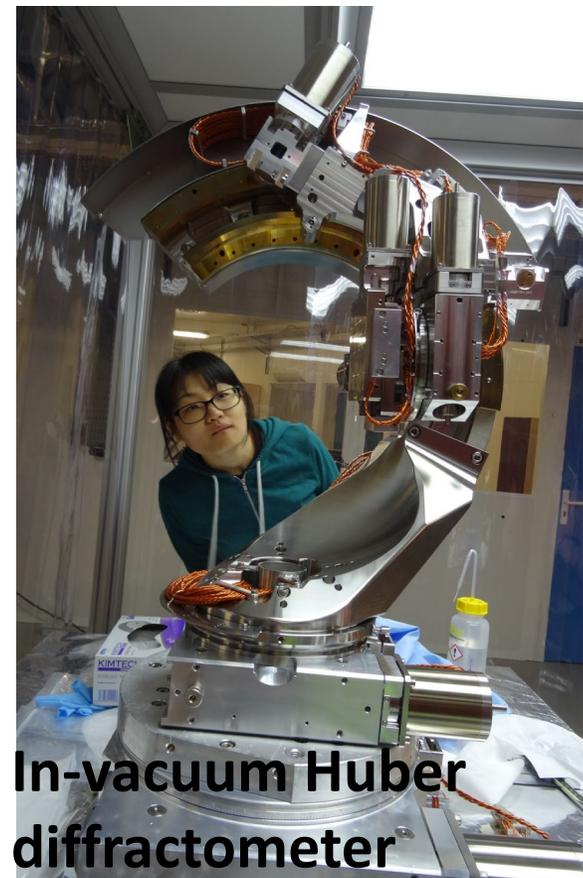
ERIXS Spectrometer



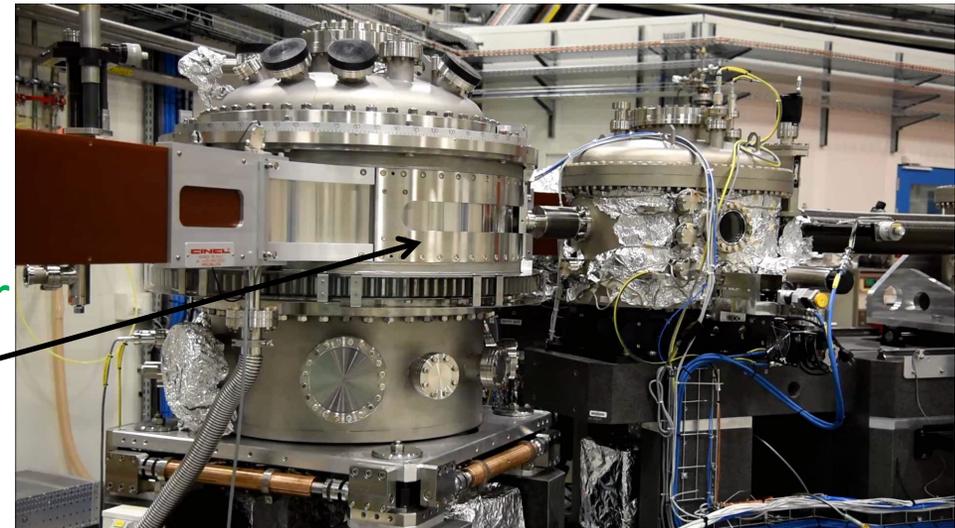
Continuously rotating
scattering arm

Speed
x8.6

Sample chamber
CINEL – Italy
ESRF



In-vacuum Huber
diffractometer



ID32@ESRF and I21@DLS

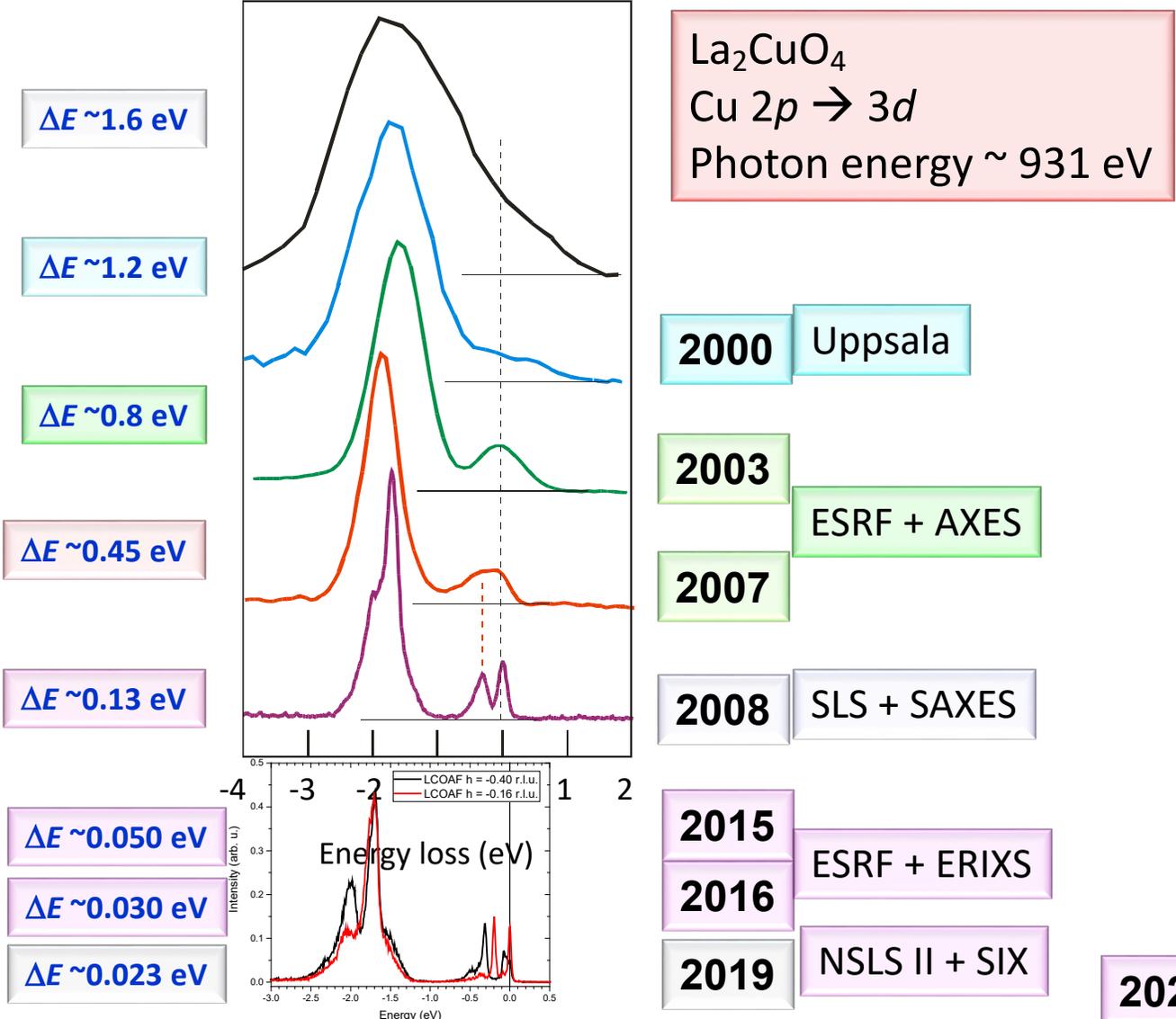
ERIXS
at
ID32



I21 at
Diamond



ENERGY RESOLUTION: progress in 20 years

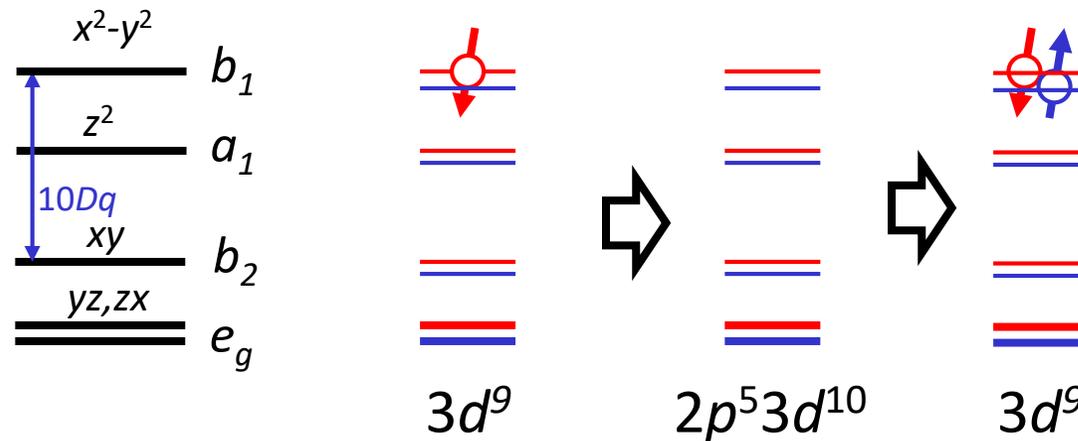
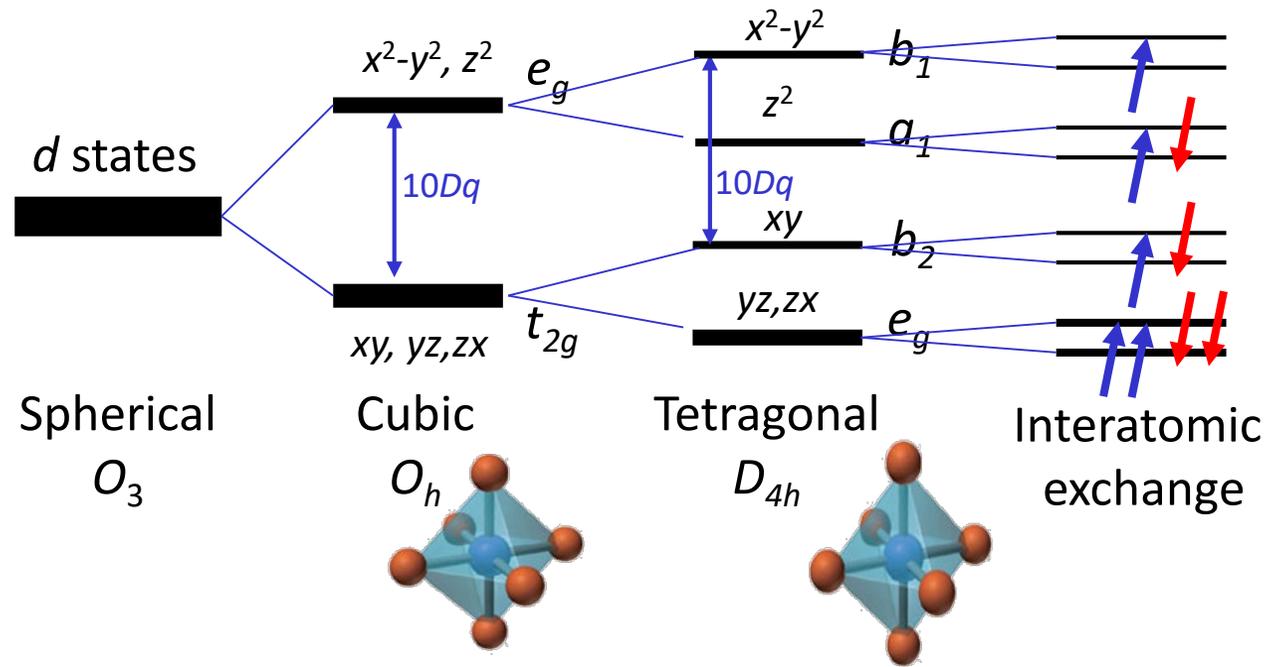


Combined resolving power has increased by a factor 70

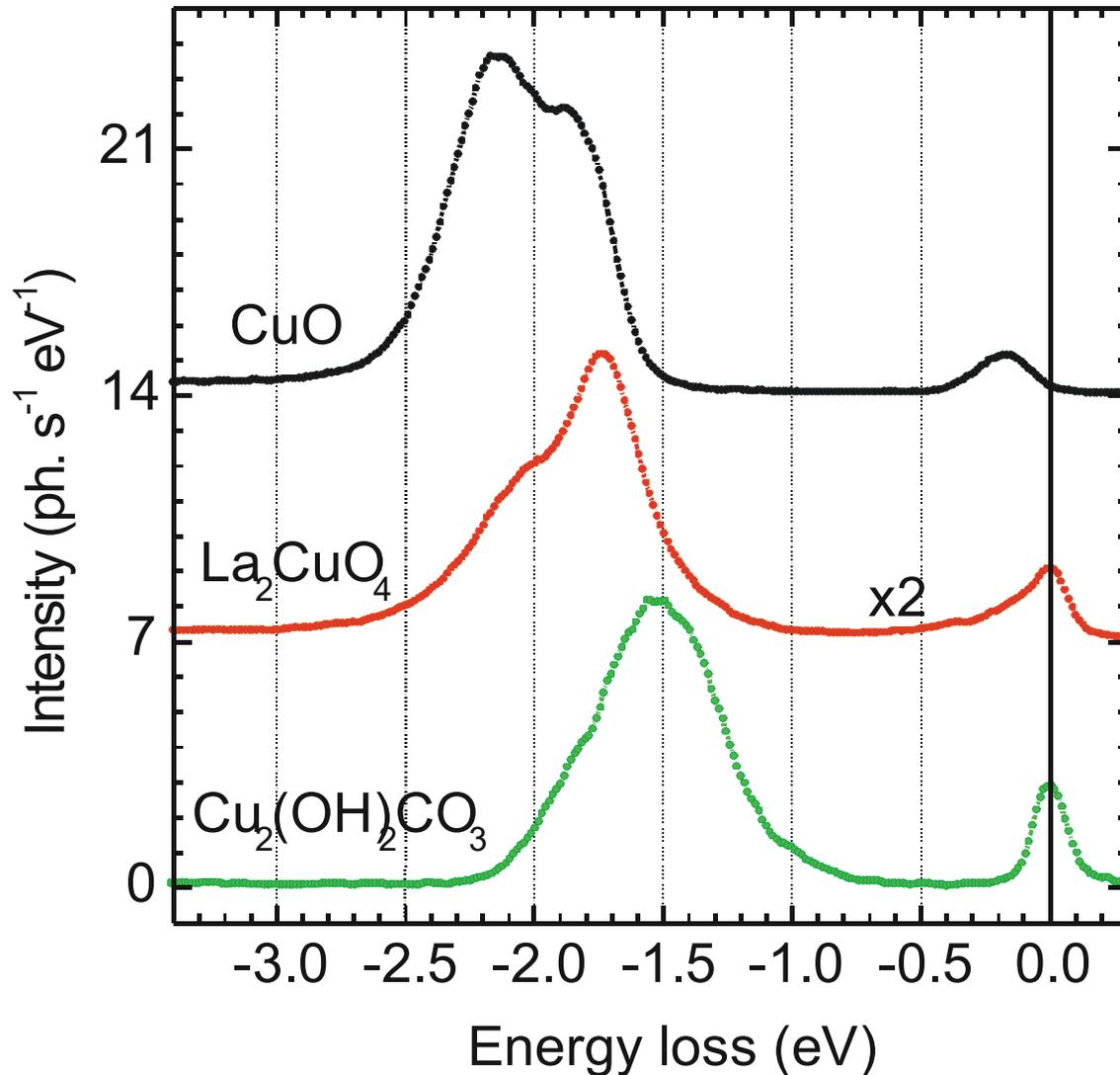
Part 3

ORBITAL EXCITATIONS

dd excitations in Cu^{2+} systems



Cu L₃ edge RIXS: CuO, La₂CuO₄, Malachite



Cu²⁺ in square
approximately
planar coordination

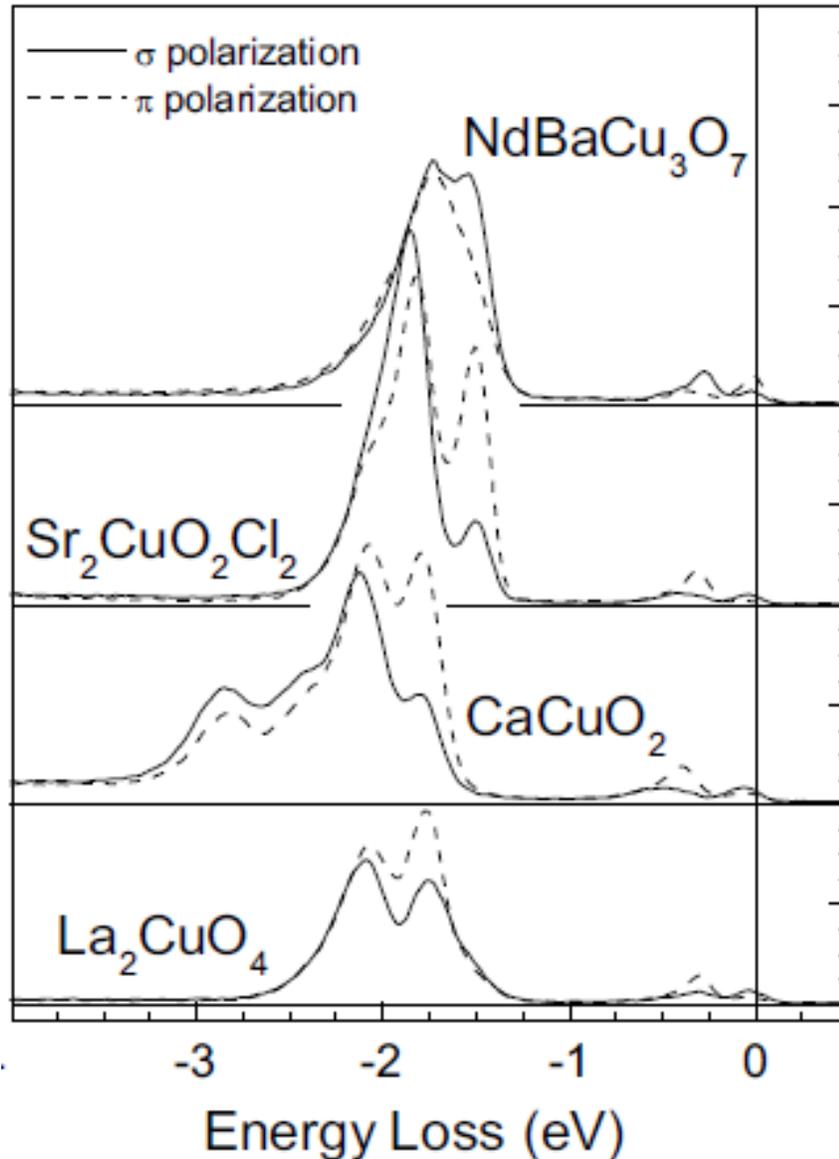
Cu-O distances:
CuO 1.7 – 2.2 Ang
LCO 1.9 – 2.4 Ang
Malachite 1.9 – 2.6 Ang

Different Cu²⁺
coordination,
symmetry,
hybridization



Different *dd* excitations

This is a very direct way of measuring the *dd*-excitation energies

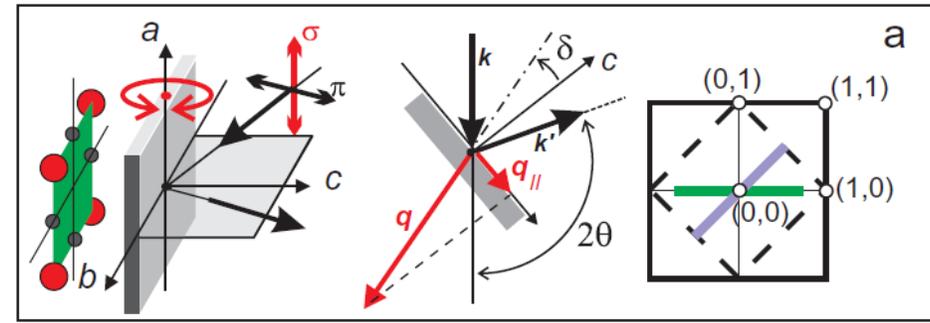


New Journal of Physics

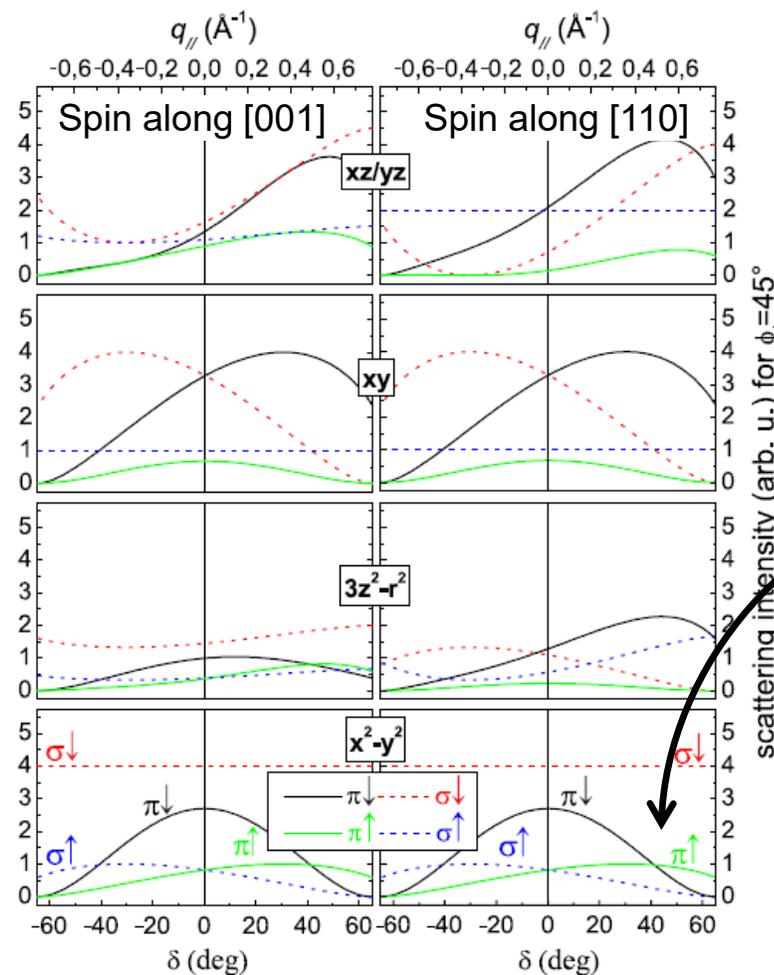
The open-access journal for physics

Energy and symmetry of *dd* excitations in undoped layered cuprates measured by Cu L_3 resonant inelastic x-ray scattering

M Moretti Sala^{1,8,9}, V Bisogni^{2,10}, C Aruta³, G Balestrino⁴, H Berger⁵, N B Brookes², G M de Luca³, D Di Castro⁴, M Grioni⁵, M Guarise⁵, P G Medaglia⁴, F Miletto Granozio³, M Minola¹, P Perna³, M Radovic^{3,11}, M Salluzzo³, T Schmitt⁶, K J Zhou⁶, L Braicovich⁷ and G Ghiringhelli⁷



dd -excitation energies from fitting using atomic cross sections

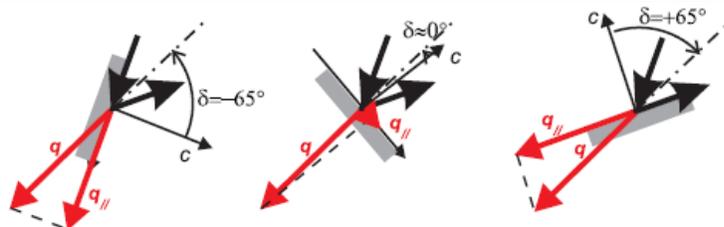
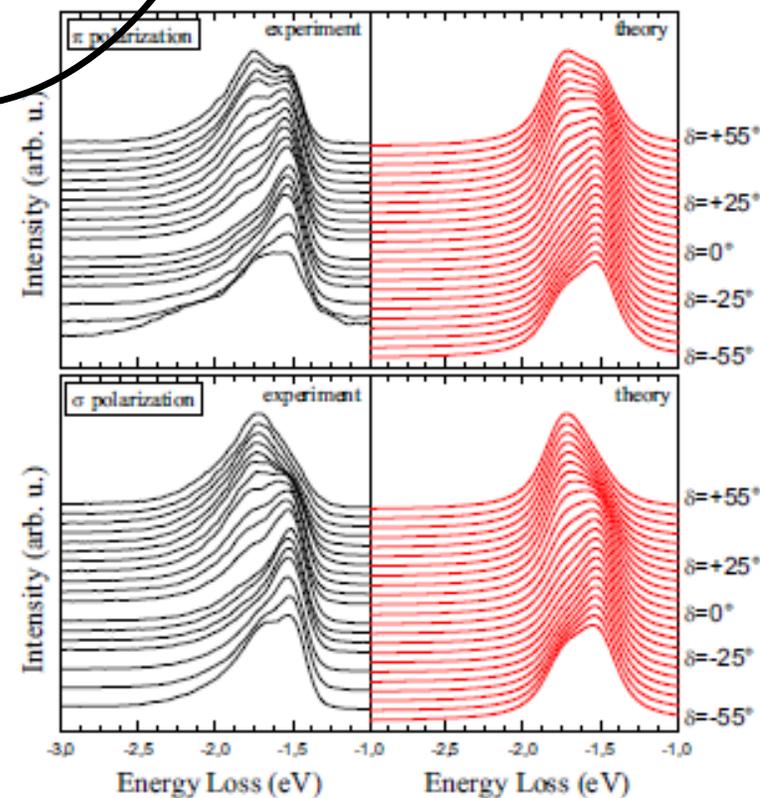


Ground state: $\underline{3d^\downarrow} x^2-y^2$

Spin flip: $\underline{3d^\uparrow} x^2-y^2$

$F(\theta_{in}, \phi_{in}, \theta_{out}, \phi_{out}, \theta_{spin}, \phi_{spin}, \varepsilon_{in}, \varepsilon_{out})$

NdBCO

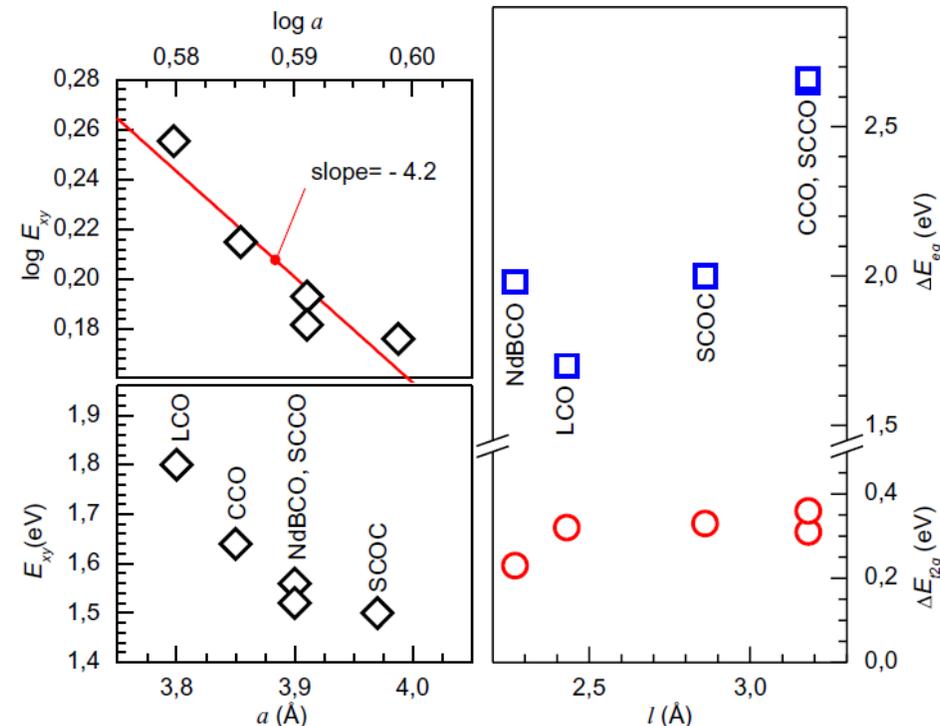
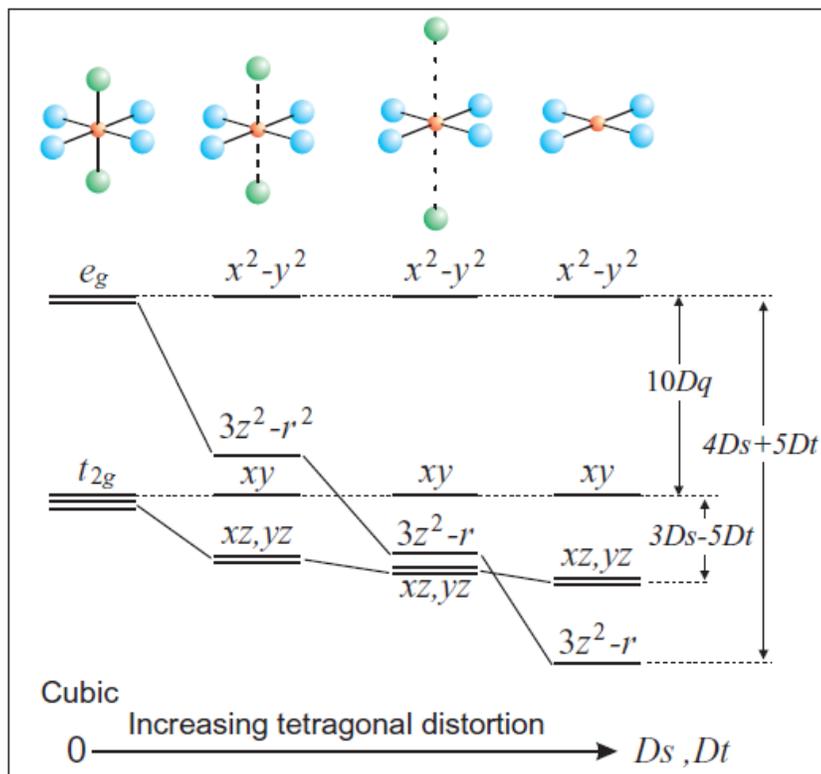


$2\theta=130^\circ$

M. Moretti Sala, et al New J. Phys. **13**, 043026 (2011)



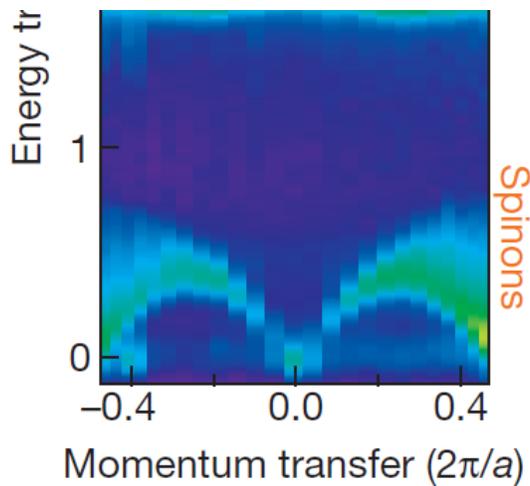
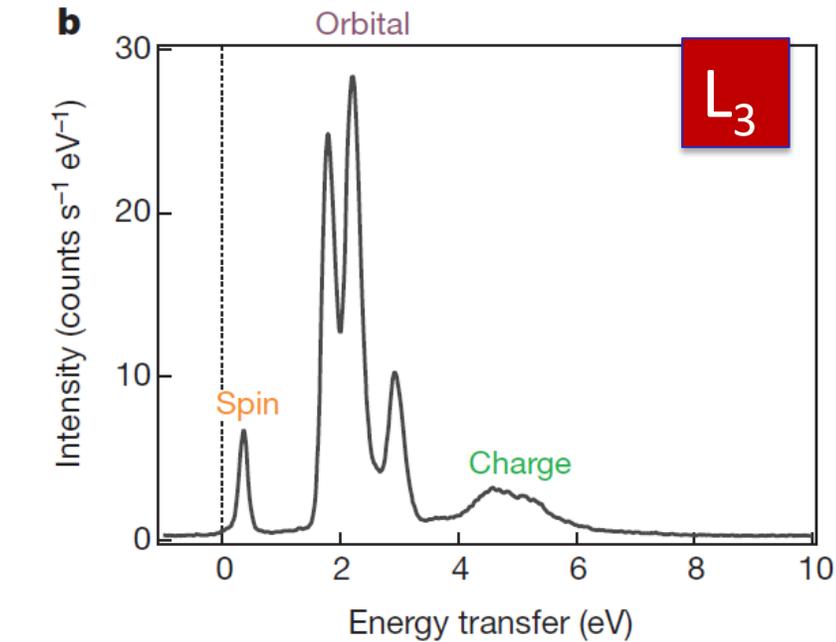
Crystal field trends in cuprates



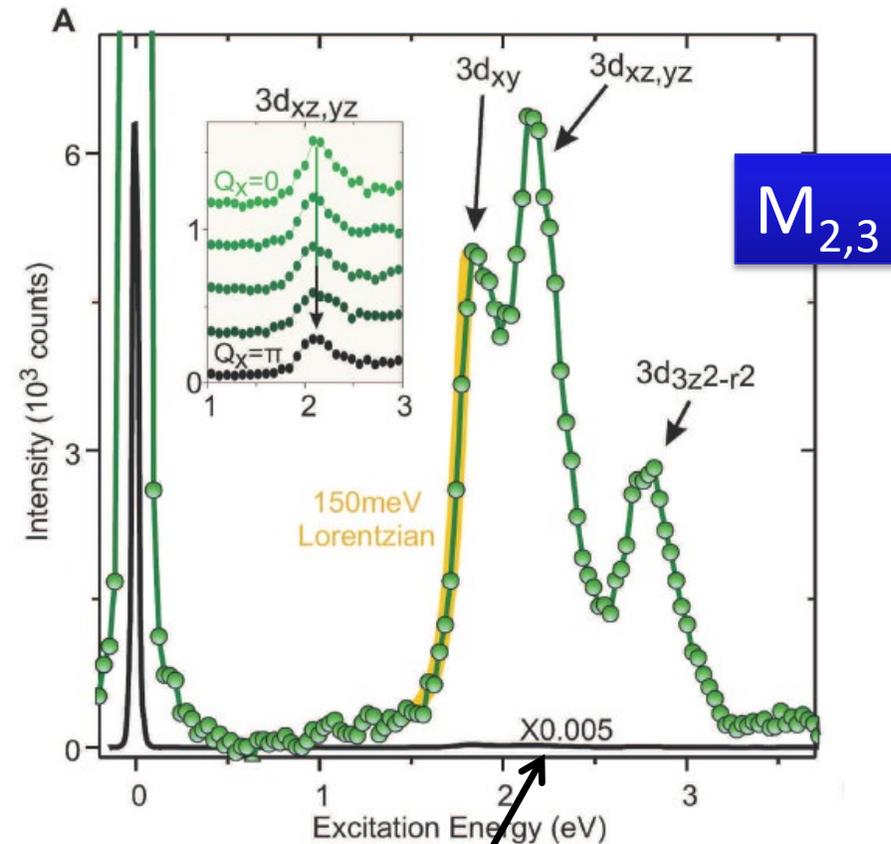
	La_2CuO_4	$\text{Sr}_2\text{CuO}_2\text{Cl}_2$	CaCuO_2
J [meV]	$130^{34,35}$	130^{35}	130^{35}
$E_{3z^2-r^2}$ ($\Gamma_{3z^2-r^2}$) [eV]	1.70 (.14)	1.97 (.10)	2.72 (.12)
E_{xy} (Γ_{xy}) [eV]	1.80 (.10)	1.50 (.08)	1.75 (.09)
$E_{xz/yz}$ ($\Gamma_{xz/yz}$) [eV]	2.12 (.14)	1.84 (.10)	2.10 (.18)

M. Moretti Sala, et al New J. Phys. **13**, 043026 (2011)

dd excitations and absorption edge: Cu L₃ vs M_{2,3} edges

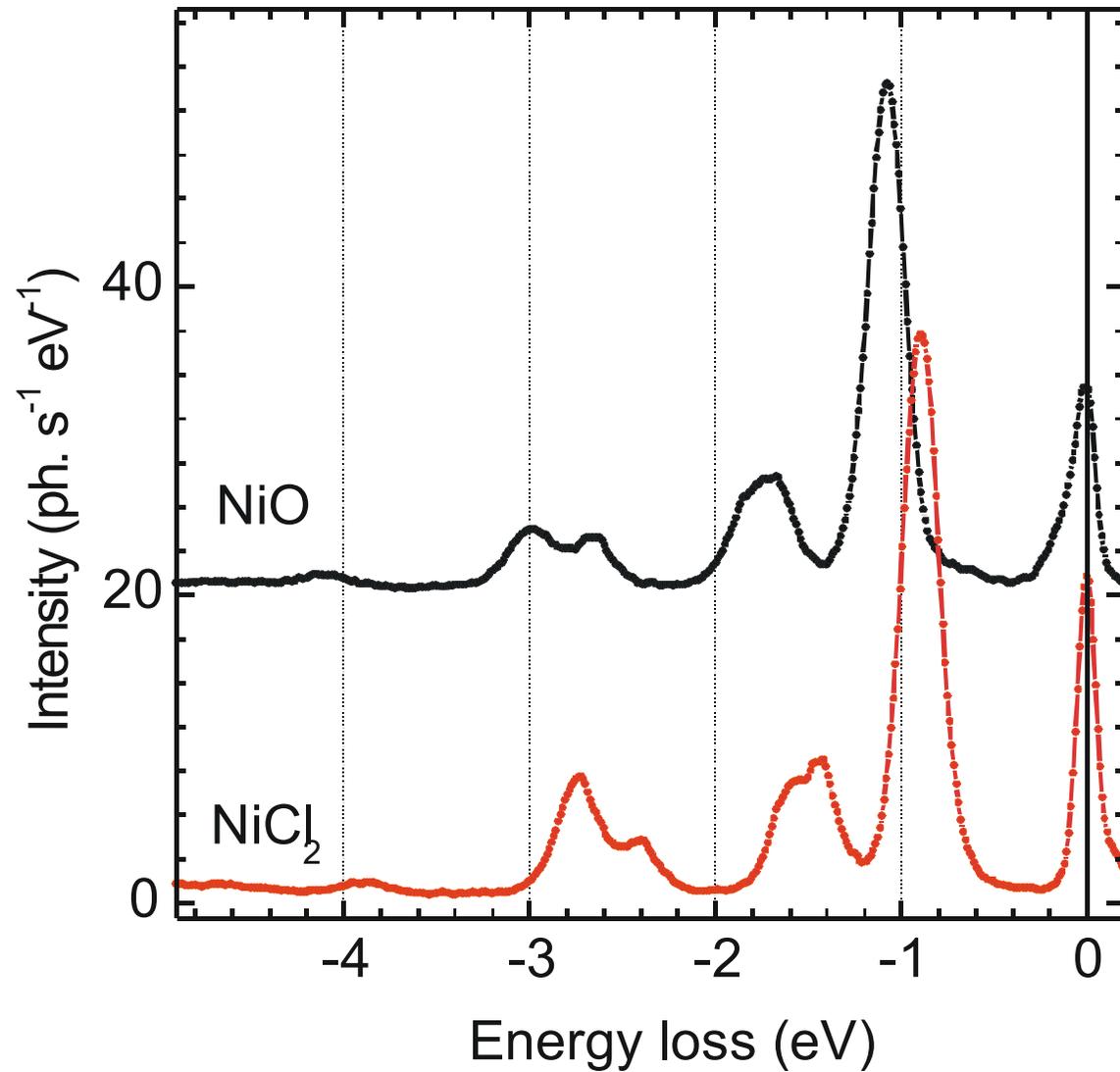


No spin excitations at Gamma point

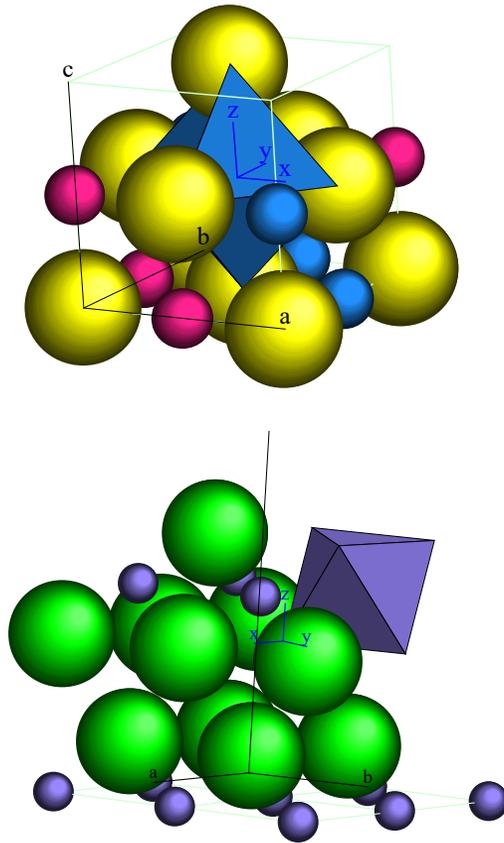


Very weak signal with respect to the elastic peak

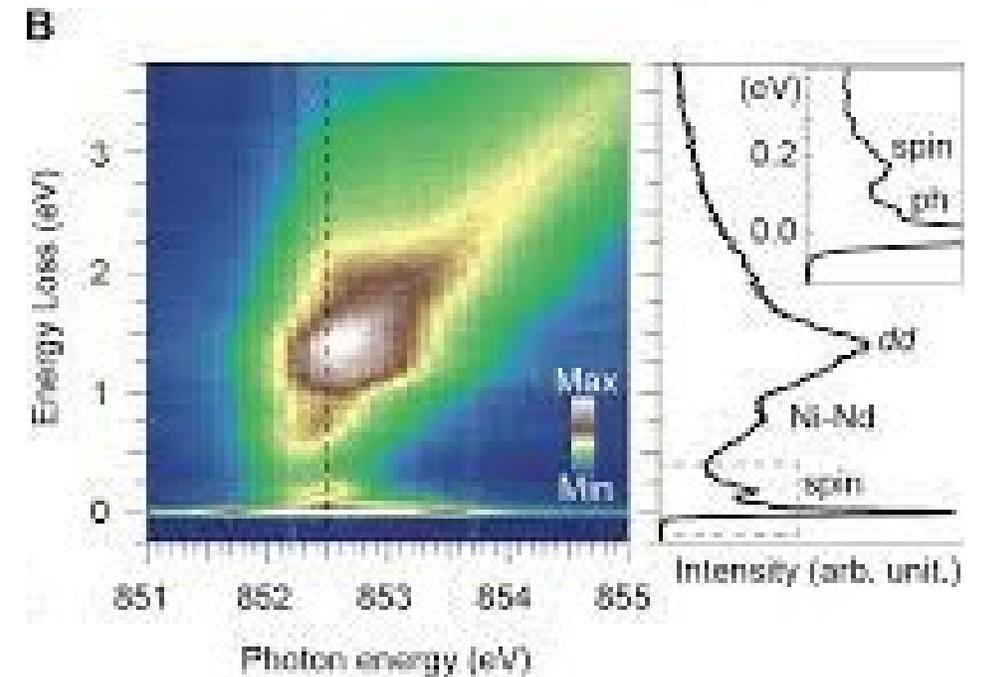
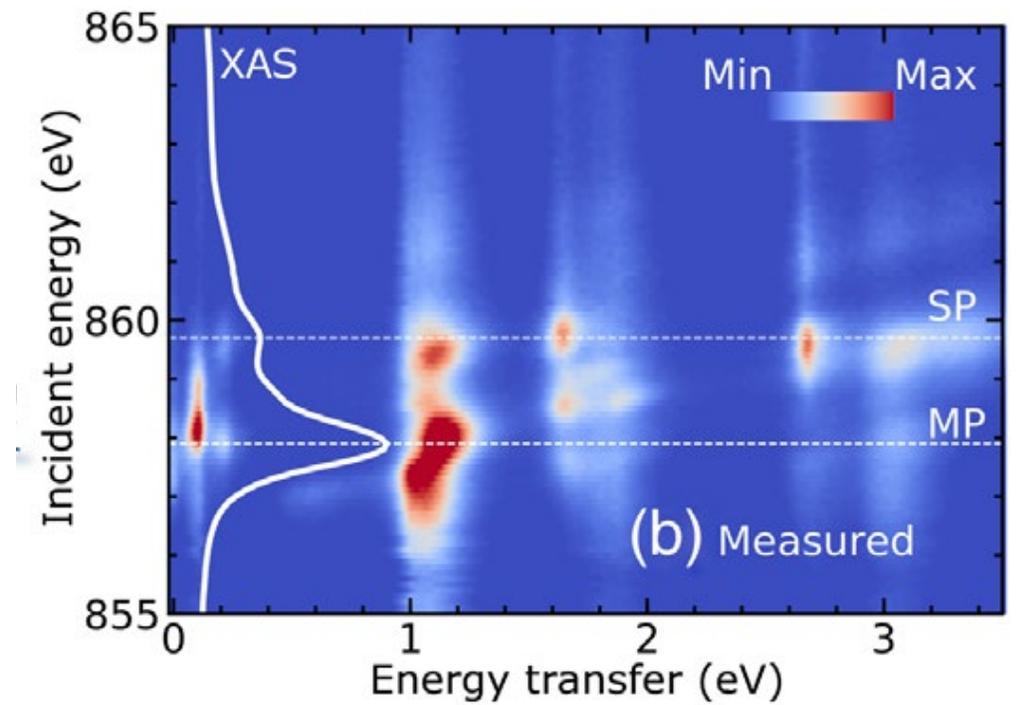
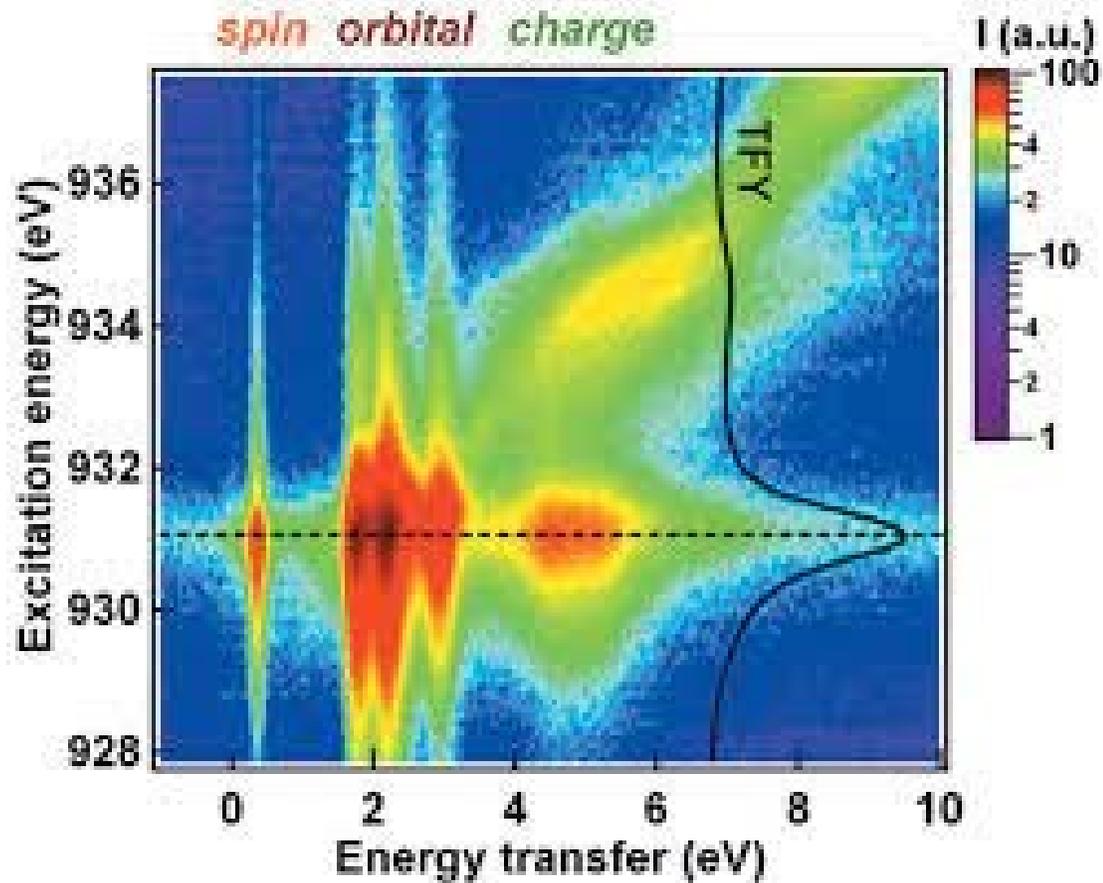
Ni L₃ edge: NiO, NiCl₂



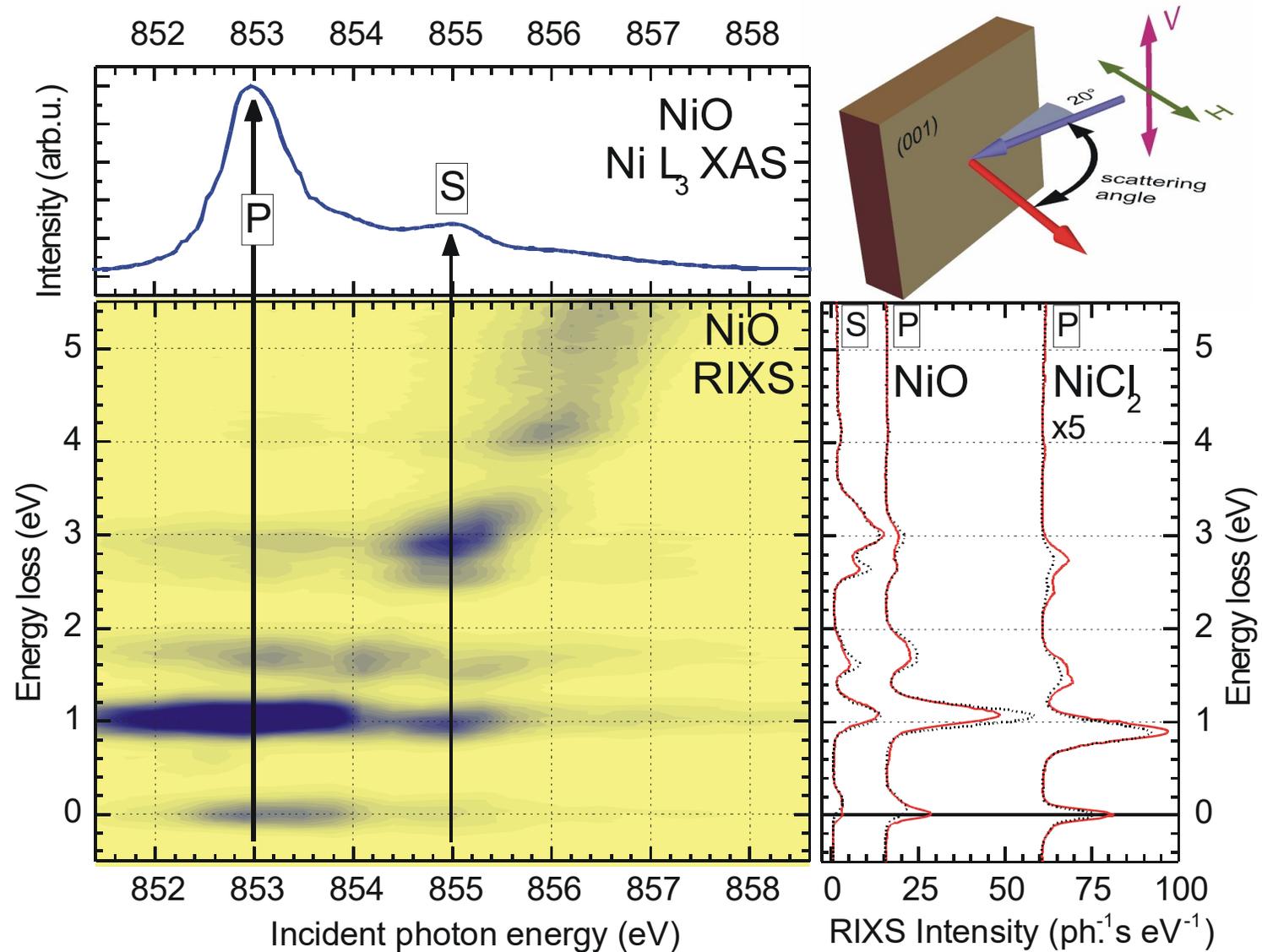
Ni²⁺ (3d⁸) in octahedral coordination



RIXS maps



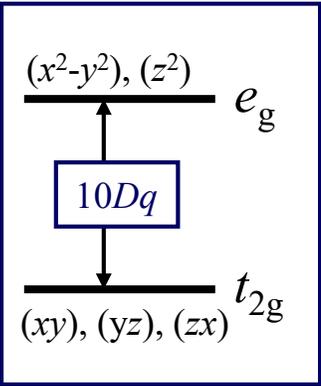
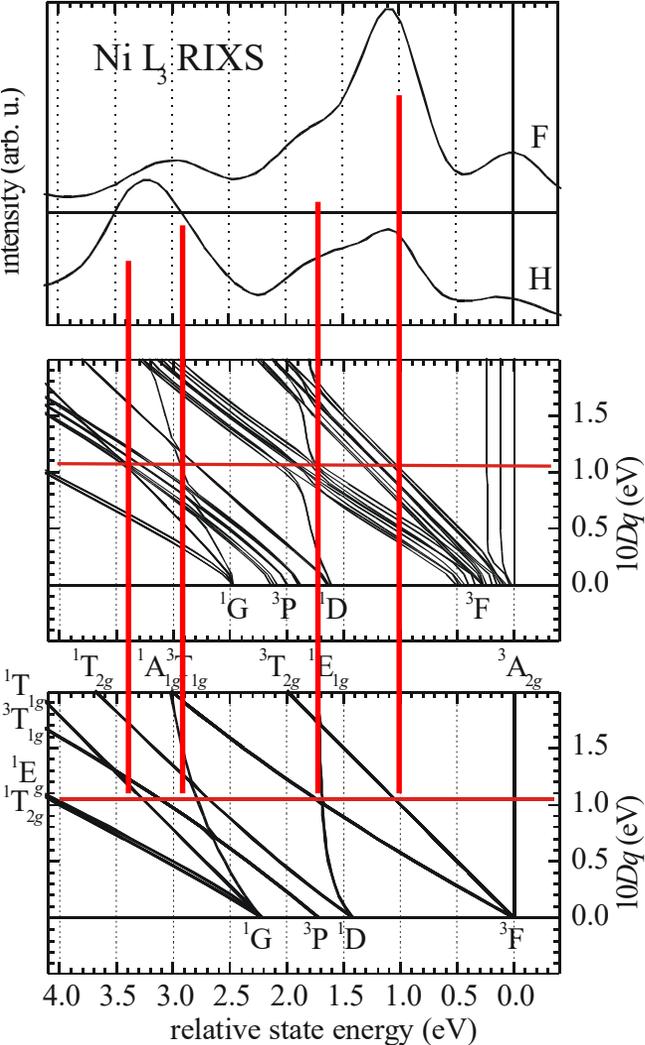
Ni²⁺ in NiO: dependence on incident photon energy



G. Ghiringhelli et al , Phys Rev Lett **102**, 027401 (2009)

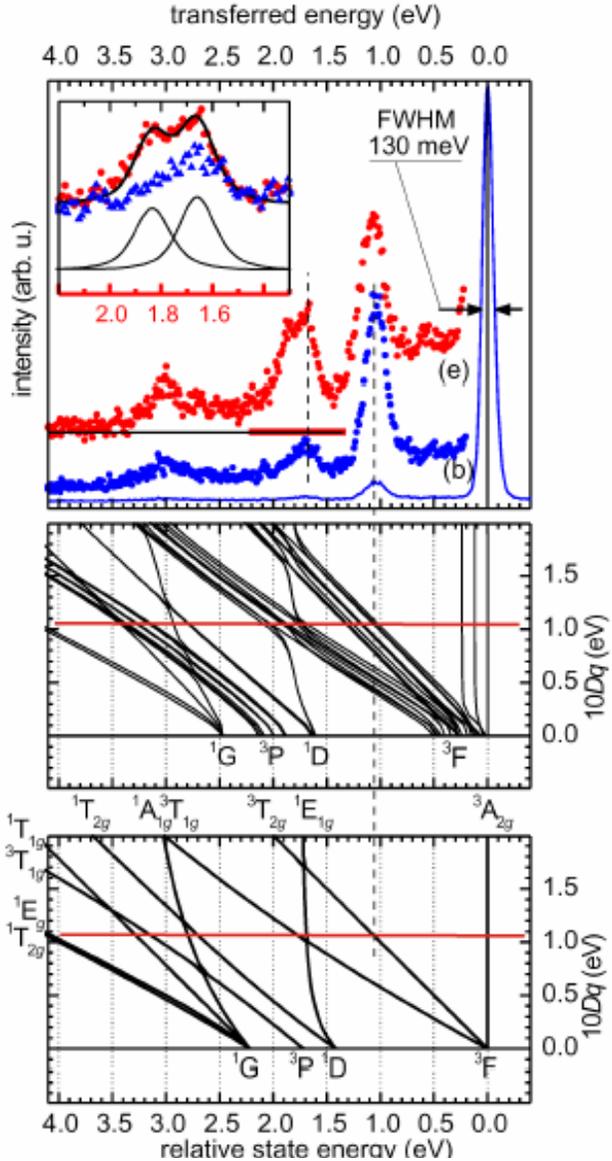
Many excited states

Crystal field model: Sugano-Tanabe diagrams



Single ion
Octahedral C.F.
3d spin-orbit
Exchange

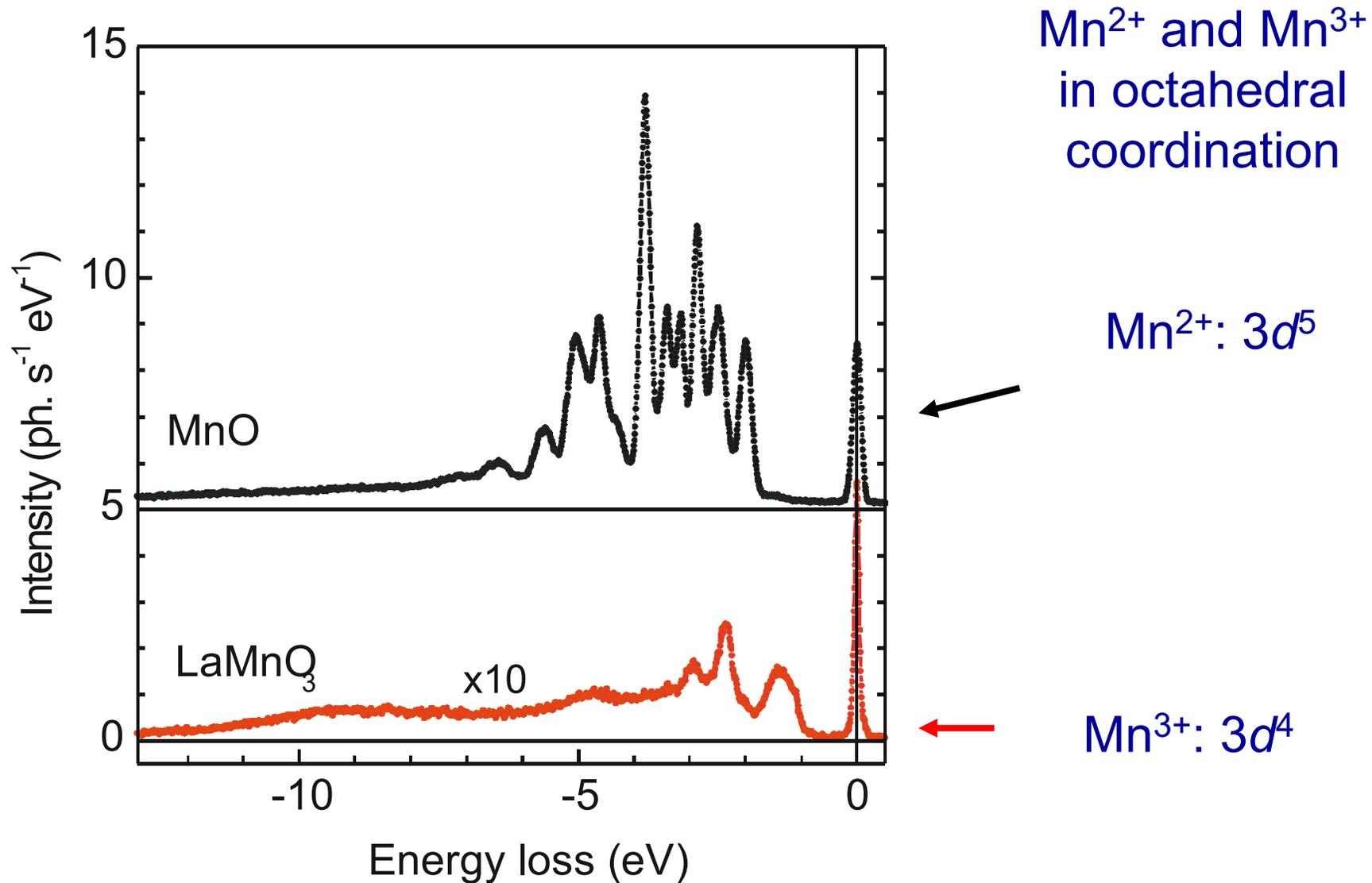
Single ion
Octahedral C.F.



G. Ghiringhelli *et al*, J. Phys. Cond. Mat. **17**, 5397 (2005)

S.G.Chiuzbaian, G. Ghiringhelli *et al*, Phys. Rev. Lett. **95**, 197402 (2005)

Mn L₃ edge: MnO, LaMnO₃



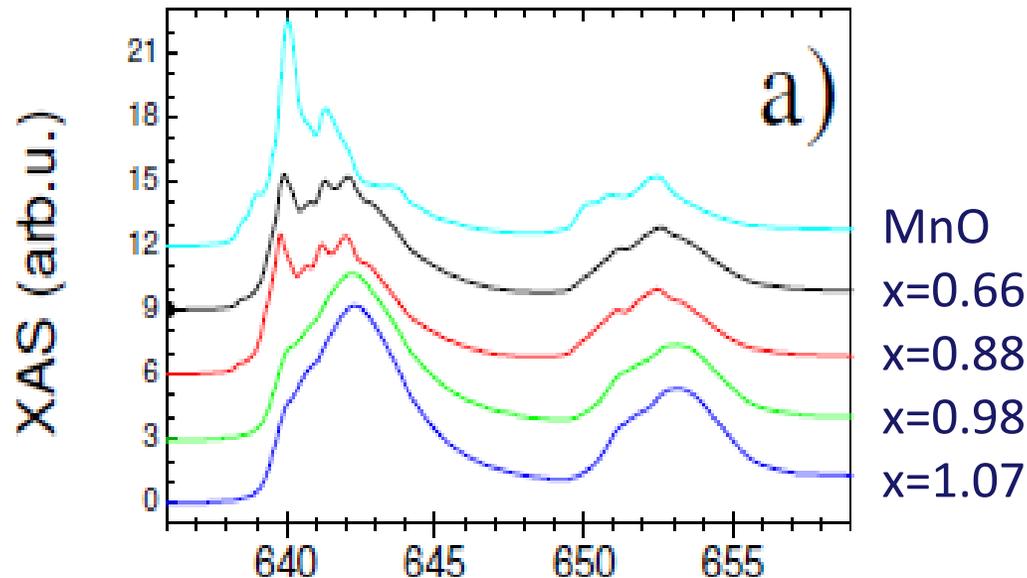
An application to thin film: Mn^{2+} in La_xMnO_3

$\text{La}_x\text{MnO}_{3-d}/\text{STO}$ films

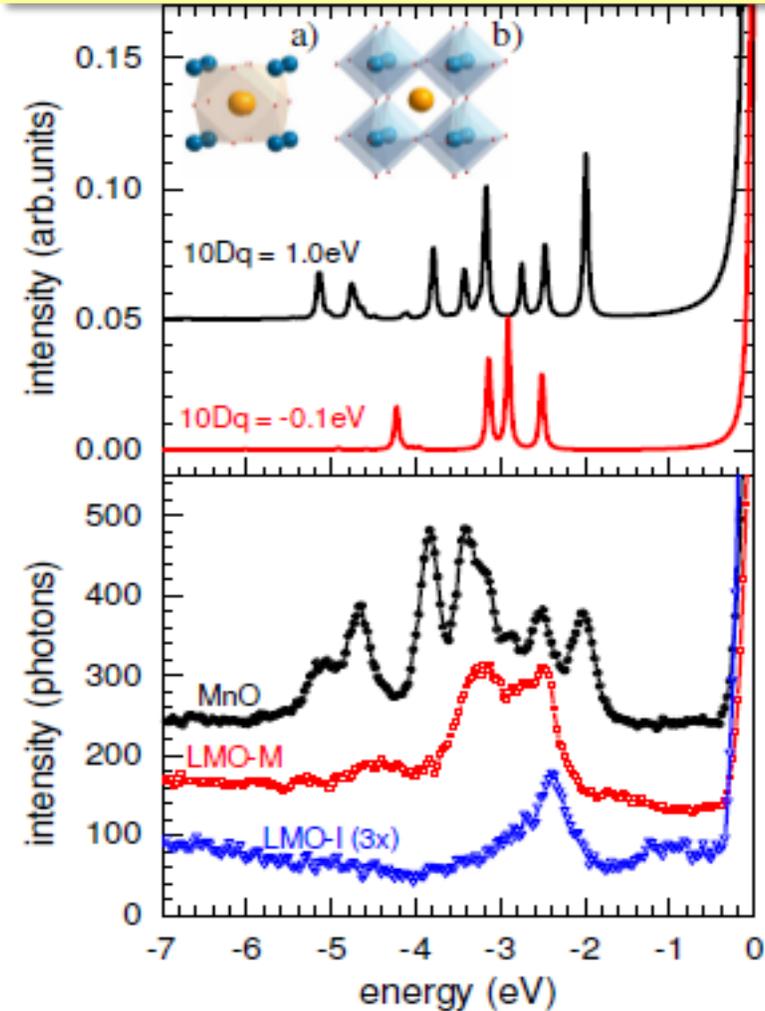
$x = \text{La}/\text{Mn}$ ratio

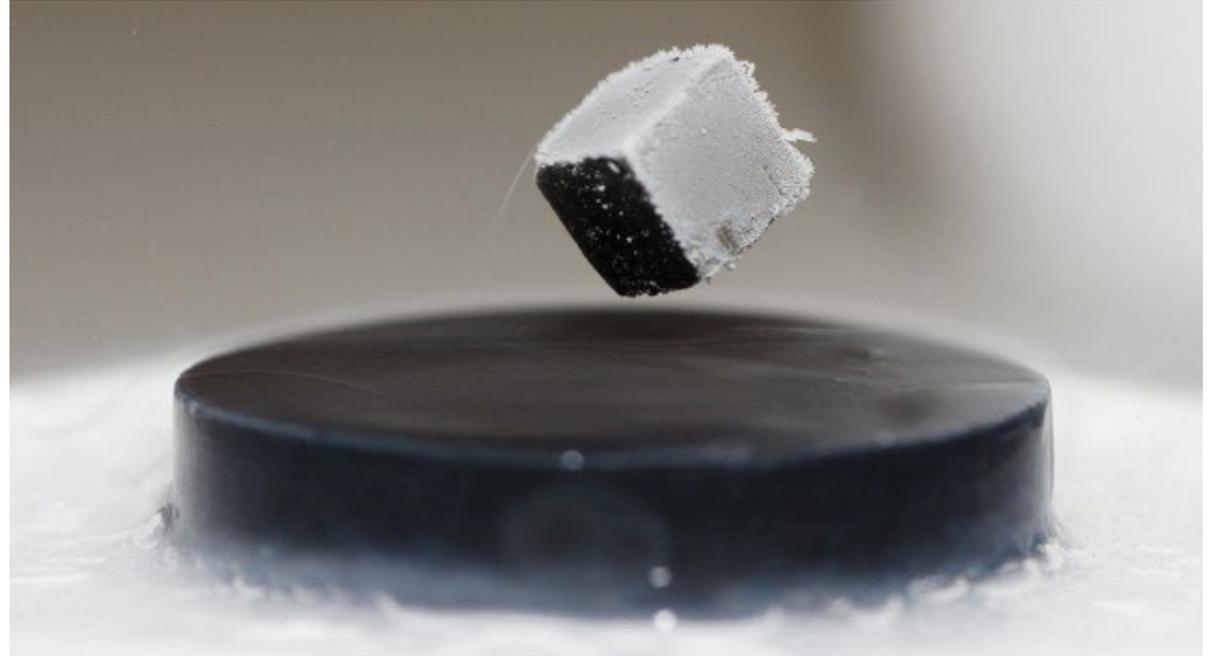
for $x < 1$ becomes FM (self doping)

XAS reveals the presence of Mn^{2+} for $x < 1$



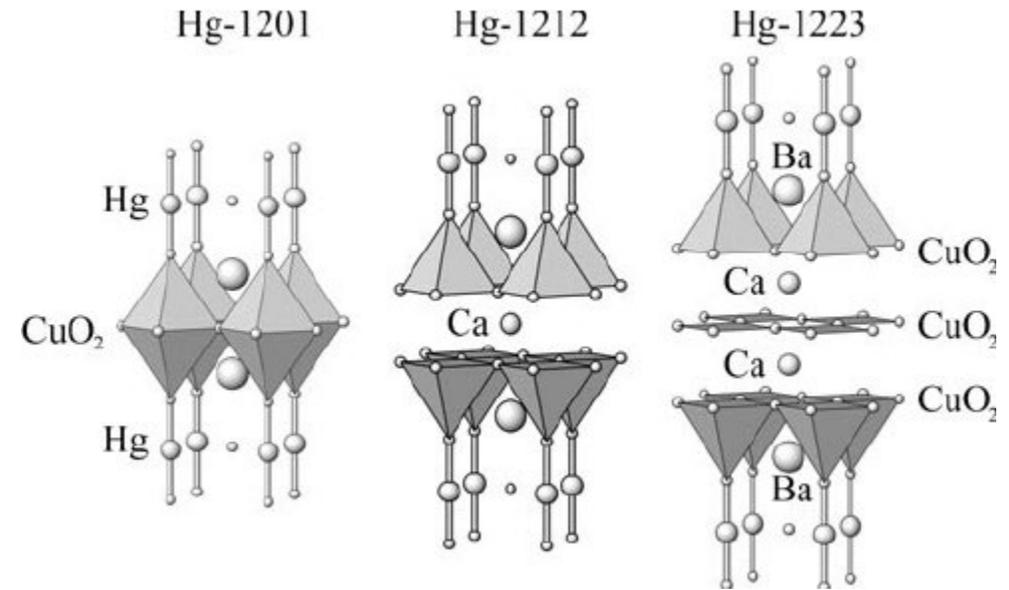
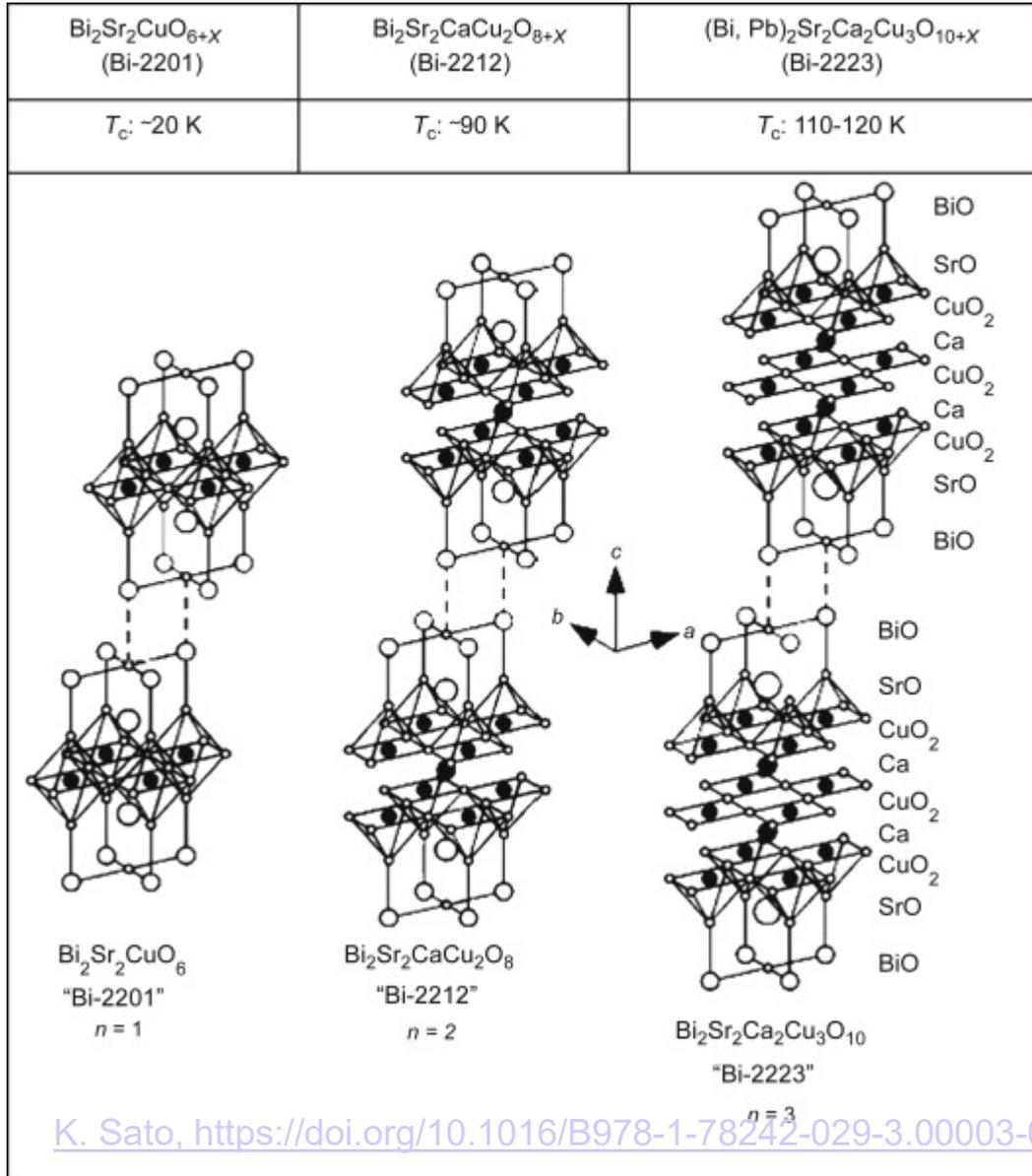
RIXS shows that Mn^{2+} is at site A, ie, it replaces La^{3+}





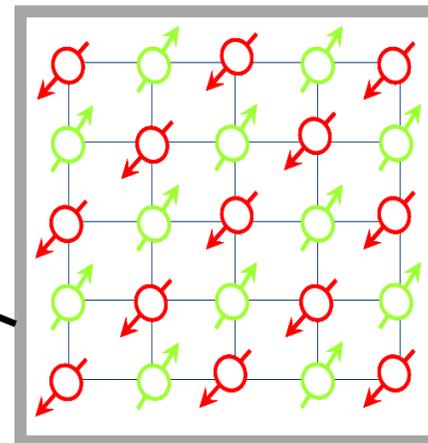
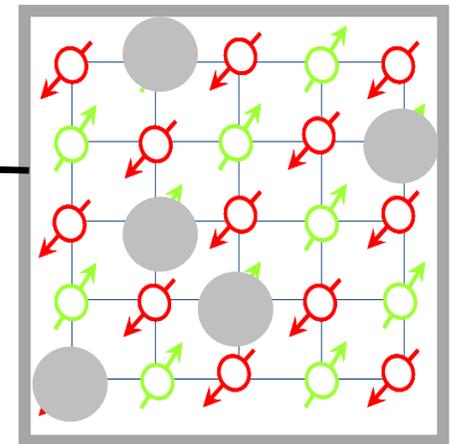
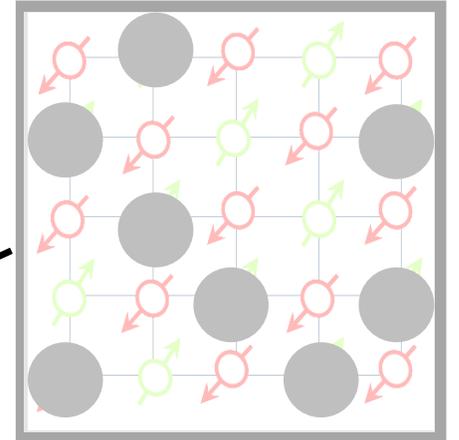
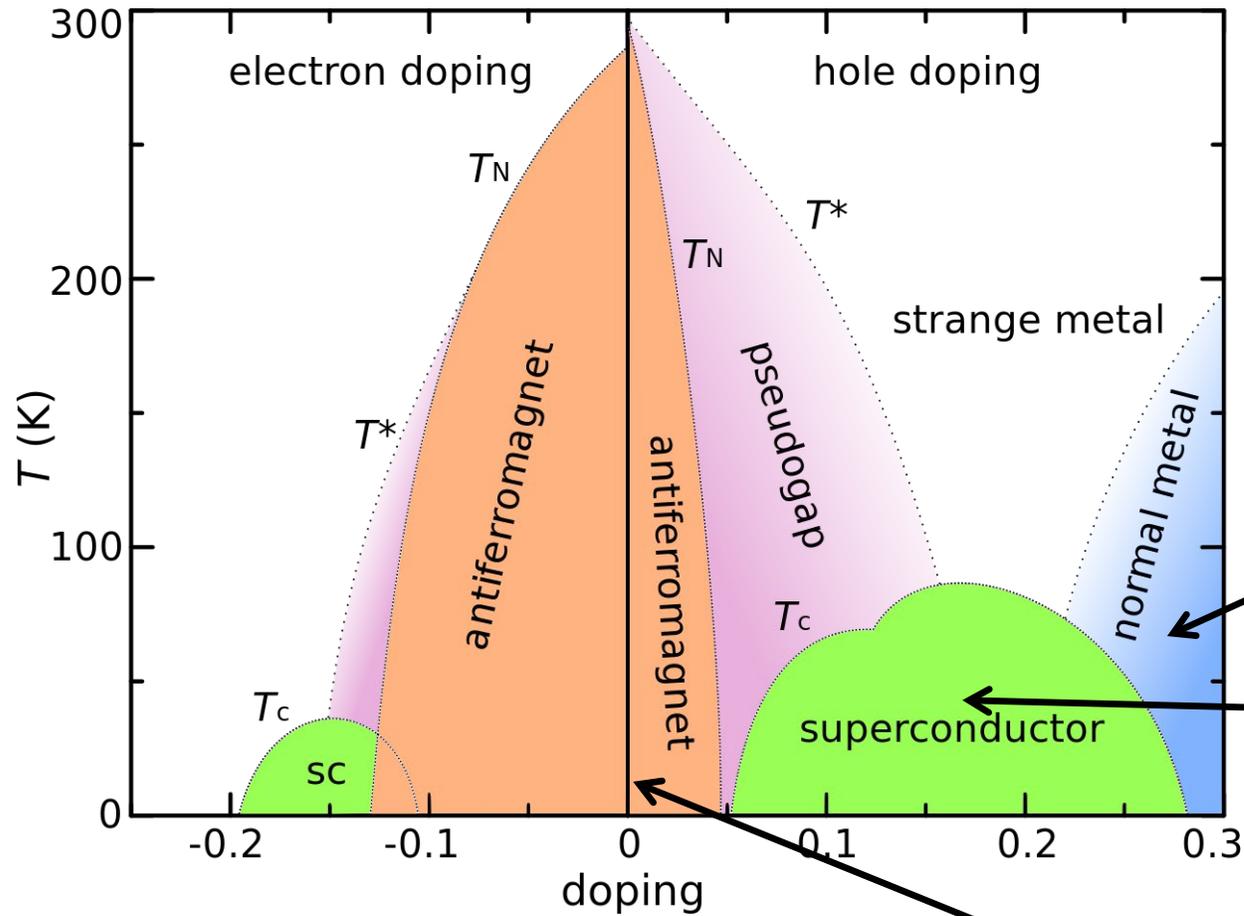
HIGH TC SUPERCONDUCTING CUPRATES

Quasi 2D materials: single layer, bi-layer, tri-layer



Antipov et al. : <http://dx.doi.org/10.1088/0953-2048/15/7/201>

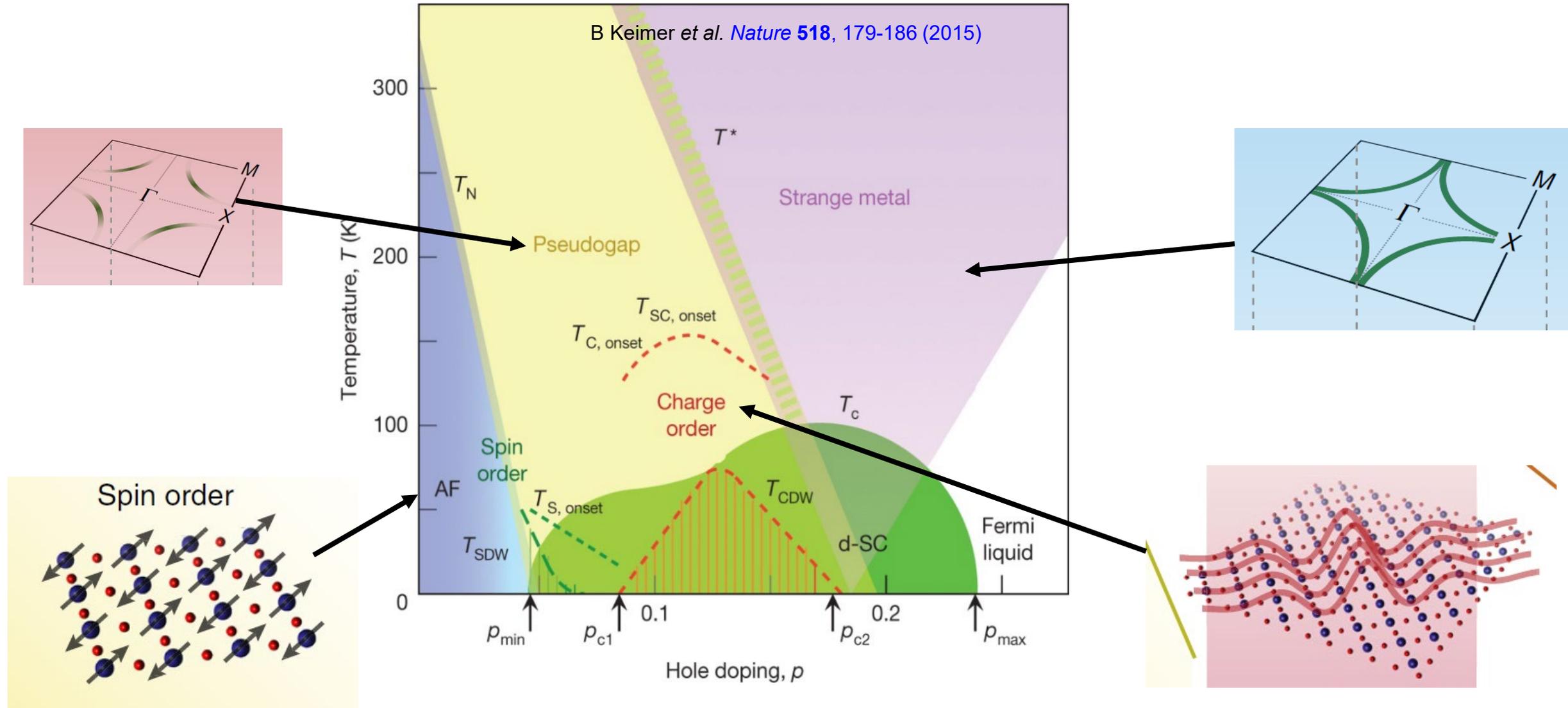
The doping of the CuO_2 planes



Wikimedia:

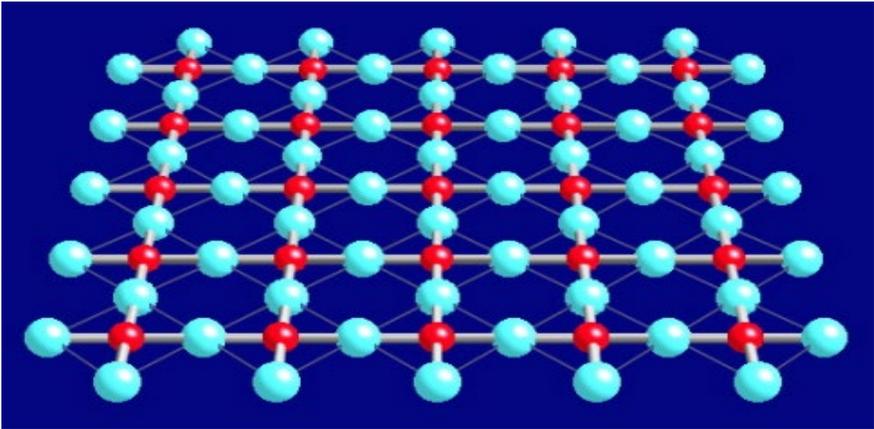
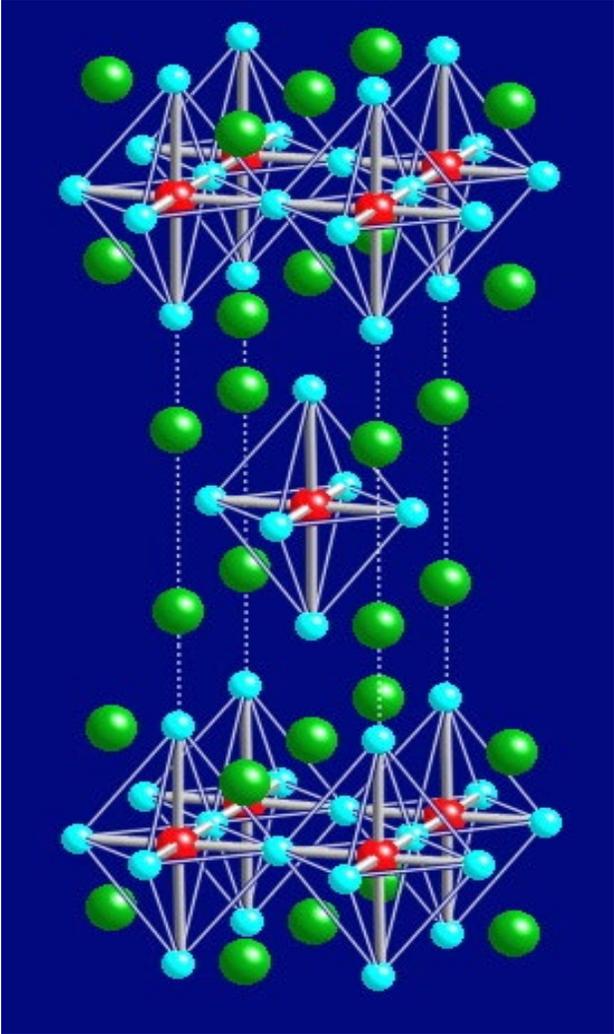
https://commons.wikimedia.org/wiki/File:Cuprates_phasediagram_en.svg

Cuprates: Magnetism, Charge Order and Superconductivity

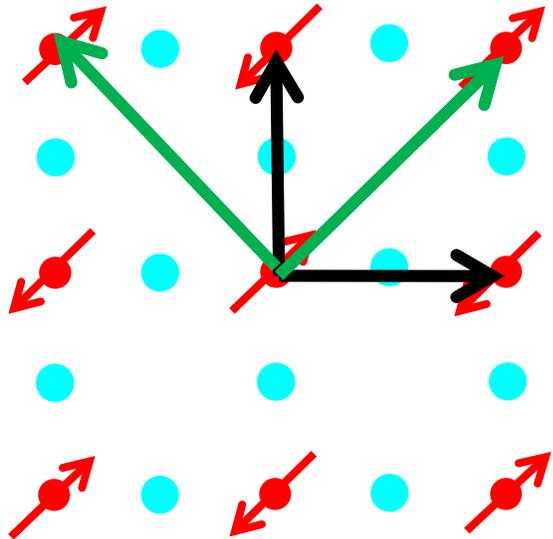


J. Pellicari and R. Comin *Nature Materials* **17**, 661 (2018)

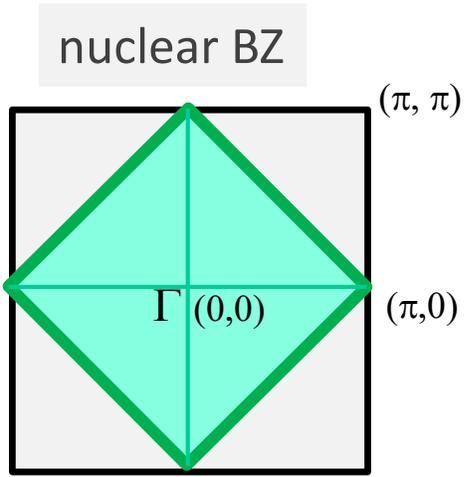
La₂CuO₄: 2D spin 1/2 Heisenberg AF insulator



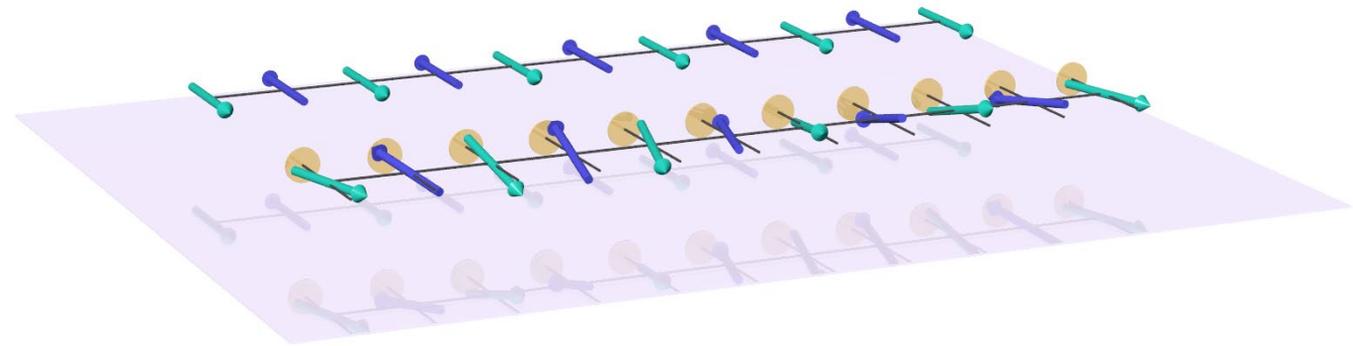
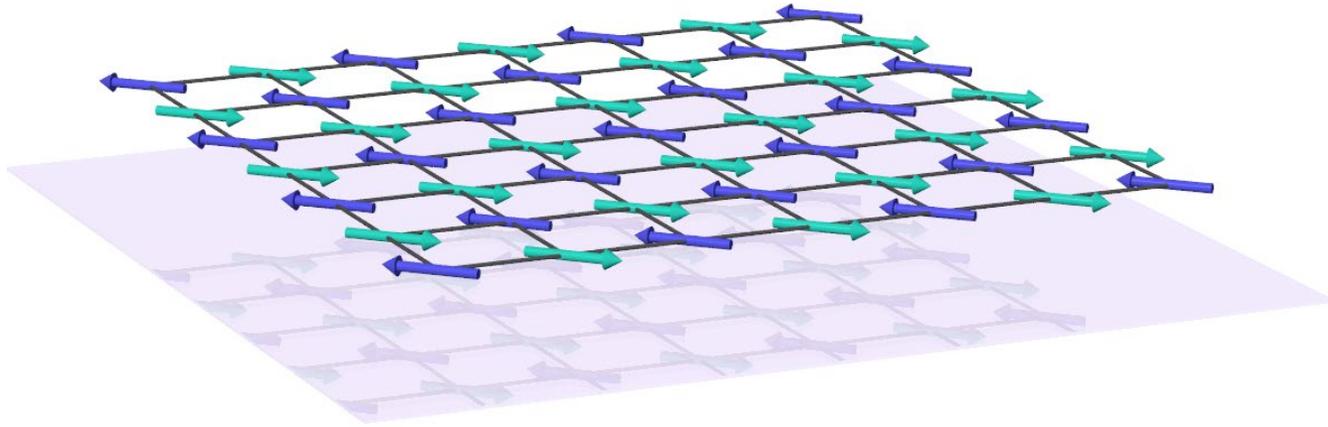
DIRECT SPACE



RECIPROCAL SPACE

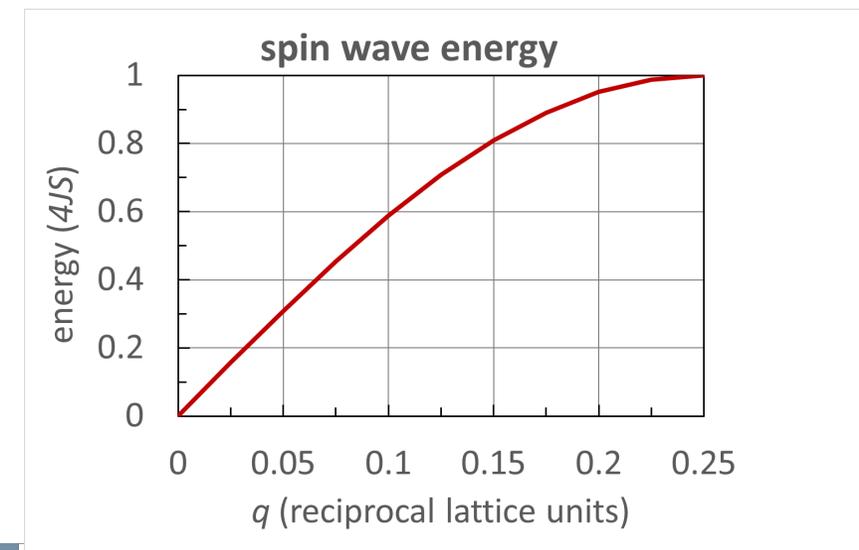


Elementary magnetic excitations are spin waves

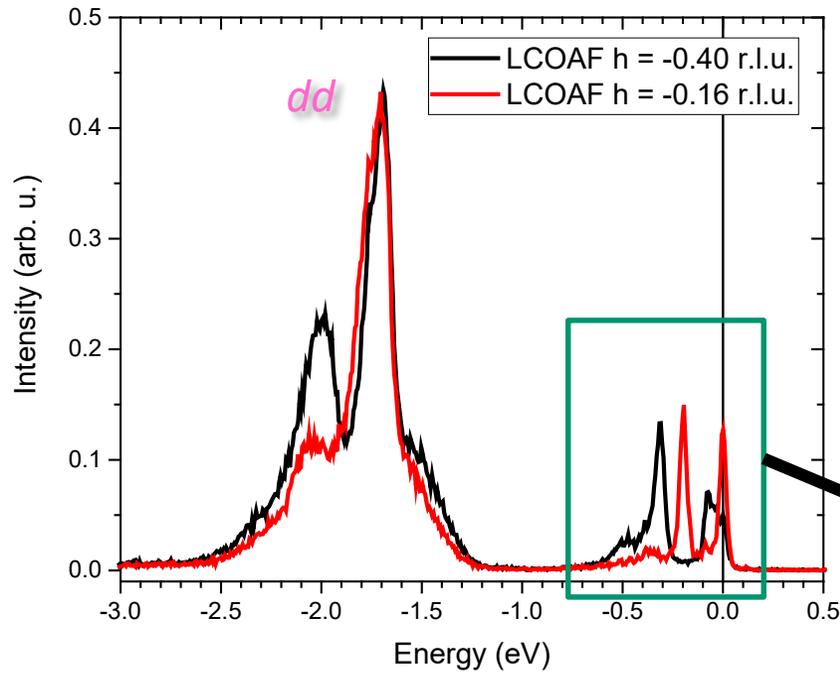


Part 4

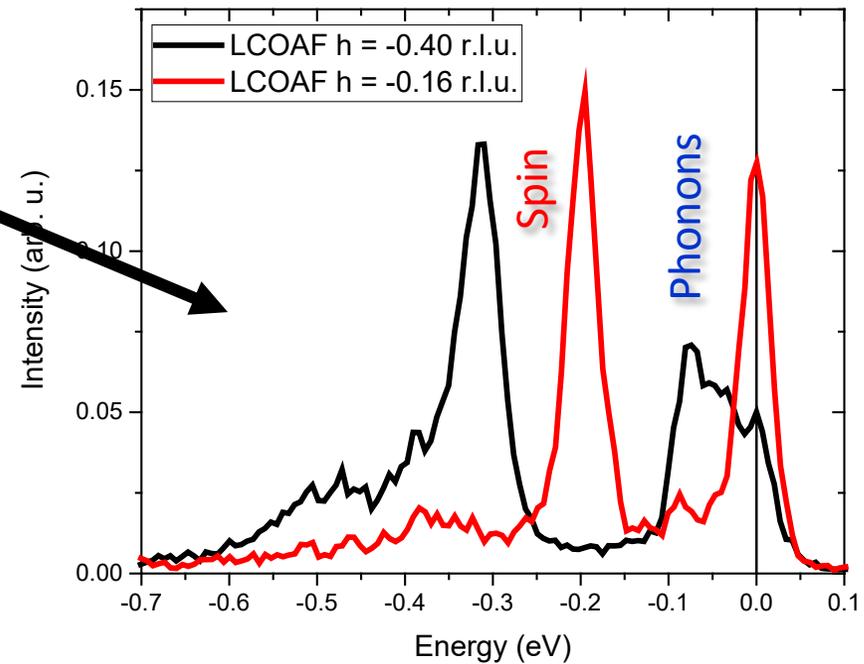
SPIN EXCITATIONS



High energy resolution is needed to look at spin excitations



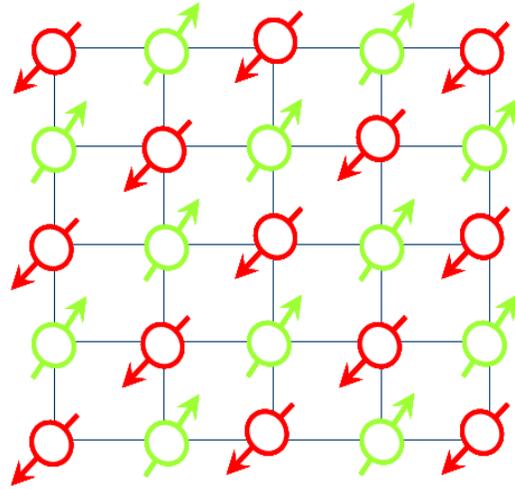
La₂CuO₄
40 meV resolution
30 min accumulation



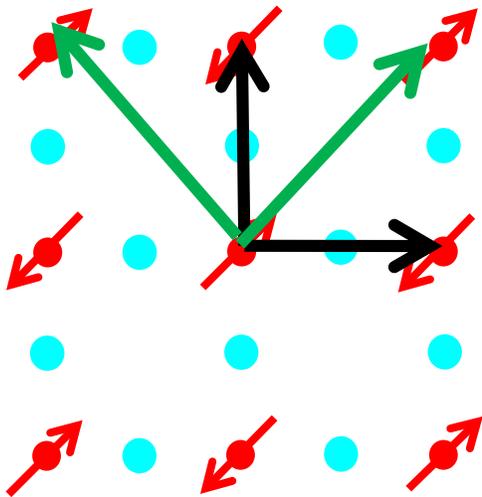
Instrumental BW of RIXS today: ~30 meV (at ESRF ID32, DLS I21, NSLS II SIX)

Spin excitations in cuprates: neutron scattering

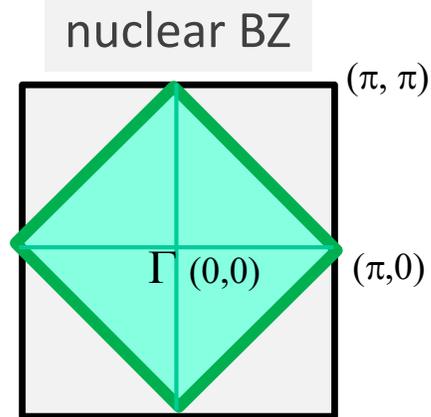
2D AF
Square lattice



DIRECT SPACE

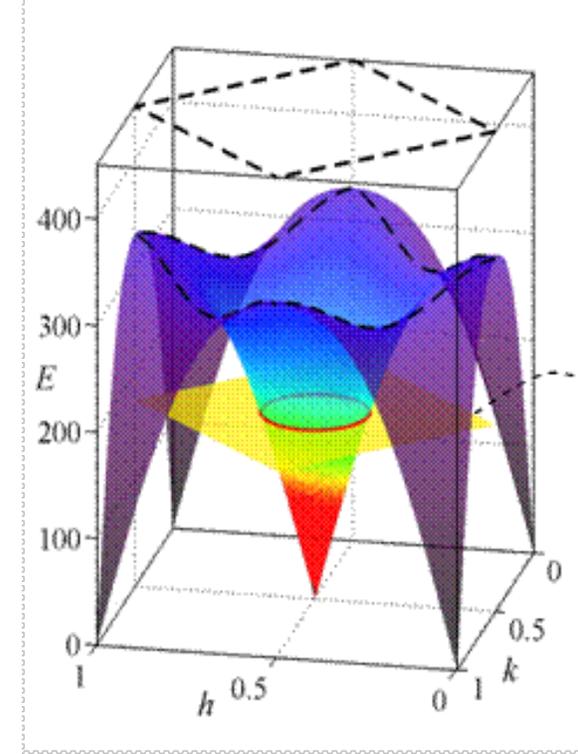
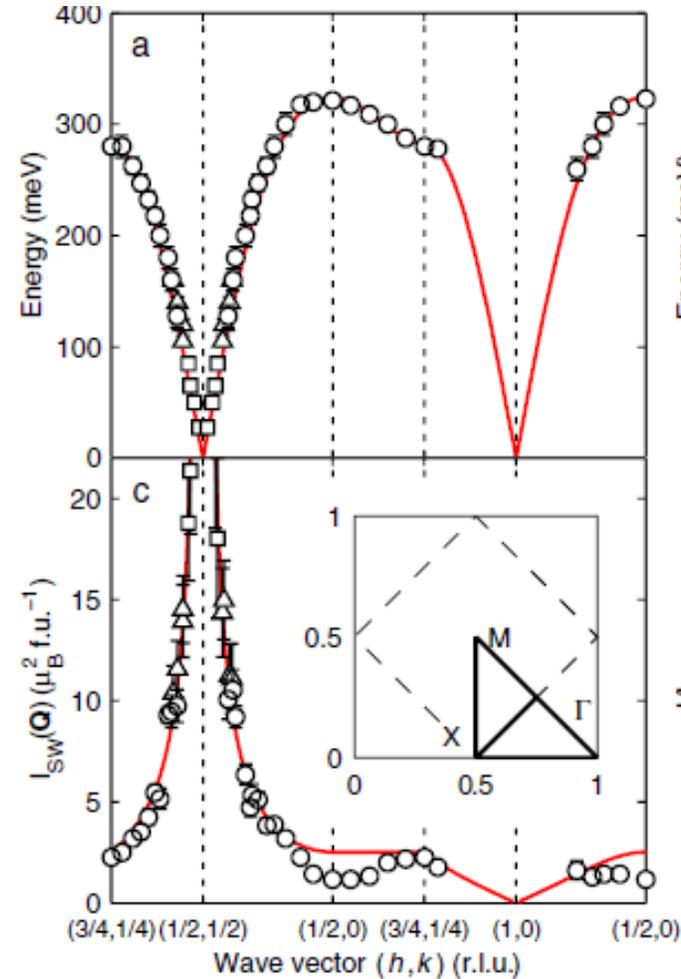


RECIPROCAL SPACE



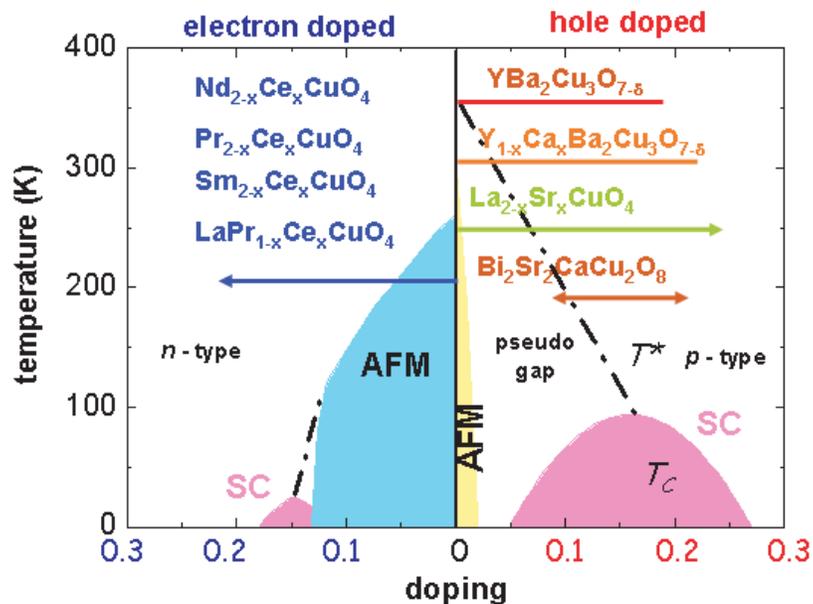
magnetic BZ

INS: La_2CuO_4

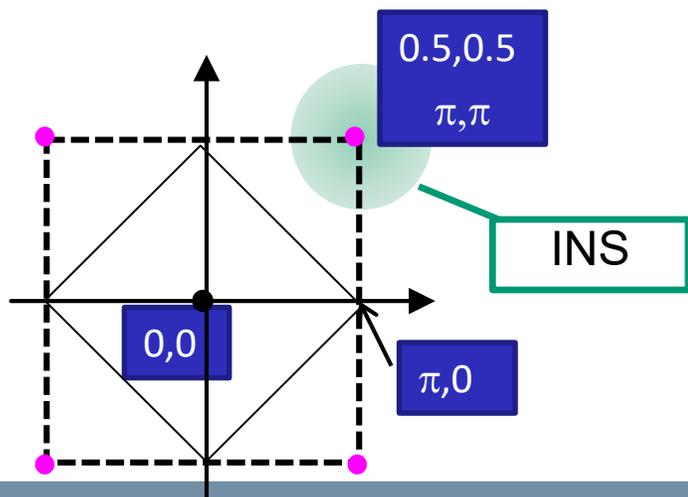


N. S. Headings, S. M. Hayden, R. Coldea, and T. G. Perring,
Phys Rev Lett. **105** 247001 (2011)

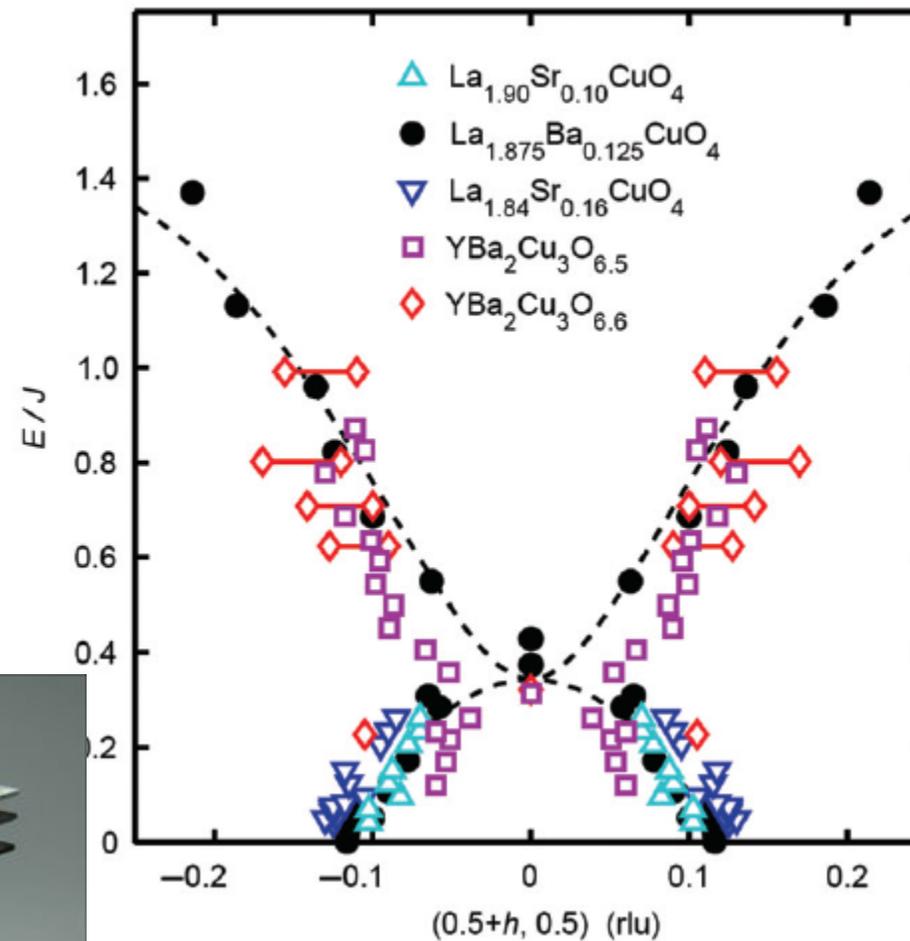
Spin excitations in HTcS: doped SC



http://for538.wmi.badw.de/projects/P4_crystal_growth/index.htm

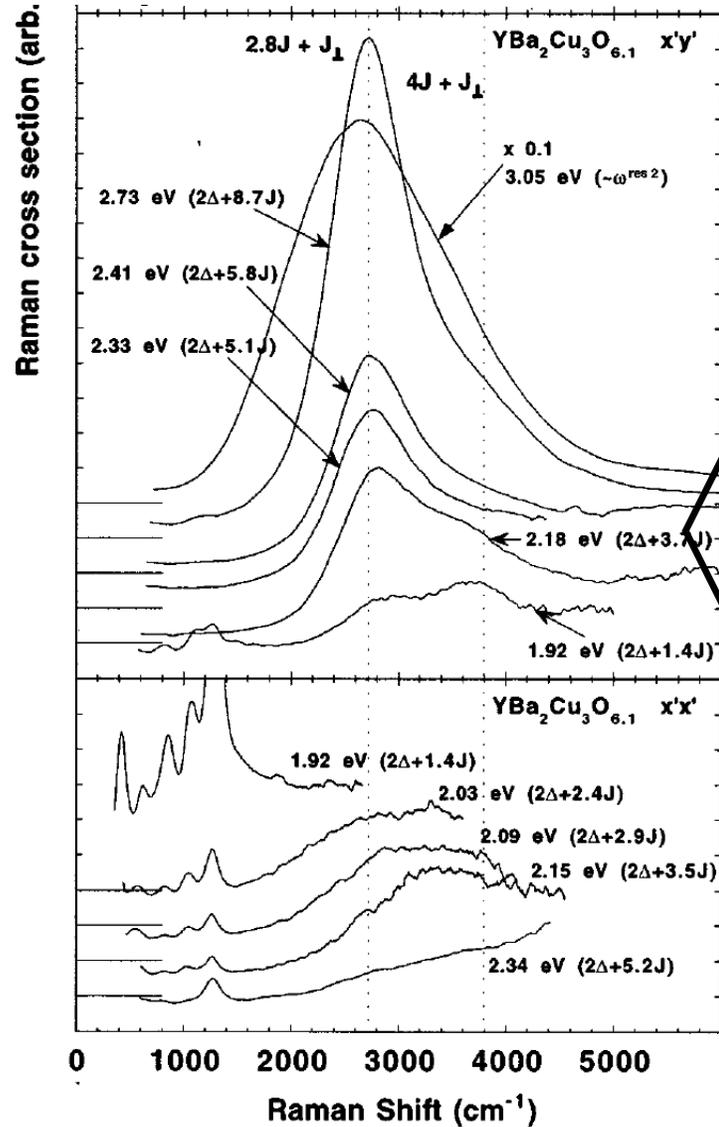


V. Hinkov et al, Eur. Phys. J. Special Topics 188, 113–129 (2010)



J.M. Tranquada, in *Handbook of High-Temperature Superconductivity: Theory and Experiment*, J.R. Schrieffer and J.S. Brooks, eds., Springer, 2007,

RIXS for spin excitations



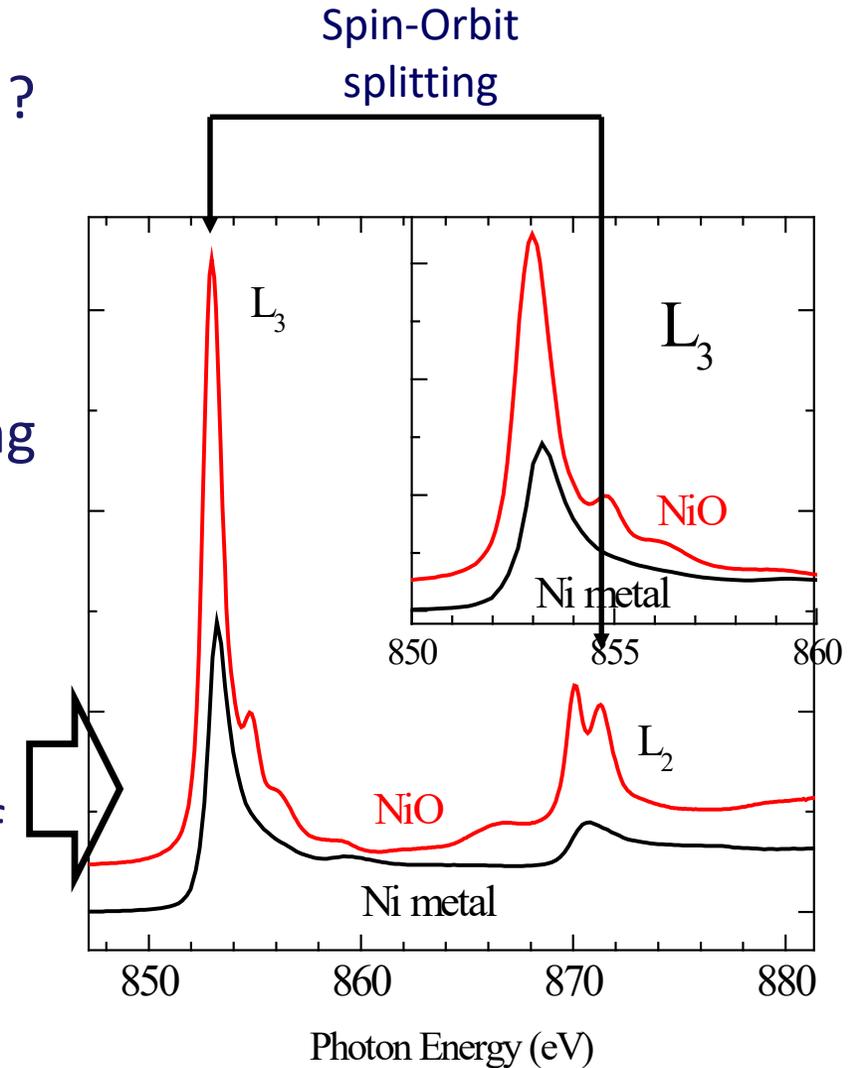
How can an x-ray photon reverse an electron spin, $\Delta S=1$?

We have learned that in radiative transitions the spin is conserved: $\Delta s_i=0$.

Indeed in Raman light scattering and optical absorption only bimagnons can be probed:

$\Delta S=0$.

The secret is in the large spin-orbit interaction of 2p states of the 3dTM (Cu, Ni, etc), 10-20 eV.

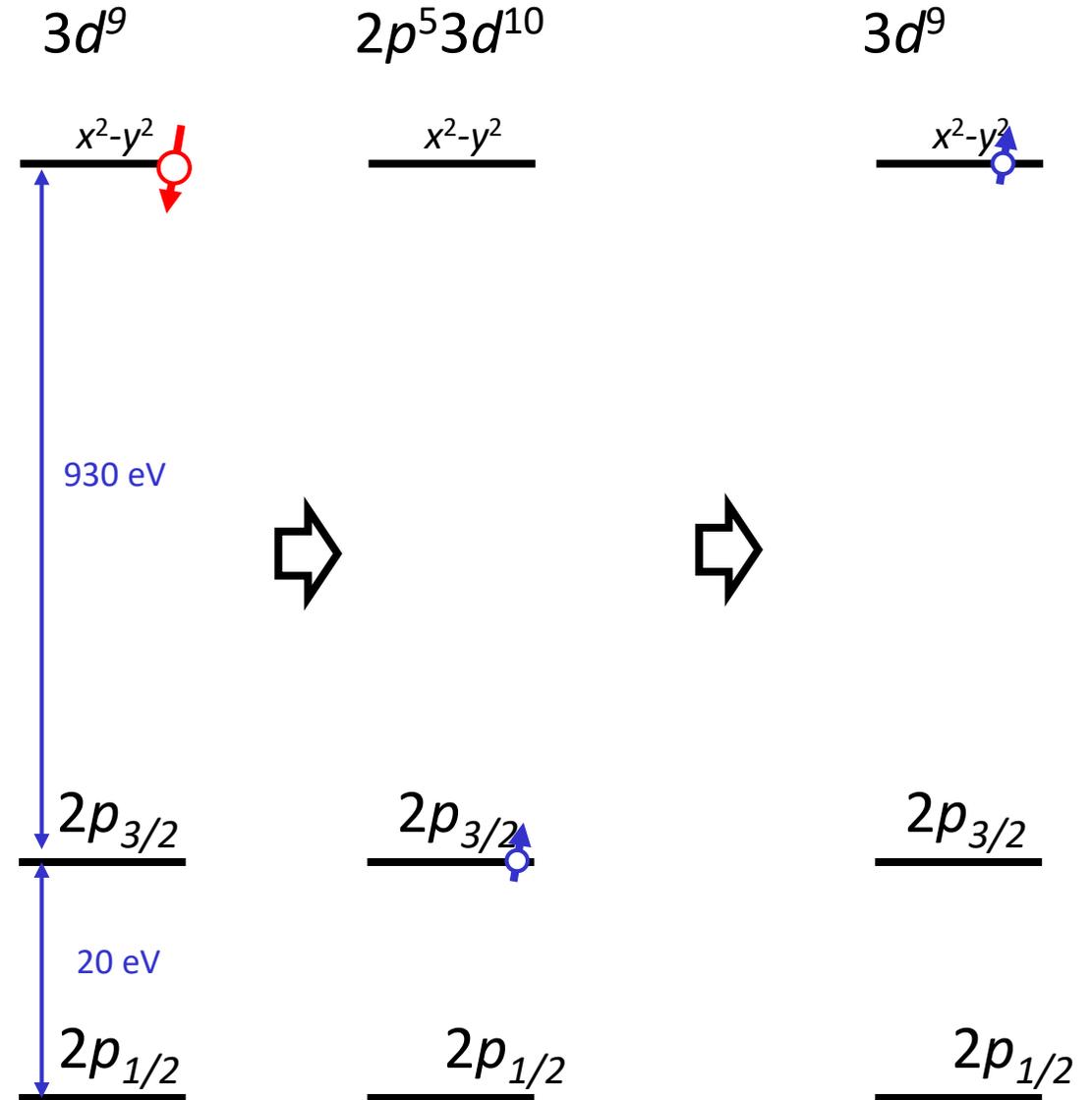


spin-flip excitations and the $2p$ S-O coupling

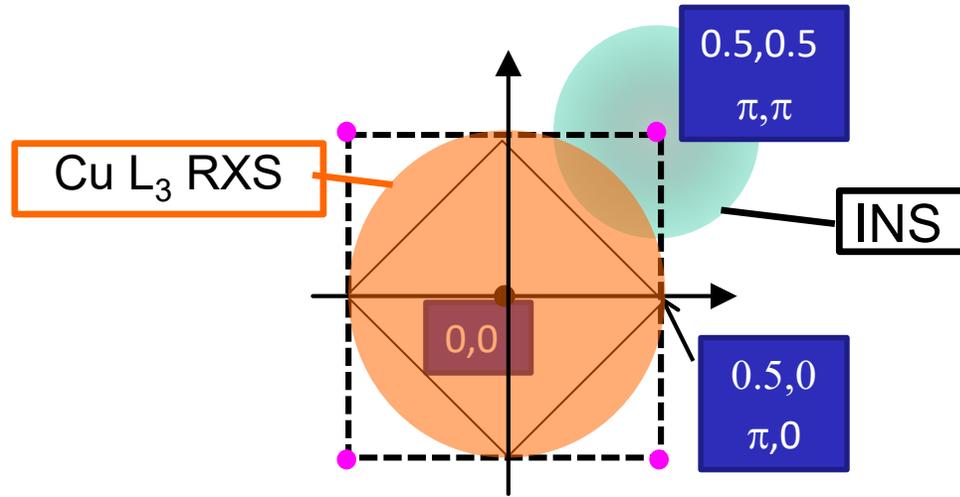
$3d$	E_g	$d_{3z^2-r^2}$ $Y_{2,0}$
		$d_{x^2-y^2}$ $\frac{Y_{2,2}-Y_{2,-2}}{\sqrt{2}}$
T_{2g}		d_{xy} $-i\frac{Y_{2,2}-Y_{2,-2}}{\sqrt{2}}$
		d_{yz} $i\frac{Y_{2,1}+Y_{2,-1}}{\sqrt{2}}$
		d_{zx} $-\frac{Y_{2,1}-Y_{2,-1}}{\sqrt{2}}$

The $3d$ spin must not be pure UP or DOWN

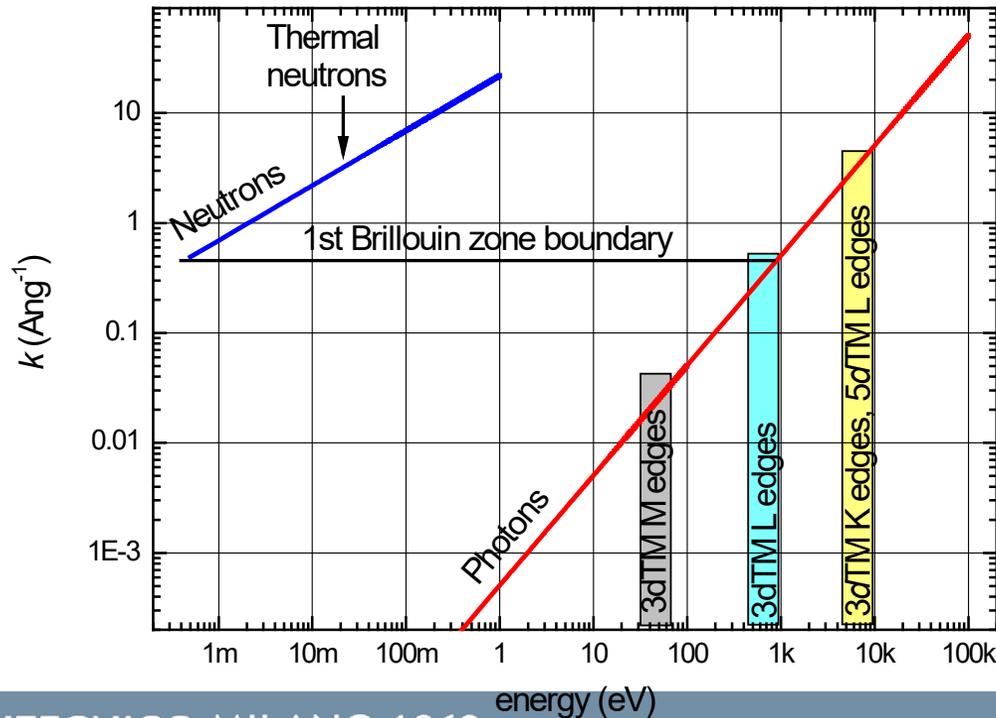
$2p_{3/2}$			
$ \frac{3}{2}, \frac{3}{2}\rangle$	$ \frac{3}{2}, \frac{1}{2}\rangle$	$ \frac{3}{2}, -\frac{1}{2}\rangle$	$ \frac{3}{2}, -\frac{3}{2}\rangle$
$Y_{1,1}^\uparrow$	$\frac{\sqrt{2}}{\sqrt{3}}Y_{1,0}^\uparrow + \frac{1}{\sqrt{3}}Y_{1,1}^\downarrow$	$\frac{1}{\sqrt{3}}Y_{1,-1}^\uparrow + \frac{\sqrt{2}}{\sqrt{3}}Y_{1,0}^\downarrow$	$Y_{1,-1}^\downarrow$
$2p_{1/2}$			
$ \frac{1}{2}, \frac{1}{2}\rangle$	$ \frac{1}{2}, -\frac{1}{2}\rangle$		
$-\frac{1}{\sqrt{3}}Y_{1,0}^\uparrow + \frac{\sqrt{2}}{\sqrt{3}}Y_{1,1}^\downarrow$	$-\frac{\sqrt{2}}{\sqrt{3}}Y_{1,-1}^\uparrow + \frac{1}{\sqrt{3}}Y_{1,0}^\downarrow$		



RIXS: Experimental conditions

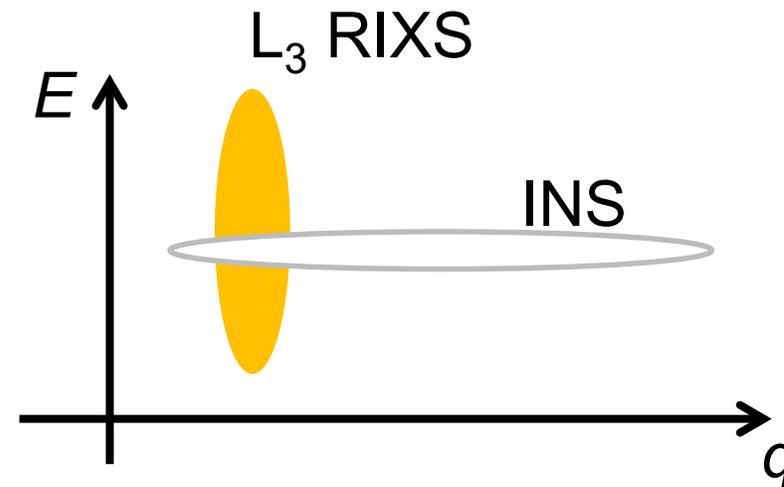


Wavevector of particles used in inelastic scattering

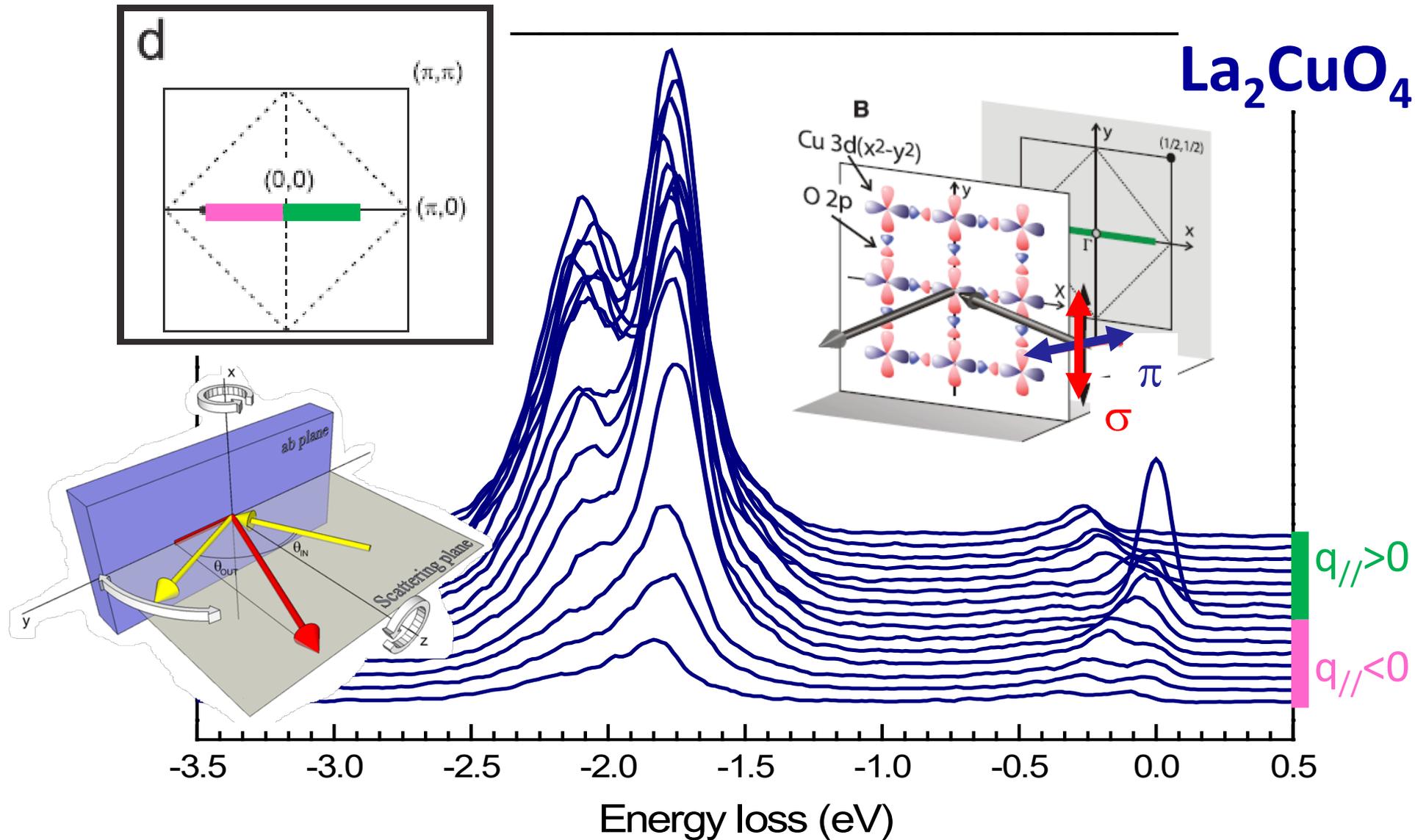


Cu L₃ resonance:

- $E_0 = 930 \text{ eV}$
- $q_{\text{max}} = 0.86 \text{ Ang}^{-1}$
- confined inside a region around Γ
- 2p core hole: spin-orbit interaction
- E resolution: 30-50 meV
- q resolution: 0.005 rlu
- 5-15 min per spectrum



First demonstration: La_2CuO_4



Theory of magnetic RIXS (1)

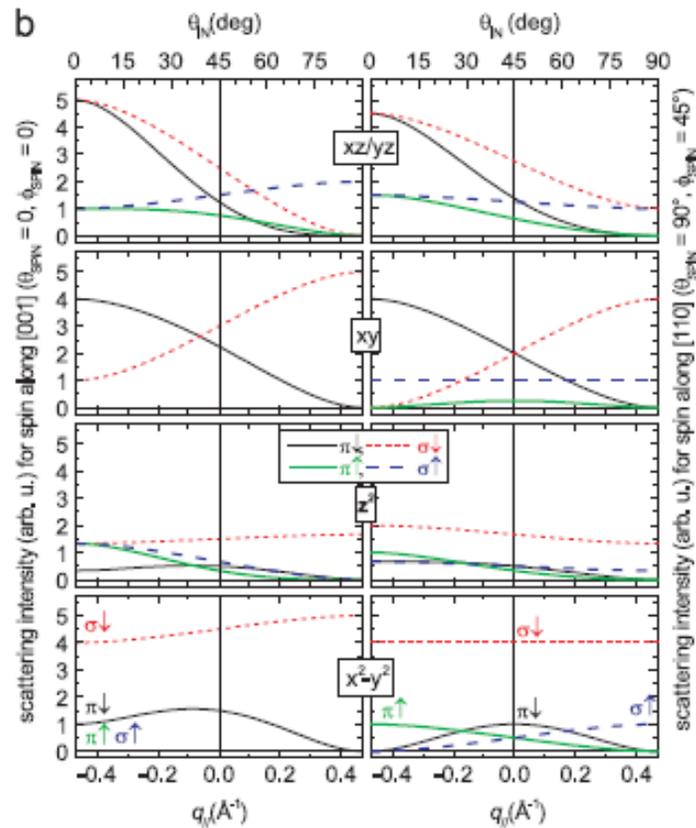
PRL 103, 117003 (2009)

PHYSICAL REVIEW LETTERS

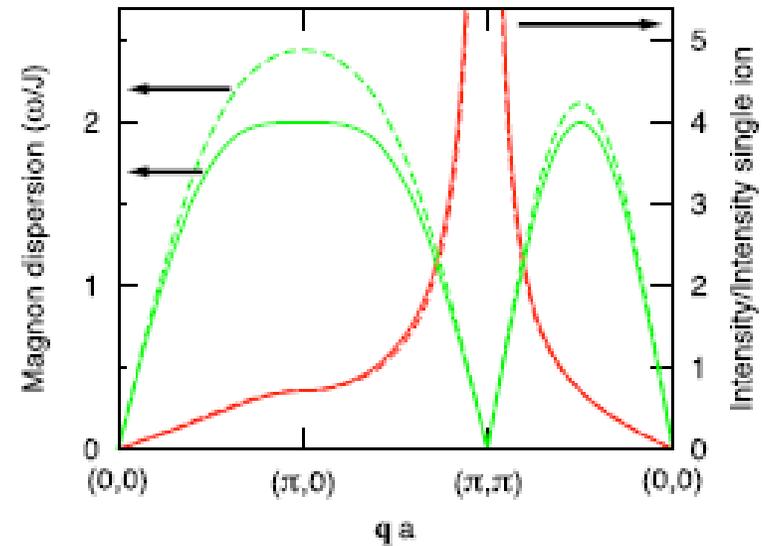
week ending
11 SEPTEMBER 2009

Theoretical Demonstration of How the Dispersion of Magnetic Excitations in Cuprate Compounds can be Determined Using Resonant Inelastic X-Ray Scattering

Luuk J.P. Ament,^{1,4} Giacomo Ghiringhelli,² Marco Moretti Sala,² Lucio Braicovich,² and Jeroen van den Brink^{1,3,4}



Single ion cross section



Linear spin wave theory

Theory of magnetic RIXS (2)

PRL 105, 167404 (2010)

PHYSICAL REVIEW LETTERS

week ending
15 OCTOBER 2010

Theory of Resonant Inelastic X-Ray Scattering by Collective Magnetic Excitations

M. W. Haverkort

Max Planck Institute for Solid State Research, Heisenbergstraße 1, D-70569 Stuttgart Germany
(Received 9 October 2009; published 15 October 2010)

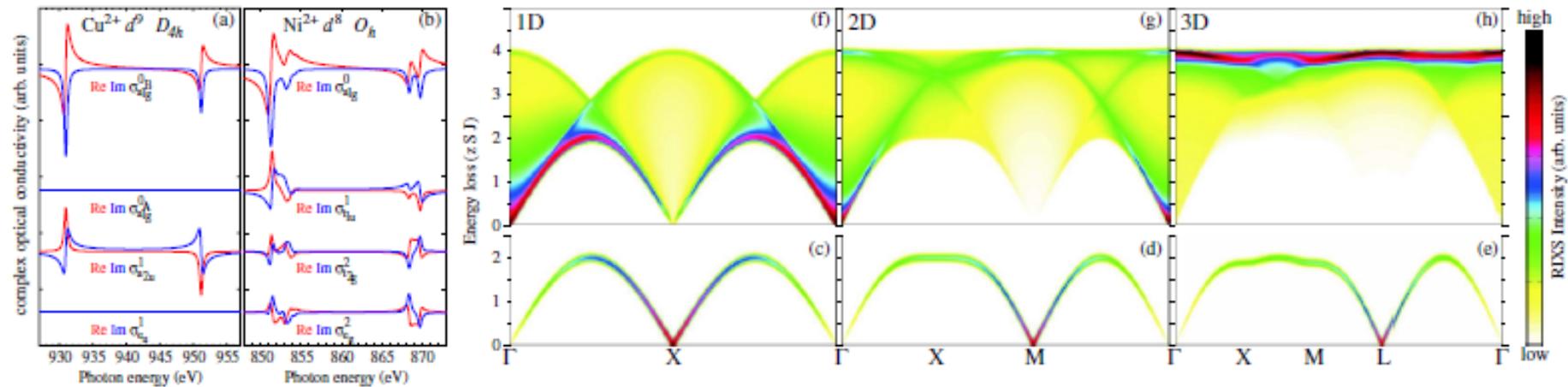
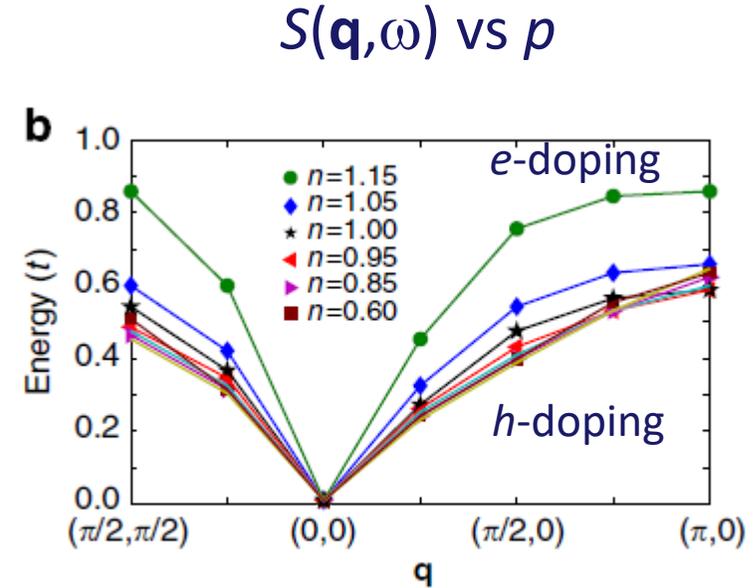
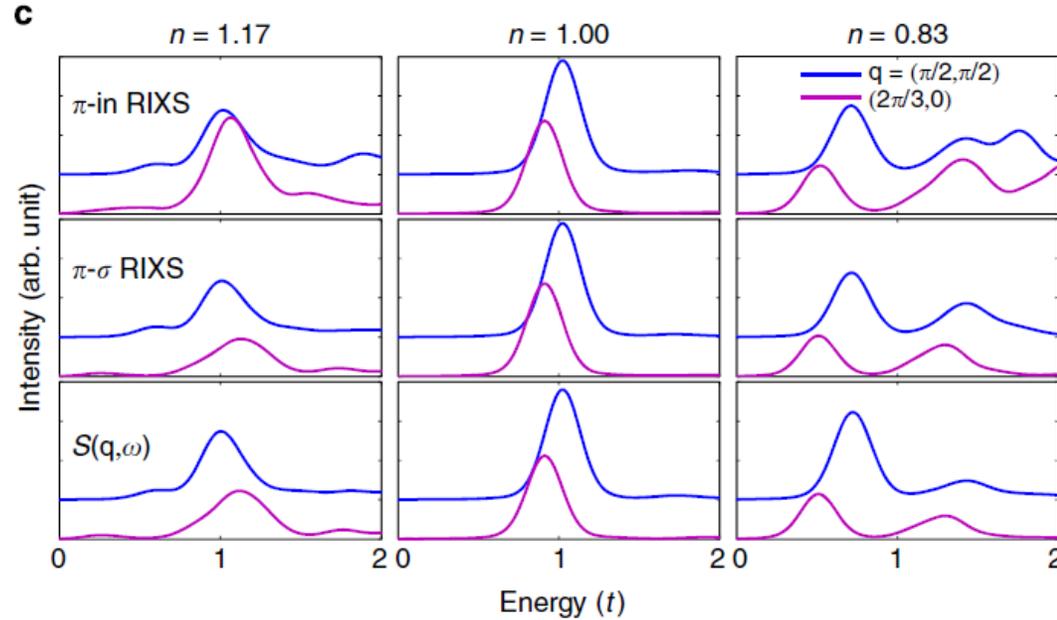


FIG. 1 (color online). Left: Fundamental x-ray absorption spectra that enter into the RIXS transition operator as energy dependent complex matrix elements calculated for (a) Cu^{2+} and (b) Ni^{2+} . Right: The Cu^{2+} and Ni^{2+} one magnon (c)–(e) and Ni^{2+} two magnon (f)–(h) RIXS spectral function, calculated using linear spin-wave theory for a 1D chain (c),(f), a 2D square (d),(g), and a 3D cubic (e),(h) Heisenberg model in energy loss units of zSJ (number of neighbors \times spin \times exchange constant).

Theory of magnetic RIXS (3)

What is the relation between RIXS
and $S(\mathbf{q},\omega)$?

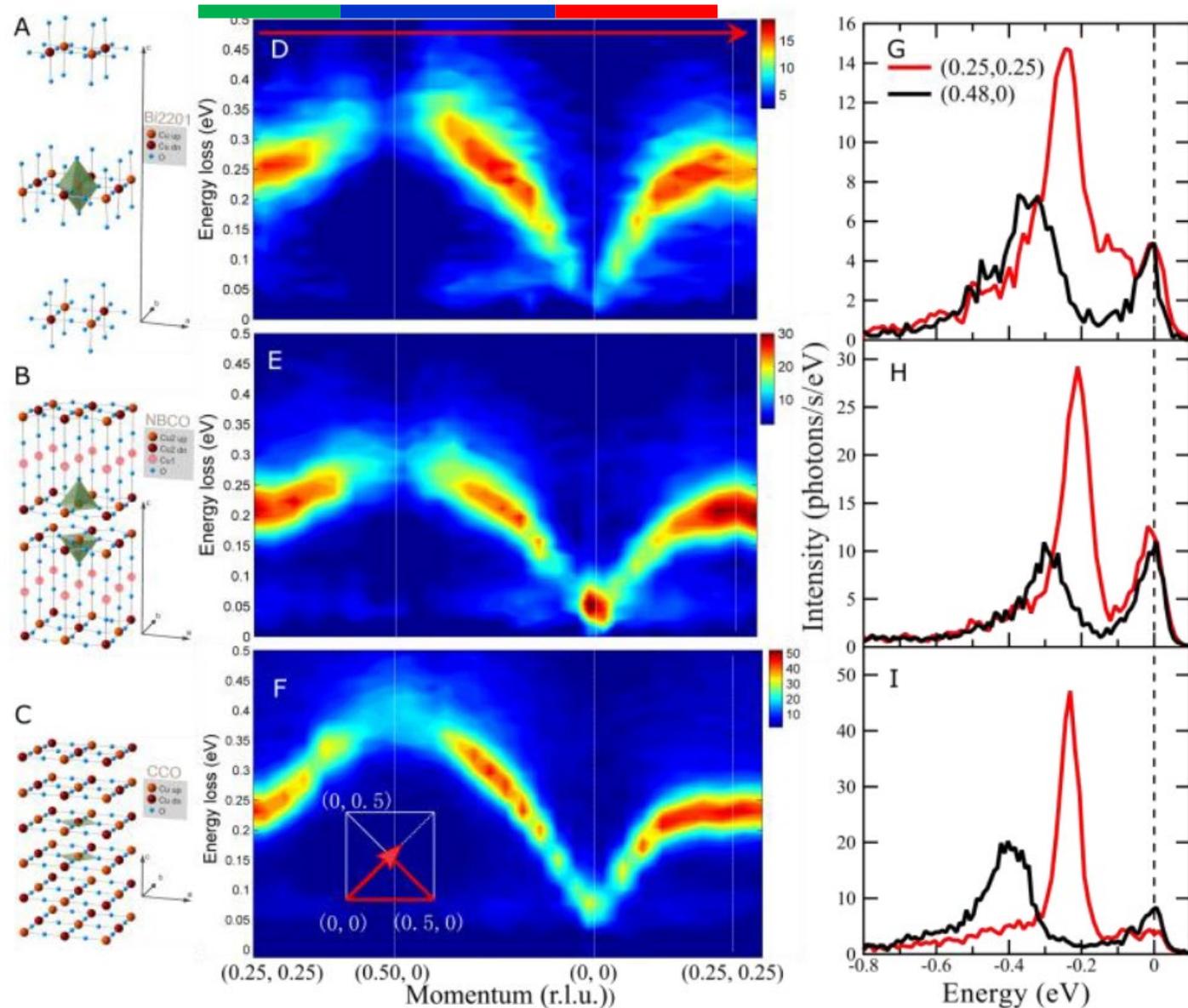


RIXS measures $S(\mathbf{q},\omega)$ quite well

Spin excitations harden with e -
doping, and change very little
with h -doping.

C.J. Jia, E.A. Nowadnick, K. Wohlfeld, Y.F. Kung, C.-C. Chen, S. Johnston, T. Tohyama, B. Moritz & T.P. Devereaux, NATURE COMMUNICATIONS, 5:3314 (2014)

Spin-waves with Cu L₃ RIXS

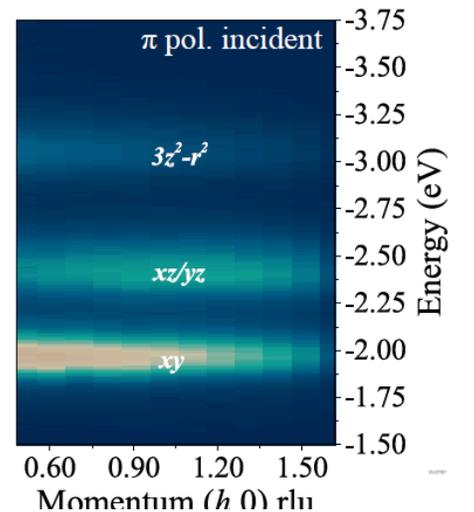
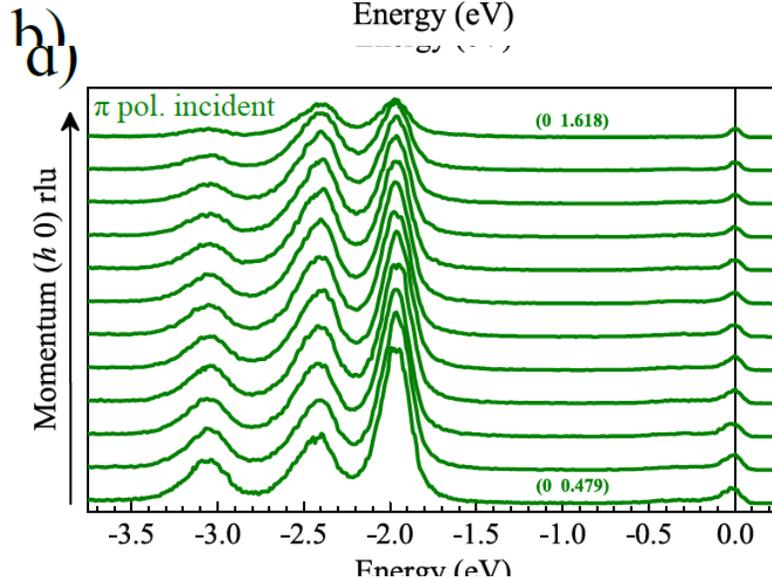
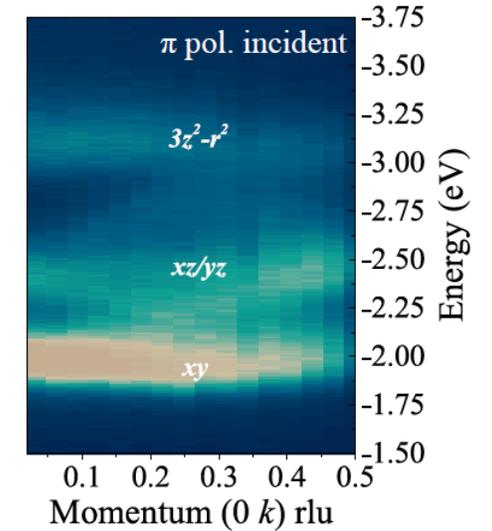
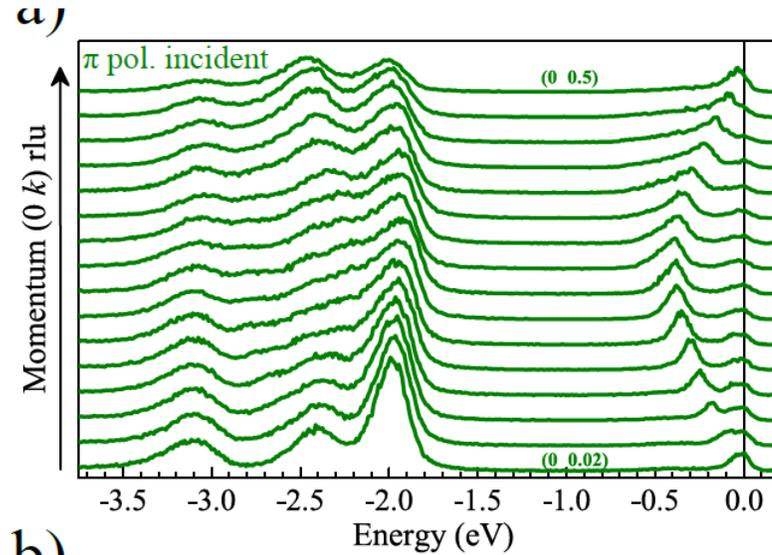
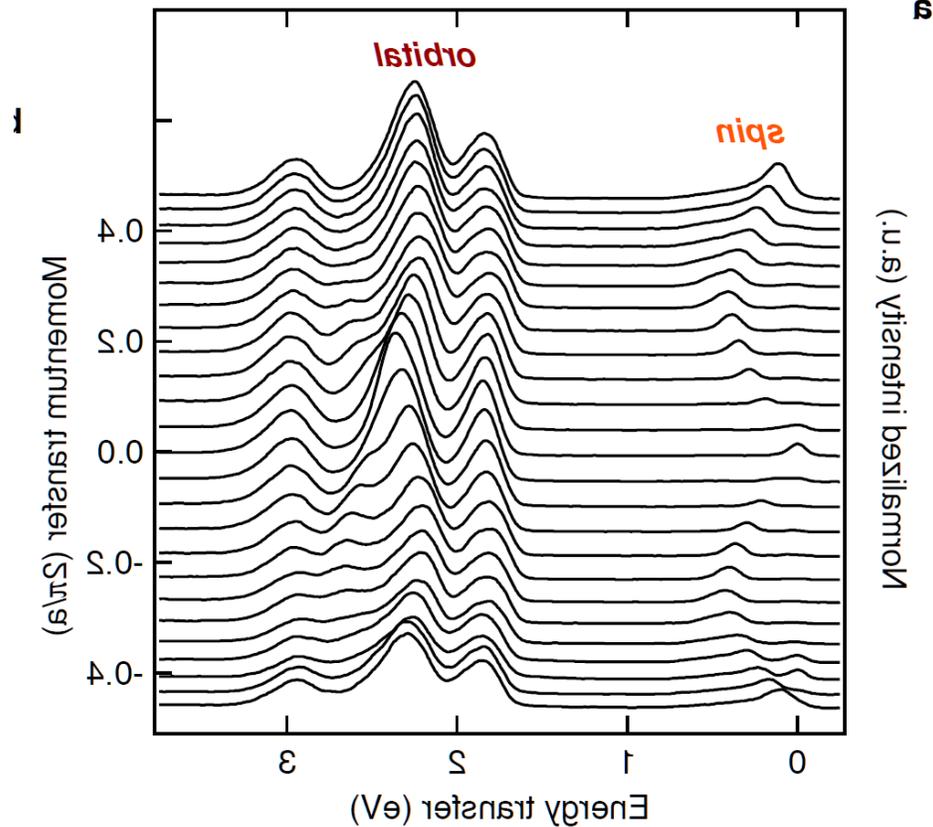


Y. Y. Peng, G. Dellea, M. Minola, M. Conni, A. Amorese, D. Di Castro, G. M. De Luca, K. Kummer, M. Salluzzo, X. Sun, X. J. Zhou, G. Balestrino, M. Le Tacon, B. Keimer, L. Braicovich, N. B. Brookes and G. Ghiringhelli, *Nature Physics* **13** 1201

Quasi 1D cuprates: spin and orbital excitations



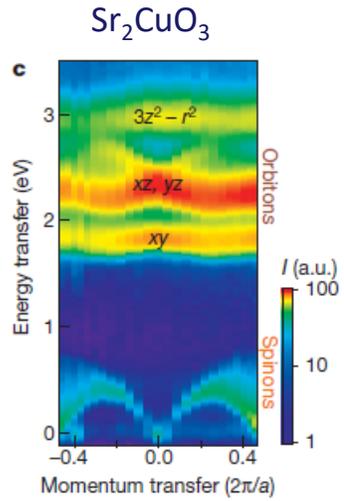
Dispersion along chain direction



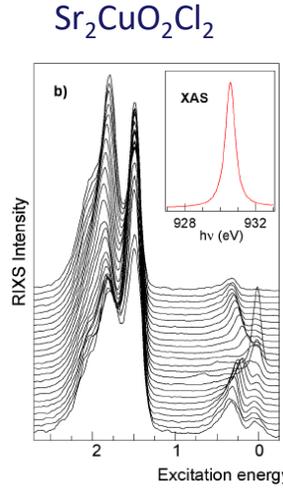
Haverkort, V. N. Strocov, L. Hozoi, C. Monney, S. Nishimoto, S. Singh, A. Revcolevschi, J.-S. Caux, L. Patthey, H. M. Rønnow, J. van den Brink & T. Schmitt, *Nature* **485** 82 (2012)

R. Fumagalli, J. Heverhagen, D. Betto, R. Arpaia, M. Rossi, D. Di Castro, N.B. Brookes, M. Moretti Sala, M. Daghofer, L. Braicovich, K. Wohlfeld, and G. Ghiringhelli, *Phys. Rev. B* **101** 205117 (2020)

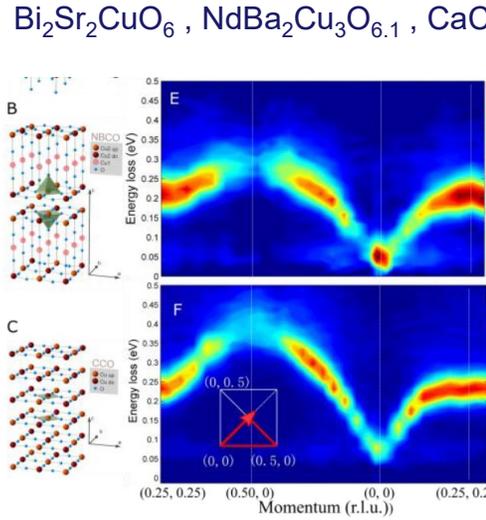
RIXS selected Highlights: spin excitations



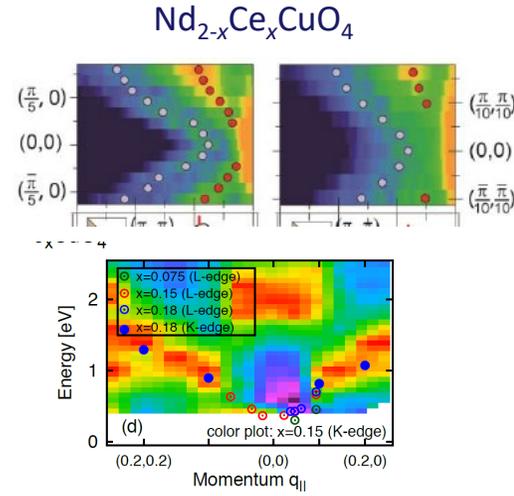
J Schlappa *et al.*, Nature (2012)



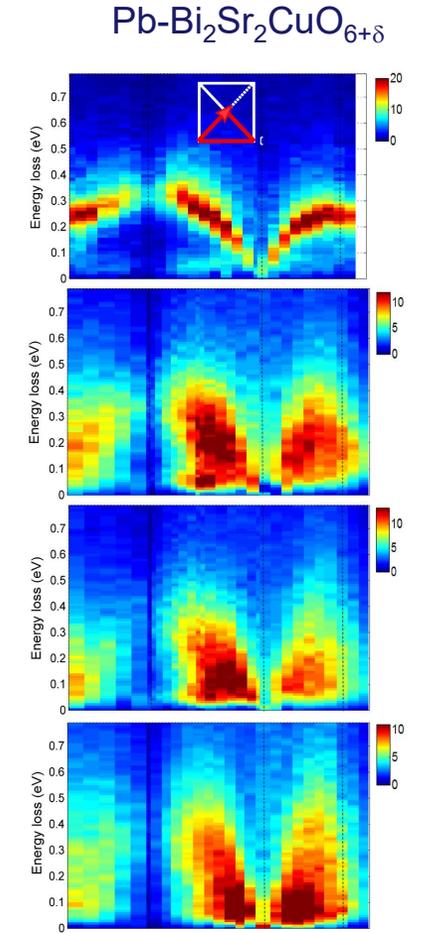
M Guarise, *et al.*, PRL (2010)



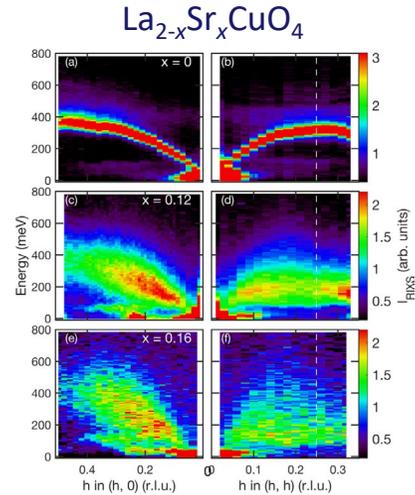
YY Peng, *et al.*, Nat. Phys. (2017)



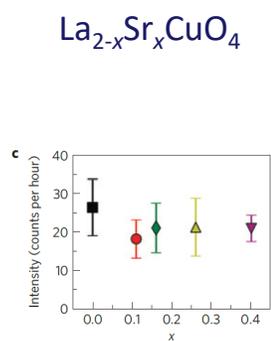
WS Lee, *et al.*, Nat. Phys. (2014)
Kishii, *et al.*, Nat Comm. (2014)



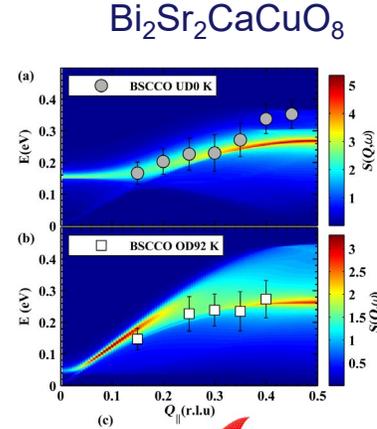
YY Peng, *et al.*, PRB. (2018)



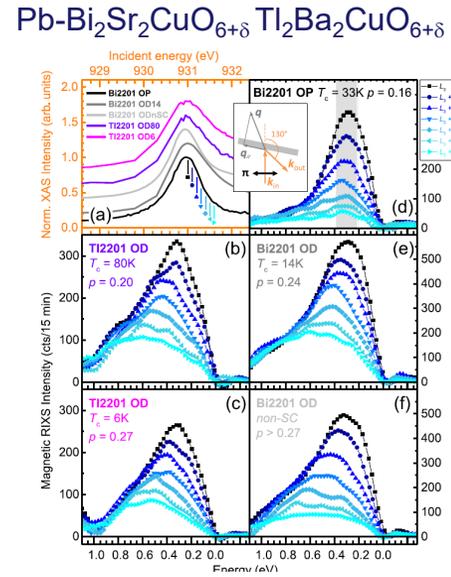
HC Roberts, *et al.*, PRB (2019)



MPM Dean *et al.*, Nat Materials (2013)



MPM Dean *et al.*, PRL (2013)



M Minola *et al.*, PRL (2017)

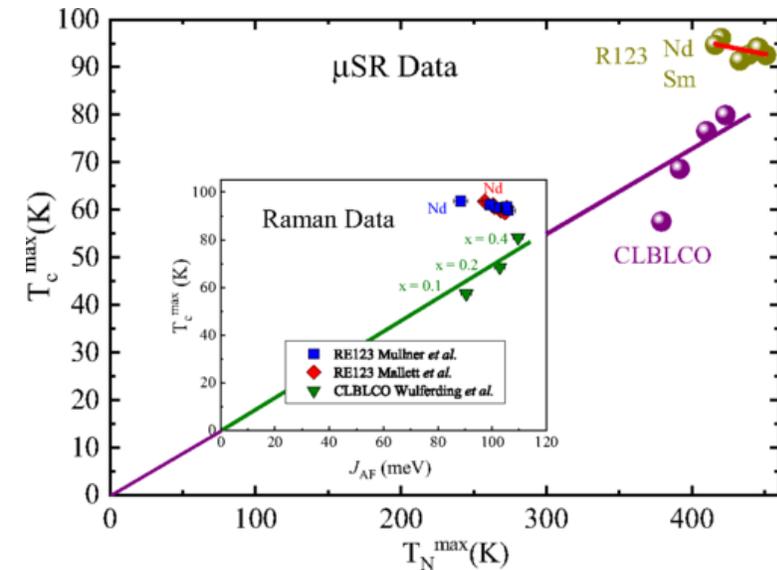
Exchange interaction and superconductivity

REVIEWS OF MODERN PHYSICS, VOLUME 84, OCTOBER–DECEMBER 2012

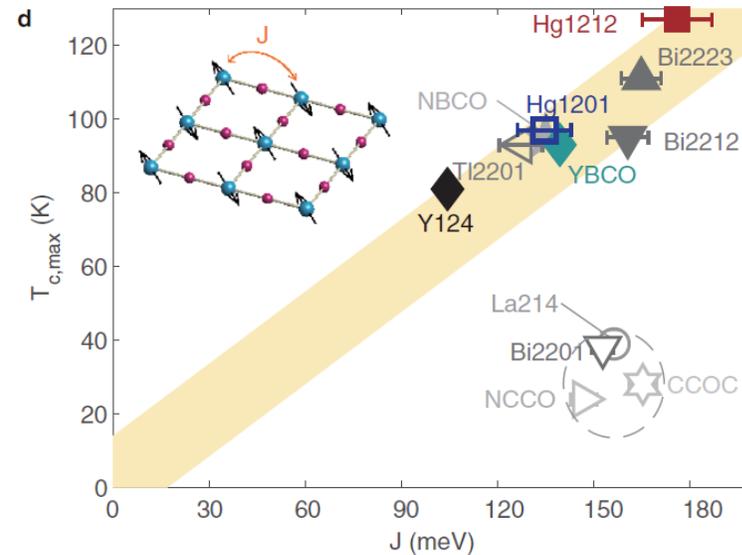
A common thread: The pairing interaction for unconventional superconductors

D. J. Scalapino*

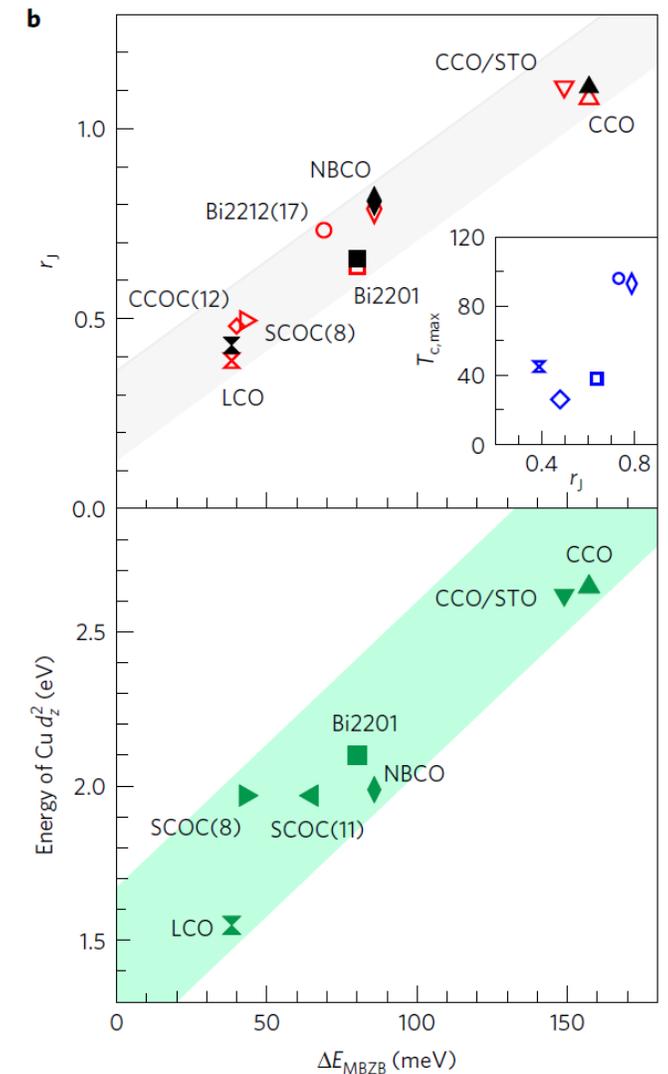
interaction for Hubbard-like models, it is proposed that spin-fluctuation mediated pairing is the common thread linking a broad class of superconducting materials.



Amit Keren, Wayne Crump, Ben P. P. Mallett, Shen V. Chong, Itai Keren, Hubertus Luetkens, and Jeffery L. Tallon, *Phys. Rev. B* **100**, 144512

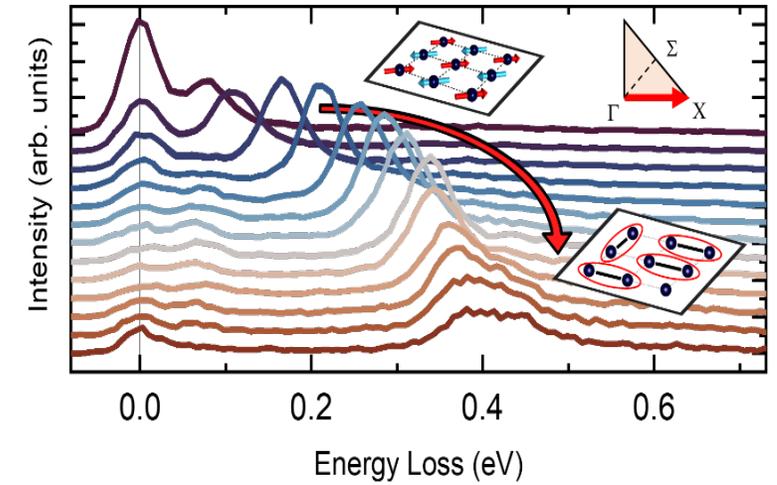
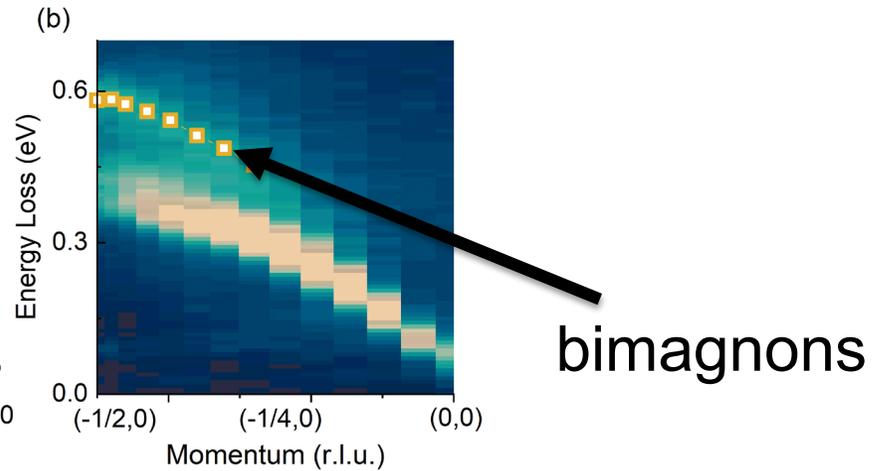
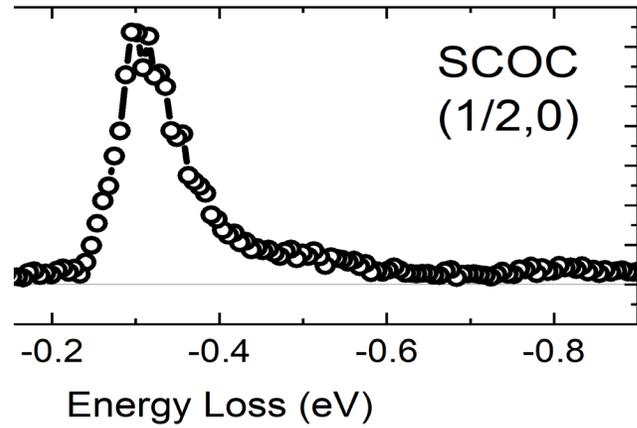
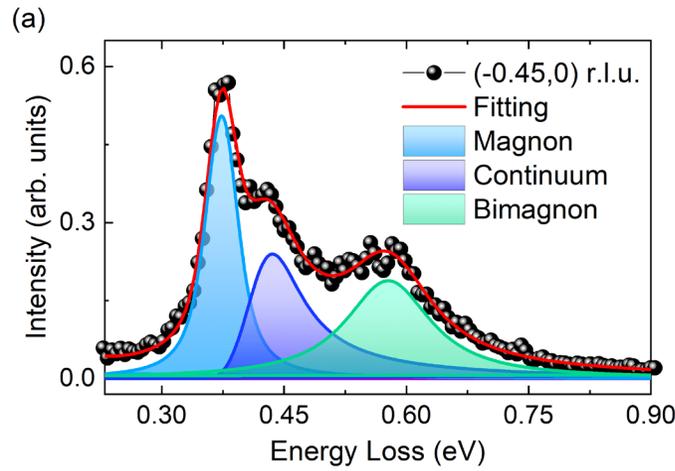
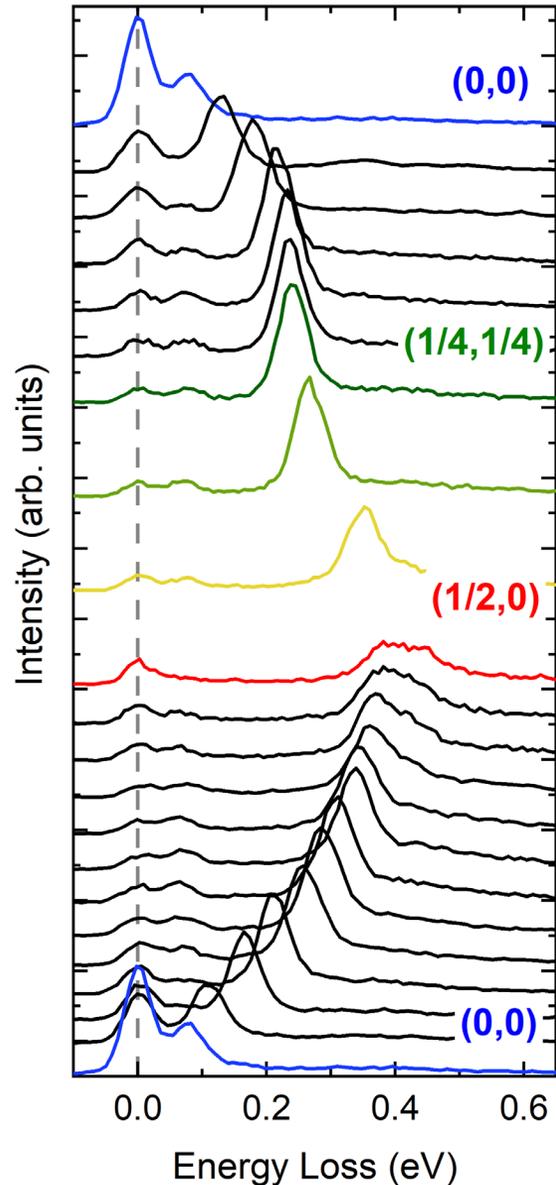


Lichen Wang, Guanhong He, Zichen Yang, Mirian Garcia-Fernandez, Abhishek Nag, Ke-Jin Zhou, Matteo Minola, Matthieu Le Tacon, Yingying Peng, Yuan Li, *Nature Communications* **13**, 3163 (2022)



Y. Y. Peng, G. Dellea, M. Minola, M. Conni, A. Amorese, D. Di Castro, G. M. De Luca, K. Kummer, M. Salluzzo, X. Sun, X. J. Zhou, G. Balestrino, M. Le Tacon, B. Keimer, L. Braicovich, N. B. Brookes and G. Ghiringhelli, *Nature Physics* **13** 1201 (2017)

Deconfined spinon pairs in CaCuO_2

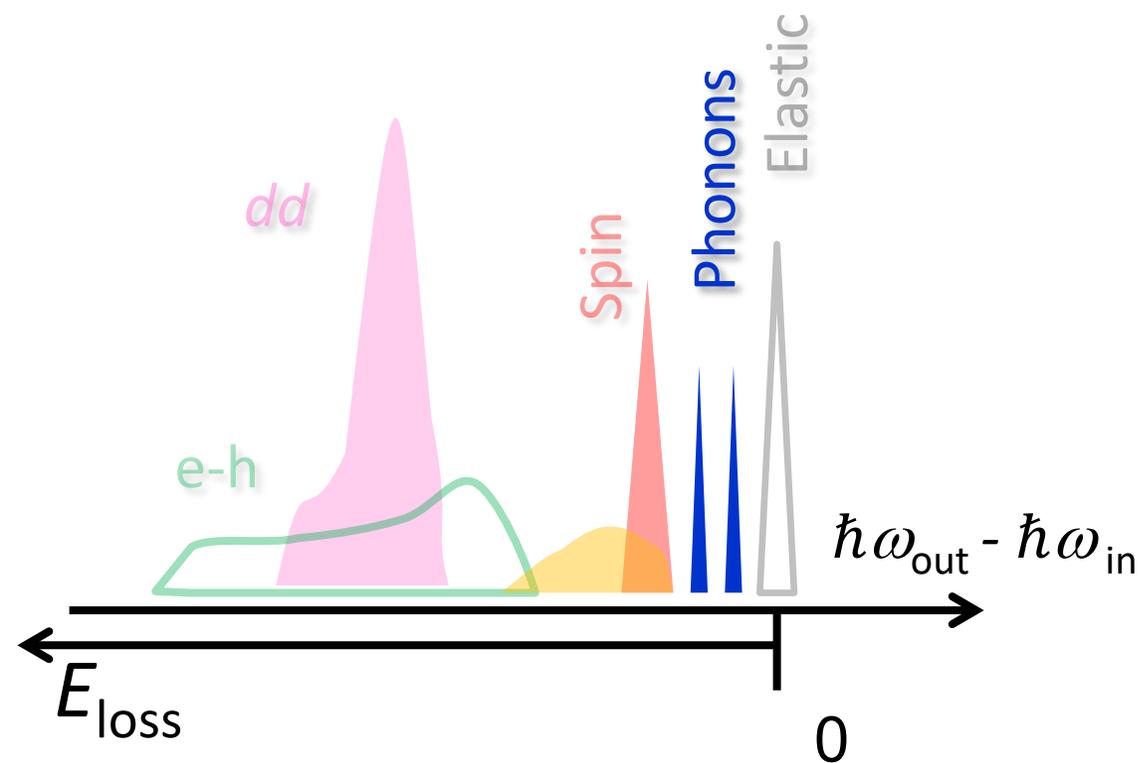


Leonardo Martinelli, Davide Betto, Kurt Kummer, Riccardo Arpaia, Lucio Braicovich, Daniele Di Castro, Nicholas B. Brookes, Marco Moretti Sala, and Giacomo Ghiringhelli, [Phys Rev. X 12, 021041 \(2022\)](#)

Part 5

PHONONS

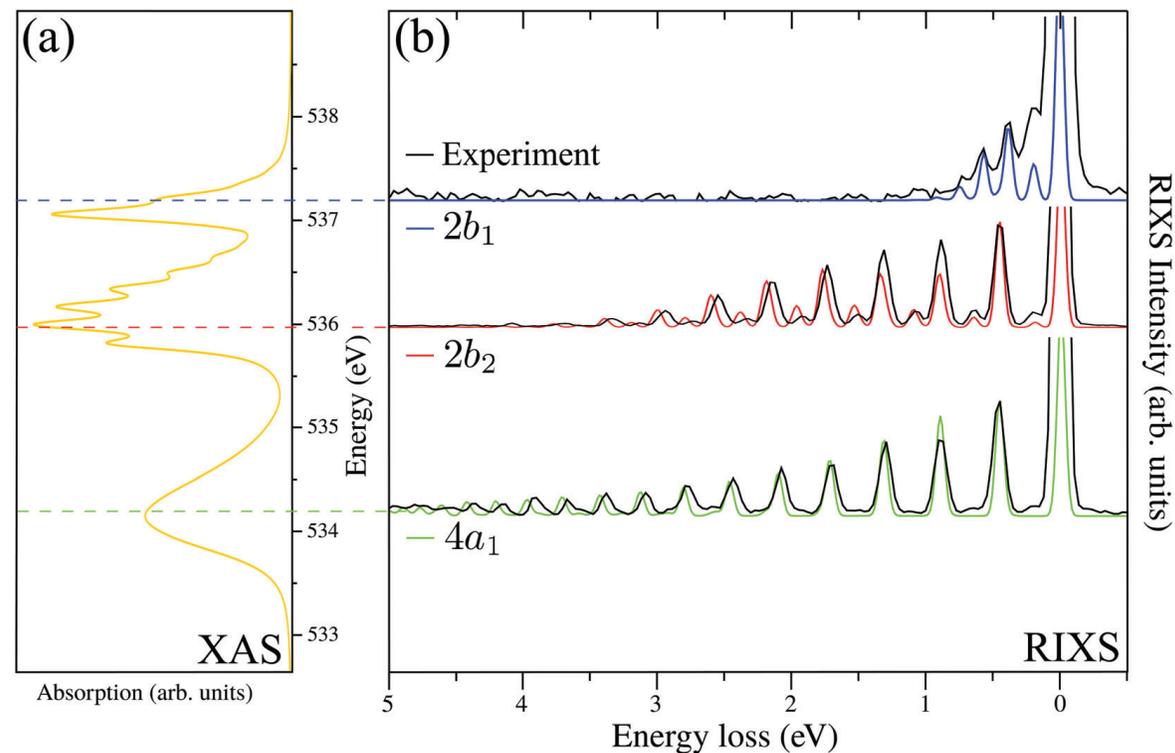
Phonons



Why do we see phonons in RIXS?

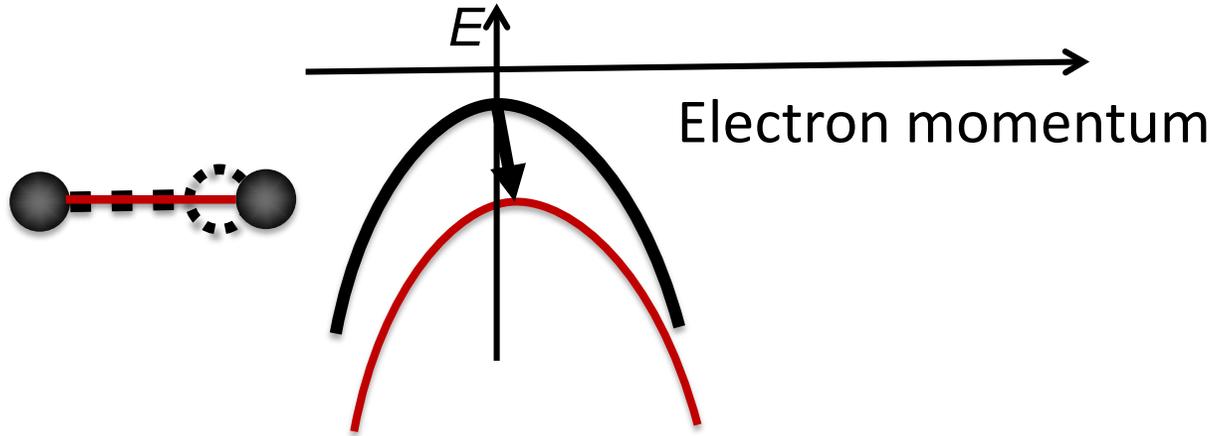
How can we use the phonon signal?

RIXS of water



Vinicius Vaz da Cruz, Emelie Ertan, Rafael C. Couto, Sebastian Eckert, Mattis Fondell, Marcus Dantz, Brian Kennedy, Thorsten Schmitt, Annette Pietzsch, Freddy F. Guimaraes, Hans Ågren, Faris Gel'mukhanov, Michael Odelius, Alexander Fohlisch and Victor Kimberg, *PCCP* **19**, 19573 (2017)

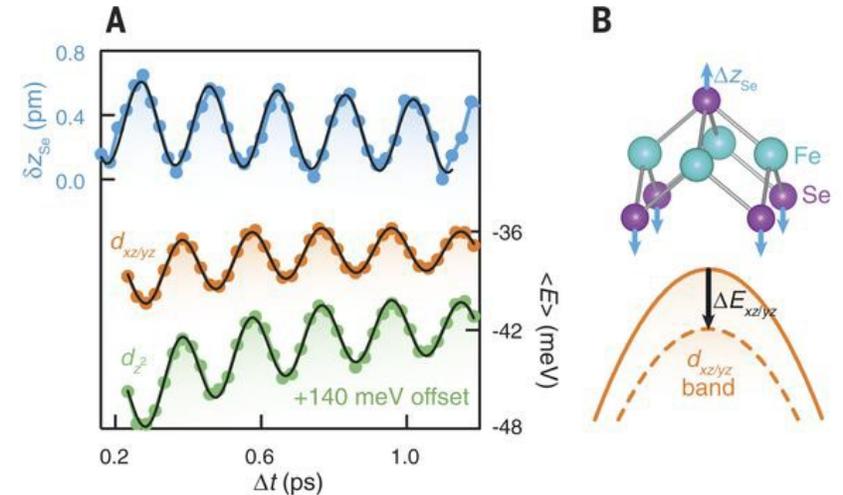
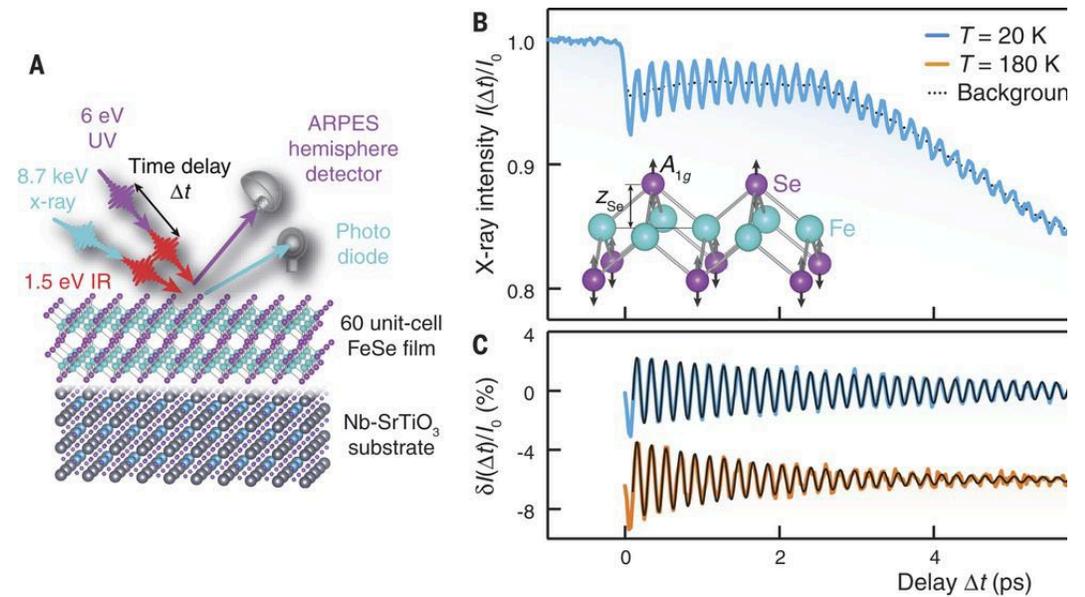
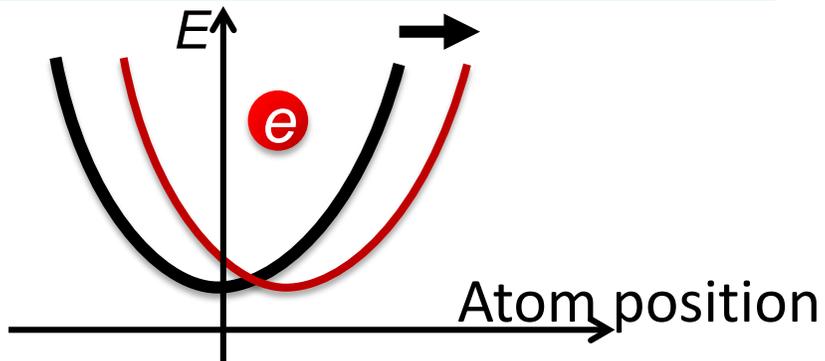
Electron phonon coupling



How \mathcal{H} is modified by an atomic displacement

\equiv

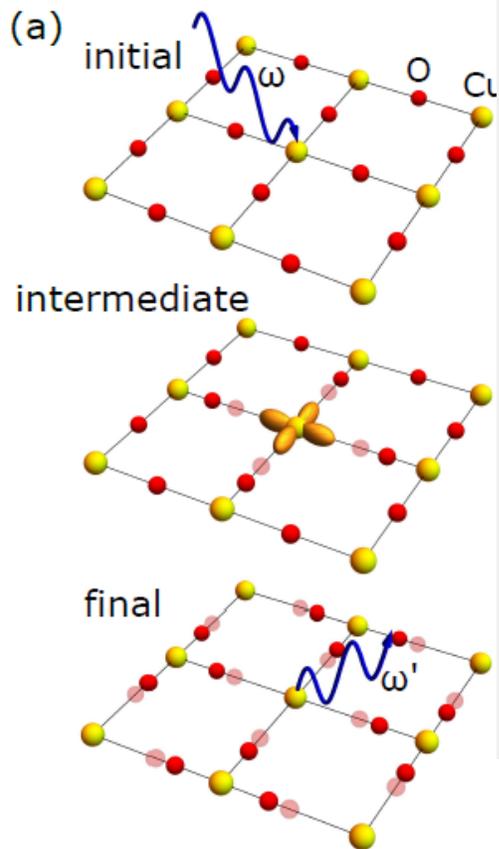
How lattice is deformed by the presence of a valence electron



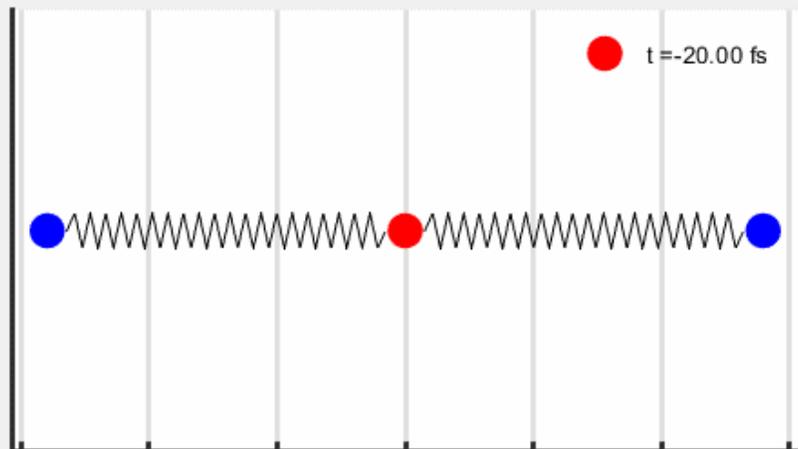
S. Gerber, S.-L. Yang, D. Zhu, H. Soifer, J. A. Sobota, S. Rebec, J. J. Lee, T. Jia, B. Moritz, C. Jia, A. Gauthier, Y. Li, D. Leuenberger, Y. Zhang, L. Chaix, W. Li, H. Jang, J.-S. Lee, M. Yi, G. L. Dakovski, S. Song, J. M. Glownia, S. Nelson, K. W. Kim, Y.-D. Chuang, Z. Hussain, R. G. Moore, T. P. Devereaux, W.-S. Lee, P. S. Kirchmann, and Z.-X. Shen, *Science* **357**, 71(2017)

Measuring EPC with RIXS: mechanism

Theory by Ament, van den Brink



Harmonic oscillator analogy



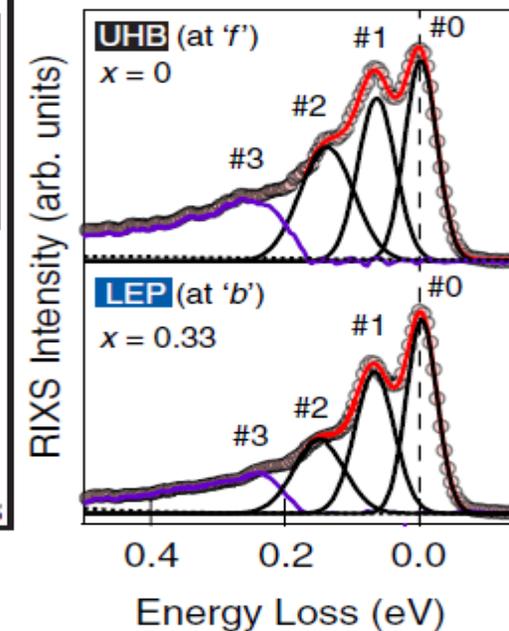
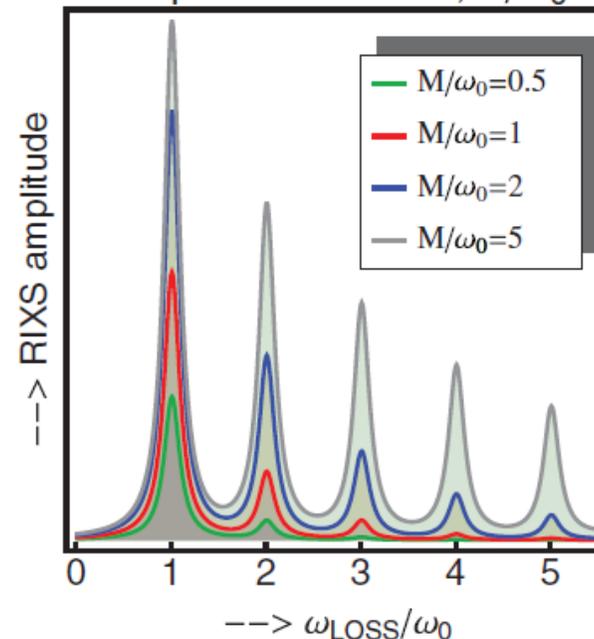
Phonon peak intensity grows with:

- EPC, i.e., M or $g = (M/w_0)^2$
- Intermediate state lifetime

2ph, 3ph peaks

Application to 1D system (O K edge)

RIXS phonon losses, $\Gamma/\omega_0=5$



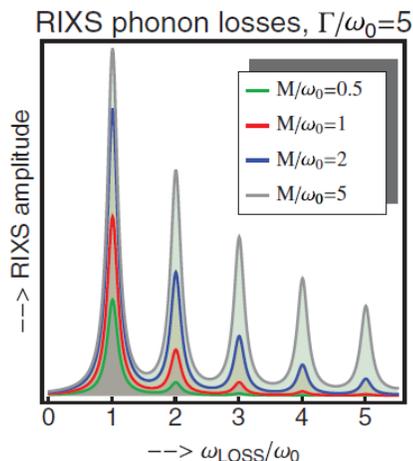
Matteo Rossi, Riccardo Arpaia, Roberto Fumagalli, Marco Moretti Sala, Davide Betto, Gabriella M. De Luca, Kurt Kummer, Jeroen van den Brink, Marco Salluzzo, Nicholas B. Brookes, Lucio Braicovich, Giacomo Ghiringhelli, [PRL 123, 027001 \(2019\)](#)

L. J. P. Ament, M. van Veenendaal and J. van den Brink, [EPL 95 \(2011\) 27008](#)

W-S Lee et al, [PRL 110, 265502 \(2013\)](#)

Phonons in RIXS spectra

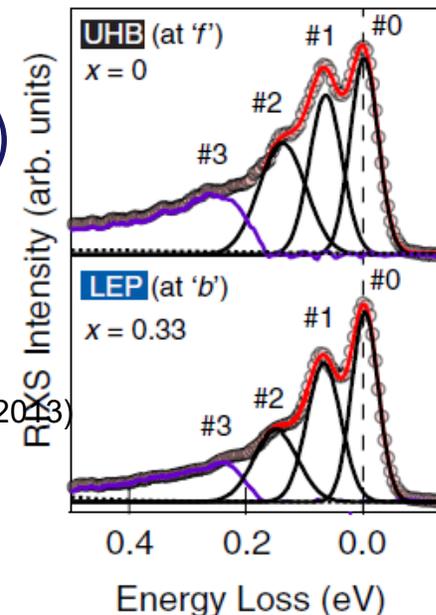
Signal is directly related to $e-ph$ interaction



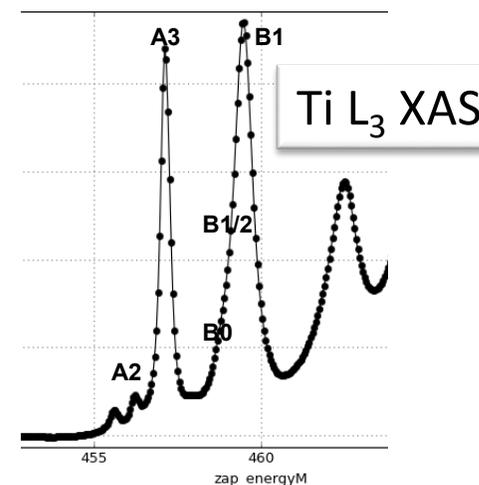
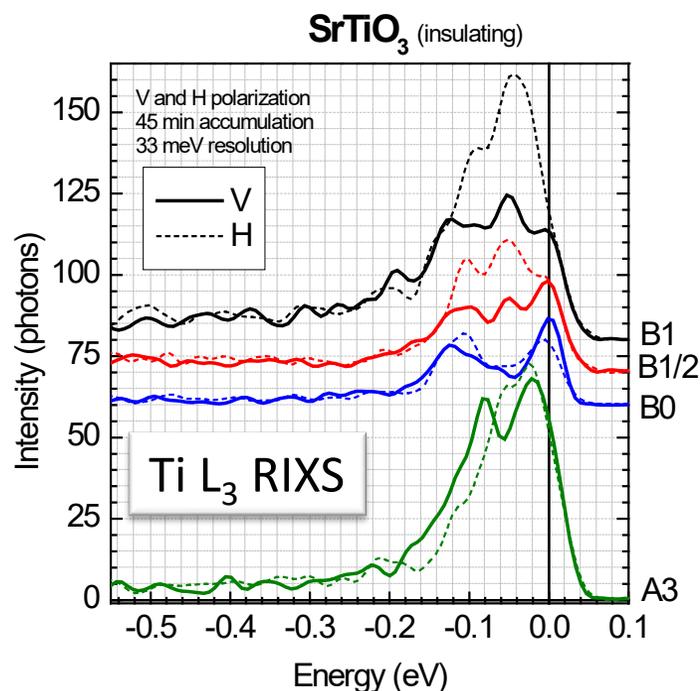
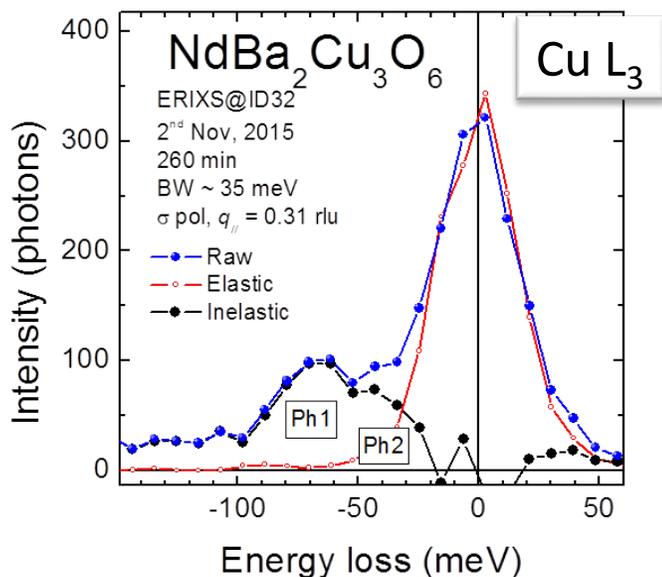
Theory

L. J. P. Ament, M. van Veenendaal and J. van den Brink, EPL **95** (2011) 27008

Application to 1D system (O K edge)



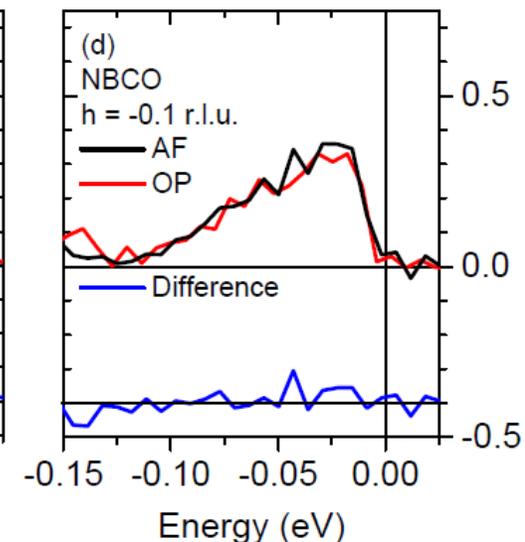
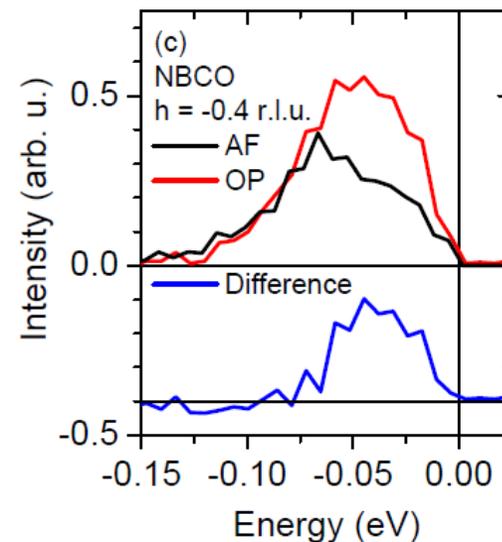
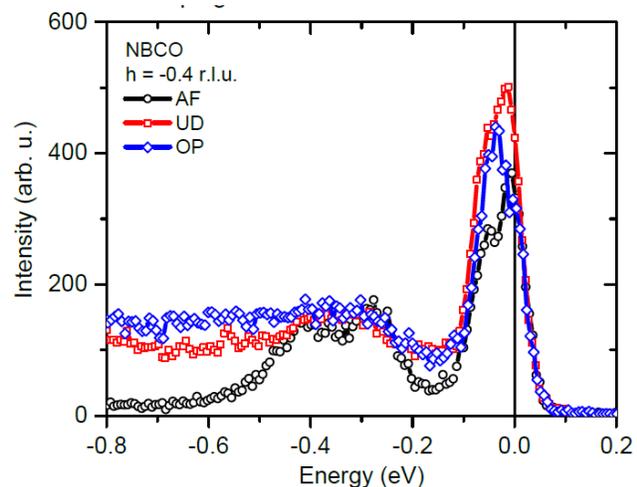
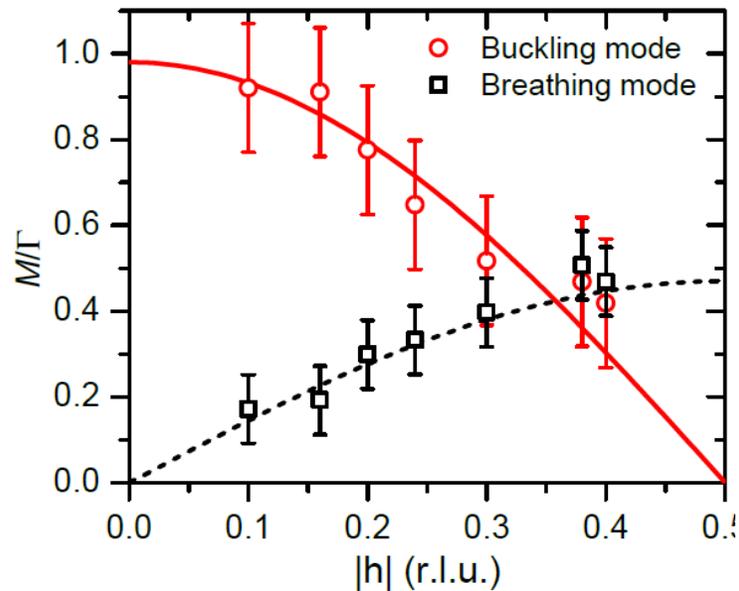
W-S Lee et al, PRL **110**, 265502 (2013)



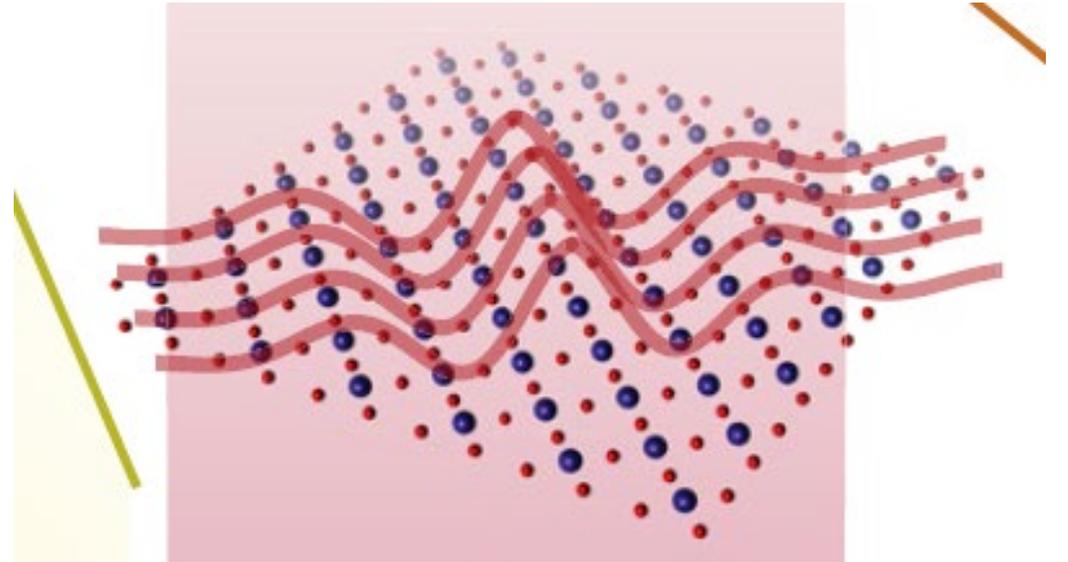
EPC in $\text{NdBa}_2\text{Cu}_3\text{O}_{7-\delta}$

Doping dependence: interplay with CDW at large q in (10)

q dependence



Lucio Braicovich, Matteo Rossi, Roberto Fumagalli, Yingying Peng, Yan Wang, Riccardo Arpaia, Davide Betto, Gabriella M. De Luca, Daniele Di Castro, Kurt Kummer, Marco Moretti Sala, Mattia Pagetti, Giuseppe Balestrino, Nicholas B. Brookes, Marco Salluzzo, Steven Johnston, Jeroen van den Brink, Giacomo Ghiringhelli, *Phys. Rev. Research* **2**, 023231 (2020)

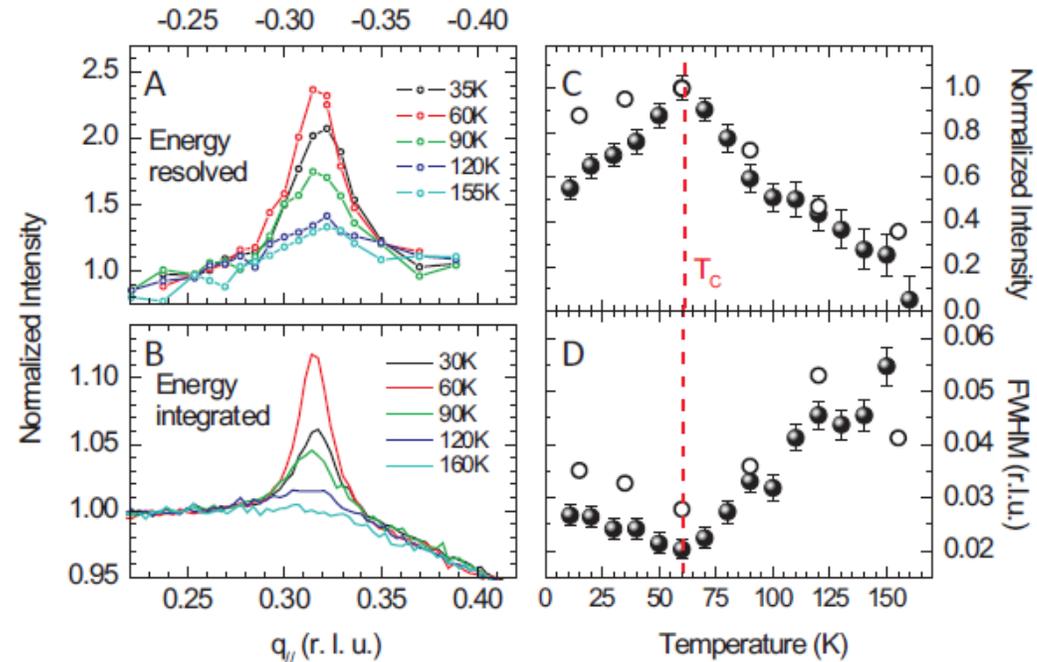
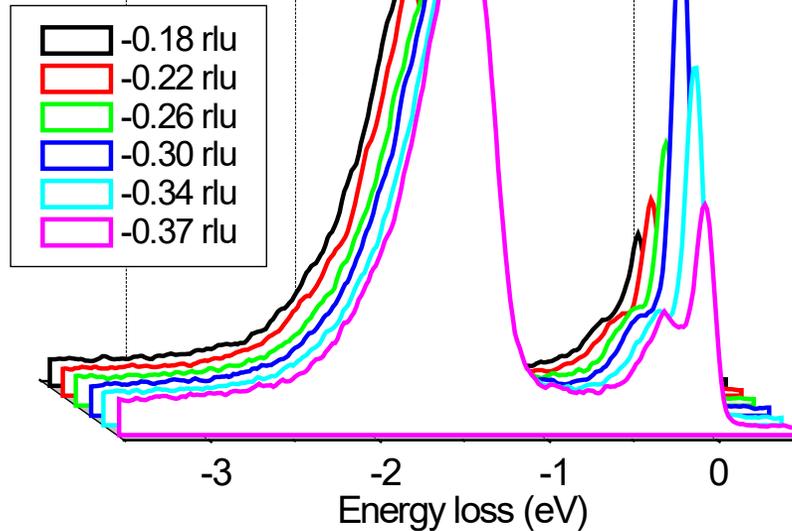


Part 5

CHARGE ORDER AND CHARGE DENSITY FLUCTUATIONS

First observation of CDW in YBCO with R(I)XS

NBCO $T_c=65K$
V pol, $T=15K$



G. Ghiringhelli, M. Le Tacon, M. Minola, S. Blanco-Canosa, C. Mazzoli, N.B. Brookes, G.M. De Luca, A. Frano, D. G. Hawthorn, F. He, T. Loew, M. Moretti Sala, D.C. Peets, M. Salluzzo, E. Schierle, R. Sutarto, G. A. Sawatzky, E. Weschke, B. Keimer, L. Braicovich, *Science* **337**, 821 (2012)

Other evidences of CDW in YBCO

NMR, Charge modulation
at low T, high field

Wu et al. *Nature* **477** 191 (2011)

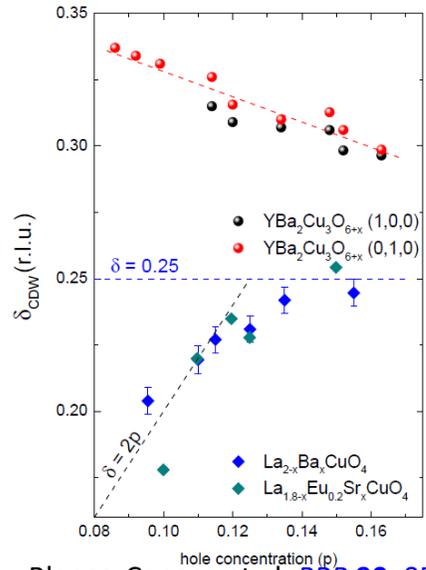
$L = 0.5$: Doubling of unit cell along c-axis
Field enhancement of the CDW (HXRDX)

Chang et al. *Nat.Phys.* **8** 871 (2012)

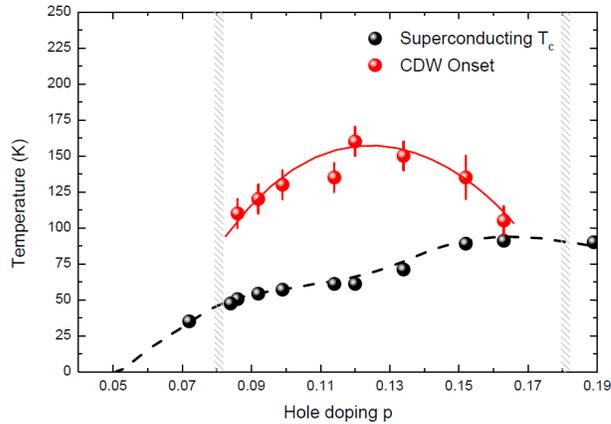
Bi-axial, Static order
under high field.

Leboeuf et al. *Nat.Phys.* **9** 79 (2013)

Ubiquitous CDW in cuprates



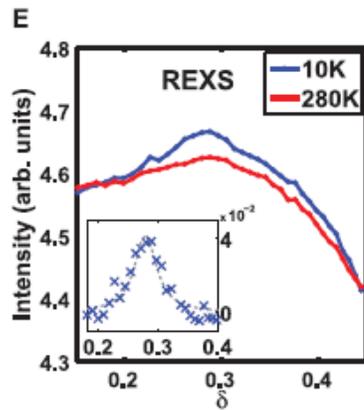
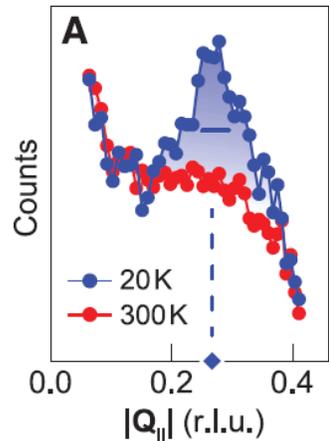
YBCO



Blanco-Canosa et al. *PRB* **90**, 054513 (2014)

Huecker et al. *PRB* **90**, 054514 (2014)

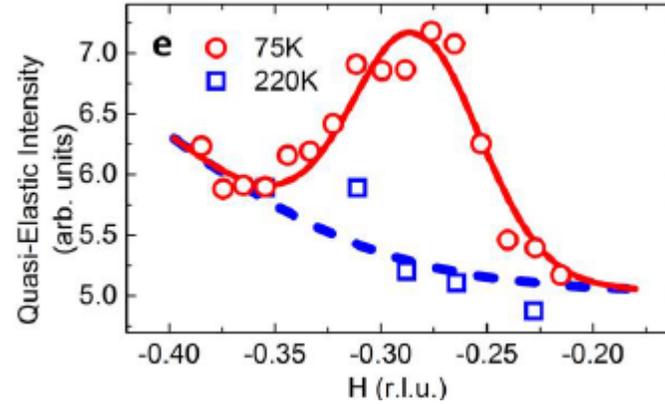
Bi2201 and Bi2212 underdoped



R. Comin et al, *Science* **343**, 390 (2014);

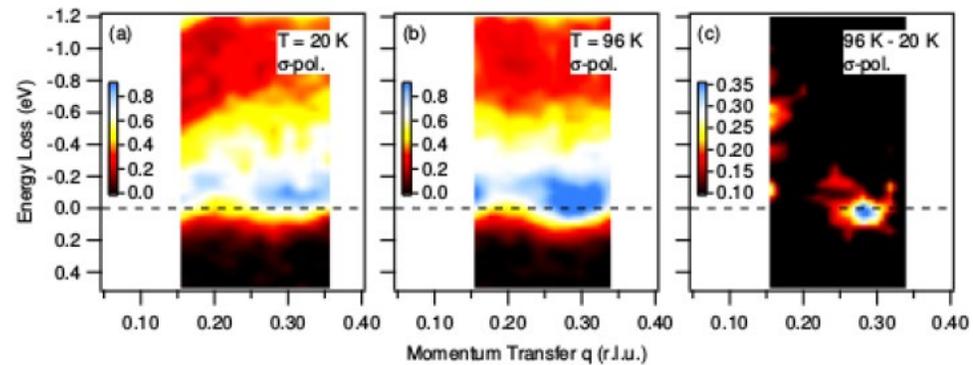
Eduardo H. da Silva Neto et al, *Science* **343**, 393 (2014)

Hg1201 underdoped



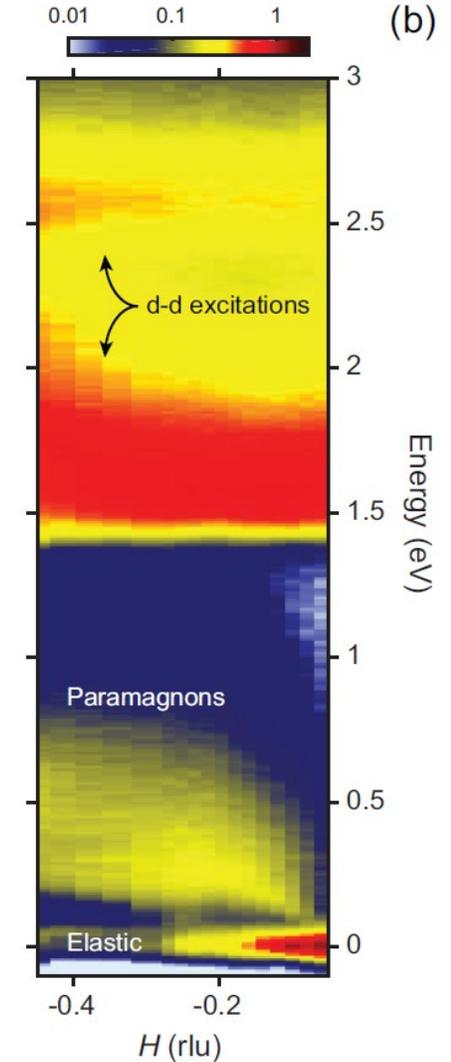
W. Tabis et al, *Nat. Comm.* **5**, 5875 (2014)

Bi2212 optimally doped



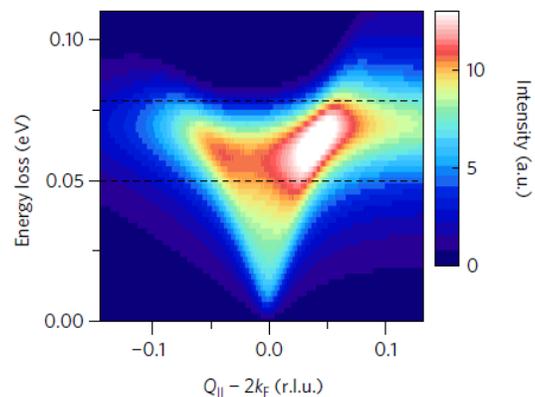
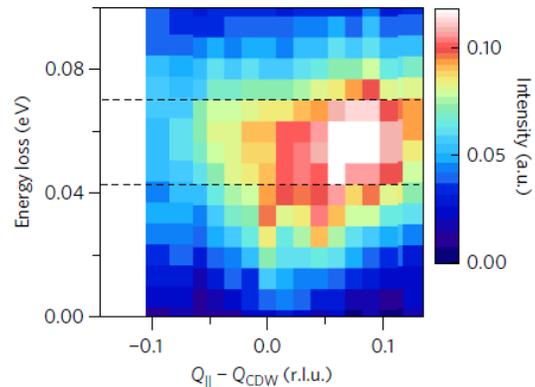
M. Hashimoto, G. Ghiringhelli et al, *PRB Rapid* **89** 220511 (2014)

NCCO e-doped

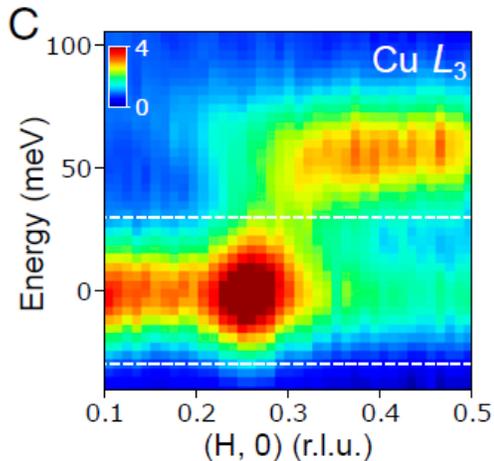


M. E. H. da Silva Neto et al, *PRB* **98** 161114 (2018)

Charge order and phonons



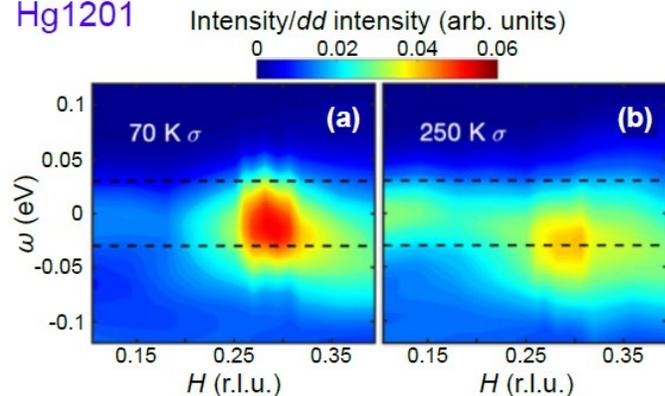
L Chaix *et al*, Nat Phys (2017)



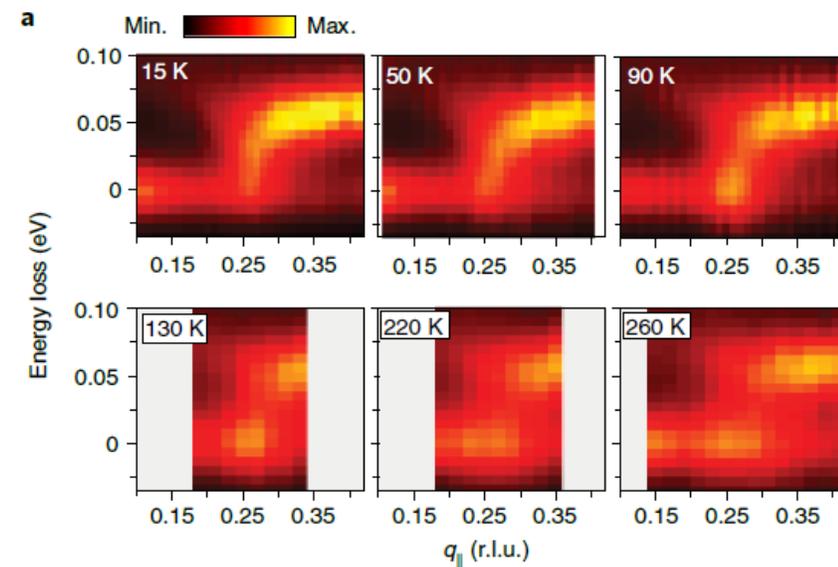
J Li *et al*, PNAS (2020)



Hg1201



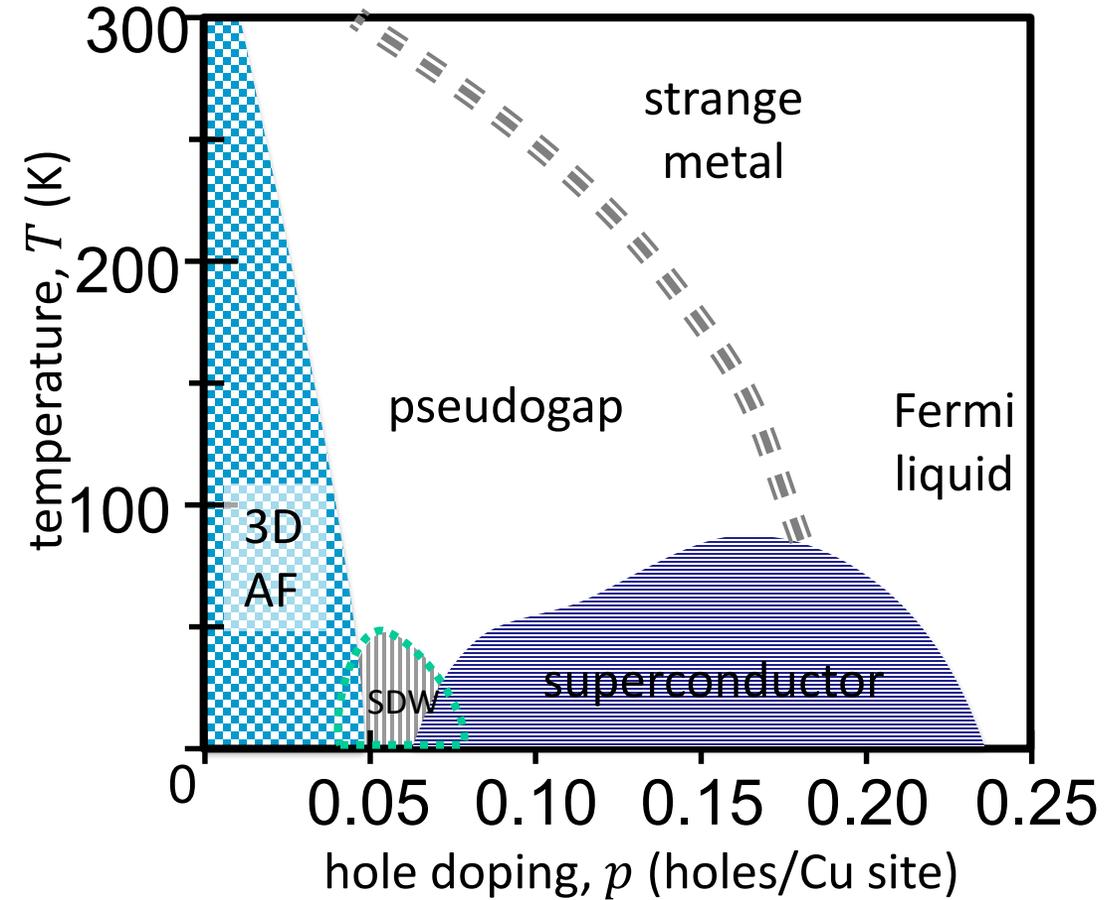
B Yu, *et al*. PRX. (2020)



WS Lee *et al*, Nat Phys (2021)

The RIXS phase diagram of cuprates

Before RIXS, circa 2007



← in plane AF correlation length

